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(on leave from IF-UNAM)

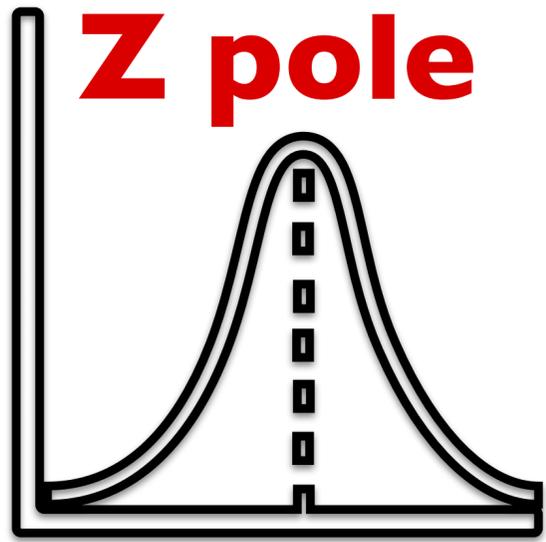
Fundamental Parameters from Electroweak Fits

Workshop on
Determination of Fundamental QCD Parameters
ICTP–SAIFR, São Paulo, September 30–October 4, 2019

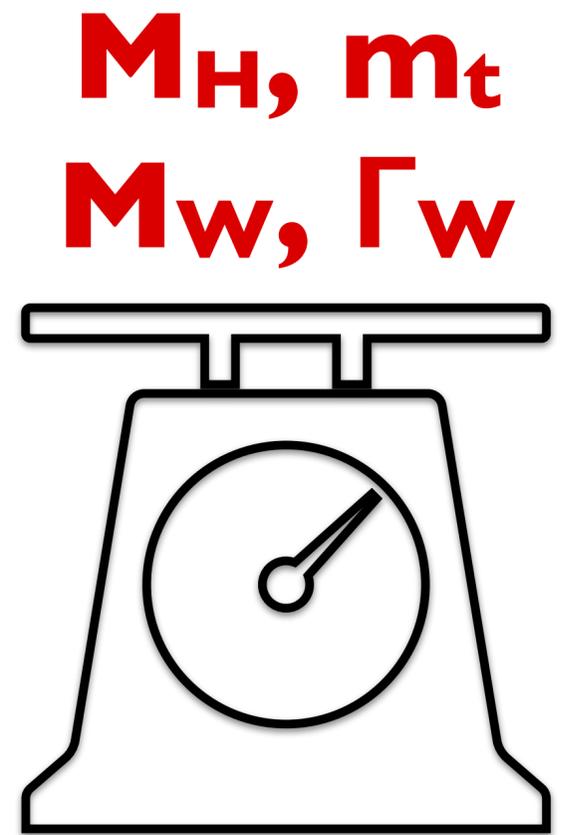
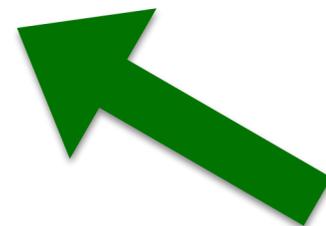
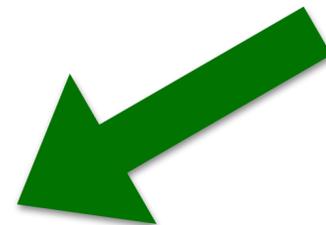
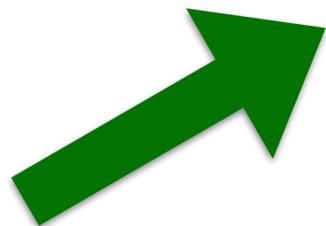
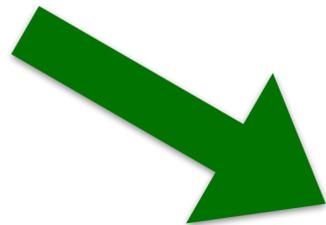
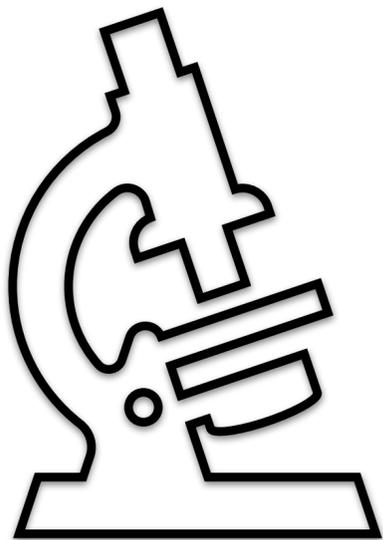


Cluster of Excellence
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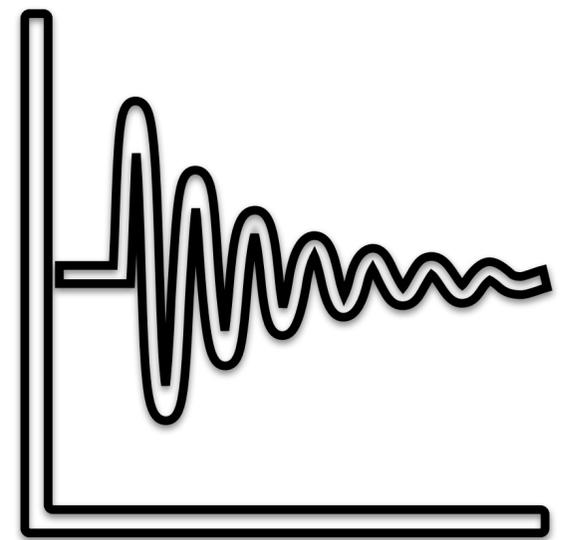
Precision Physics, Fundamental Interactions
and Structure of Matter



**low-energy
precision**



$m_c, m_b, \Delta\alpha\dots$



Global electroweak fits

- * *Various groups, programs, approaches, renormalization schemes:*
 - * *GAPP* ($\overline{\text{MS}}$ scheme, FORTRAN, options for BSM fits, used for [PDG](#))
JE, hep-ph/0005084
 - * *Gfitter* (on-shell scheme, C++)
Flächer et al., arXiv:0811.0009
 - * *HEPfit* (on-shell scheme, allows fit to Wilson coefficients)
de Blas et al., arXiv:1608.01509
 - * *ZFITTER* (on-shell scheme, FORTRAN, used for [LEPEWWG](#))
Bardin et al., hep-ph/9412201

Outline

- * $\sin^2\theta_W$

- * news on $A_{\text{FB}}(b)$ and APV

- * Tevatron and LHC

- * Qweak

- * *heavy weights*

- * M_W

- * m_t

- * M_H

- * α_s

- * LEP luminosity $\rightarrow \sigma_{\text{had}} \& \Gamma_Z$

- * τ decays

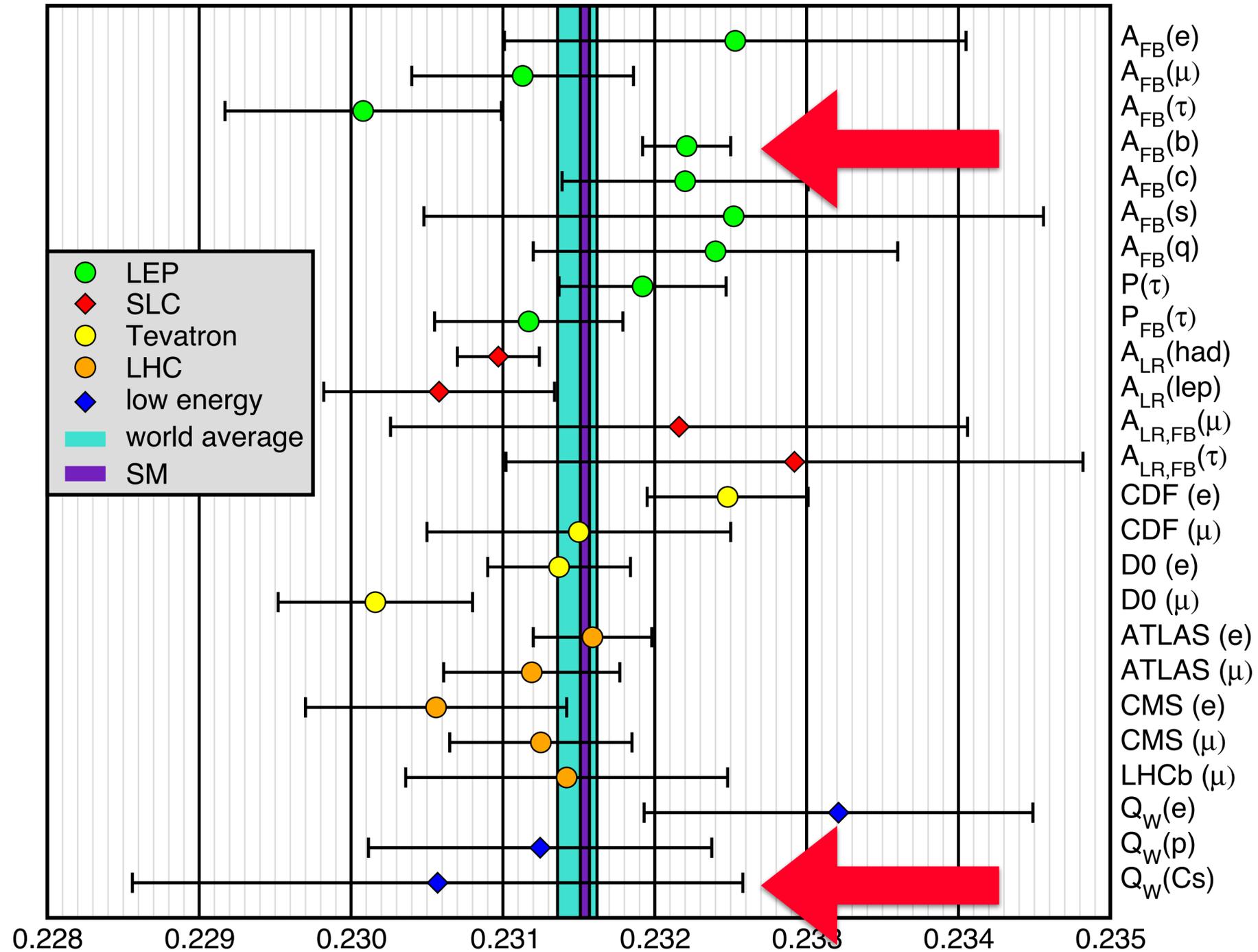
- * *outlook*

- * parity violating electron scattering

- * FCC-ee

$$\sin^2\theta_w$$

Weak mixing angle measurements



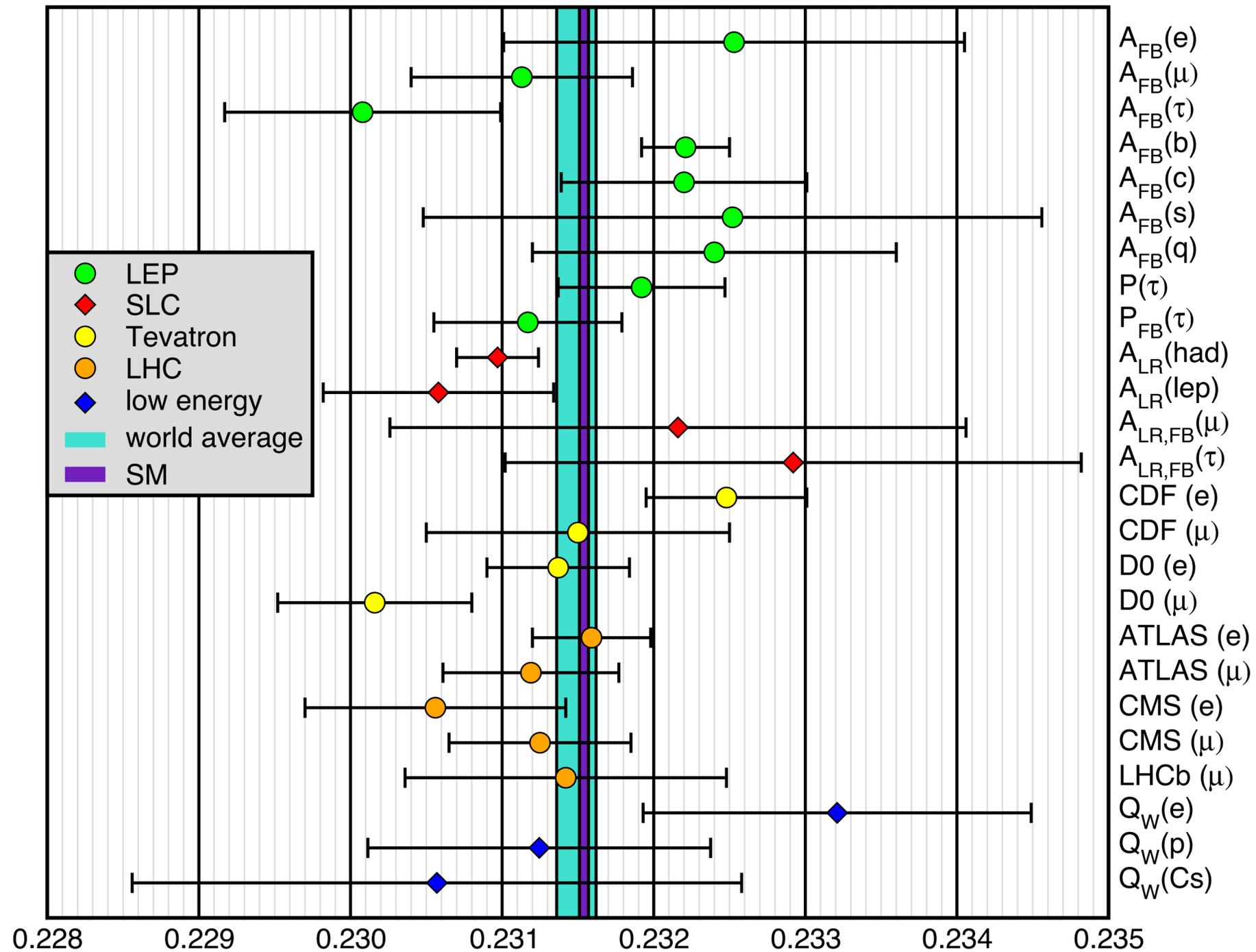
2-loop QCD correction
with $m_b \neq 0$

Bernreuther et al.
arXiv:1611.07942

new measured
transition vector polarizability

Tho et al.
arXiv:1905.02768

Weak mixing angle measurements



LEP & SLC:
 0.23153 ± 0.00016

Tevatron:
 0.23148 ± 0.00033

LHC:
 0.23131 ± 0.00033

average direct
 0.23149 ± 0.00013

global fit
 0.23153 ± 0.00004

Parity Violating e⁻ Scattering (PVES) — Elastic

Qweak @ CEBAF (JLab)

hydrogen (completed)

$$E_e = 1149 \text{ MeV}$$

$$|Q| = 158 \text{ MeV}$$

$$A_{PV} = 2.3 \times 10^{-7}$$

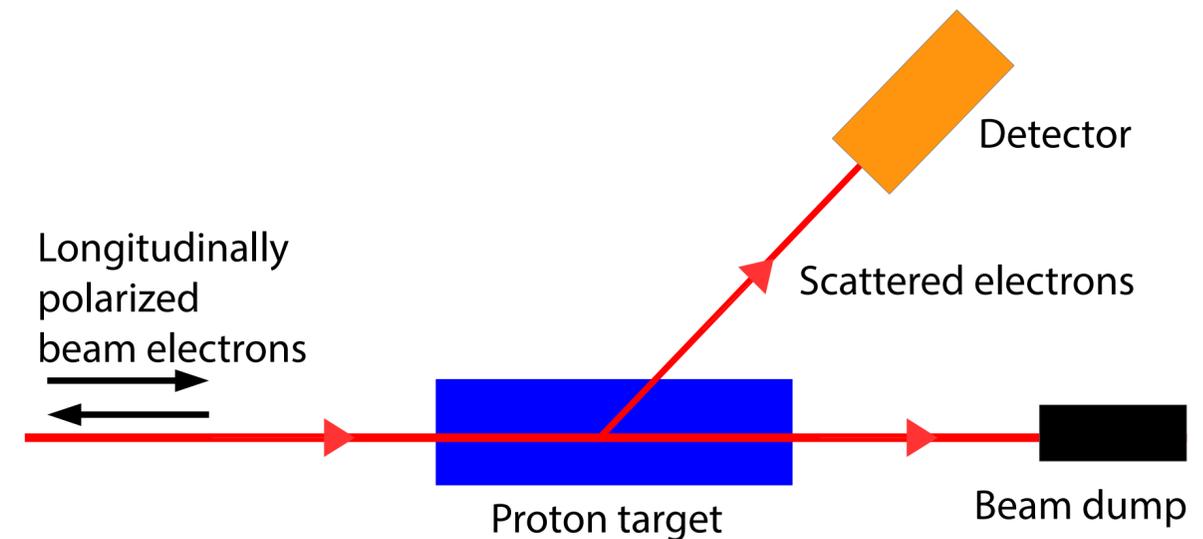
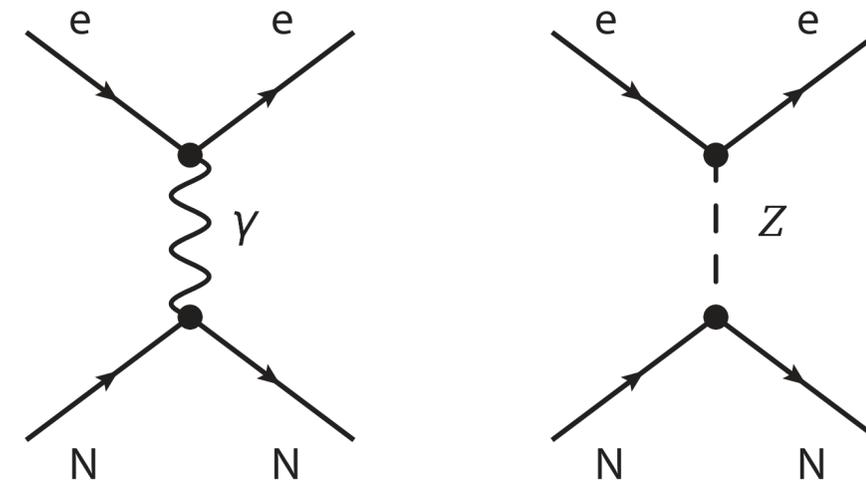
$$\Delta A_{PV} = \pm 4.1\%$$

$$\Delta Q_W(p) = \pm 6.25\%$$

$$\underline{\sin^2\theta_W = 0.2383 \pm 0.0011}$$

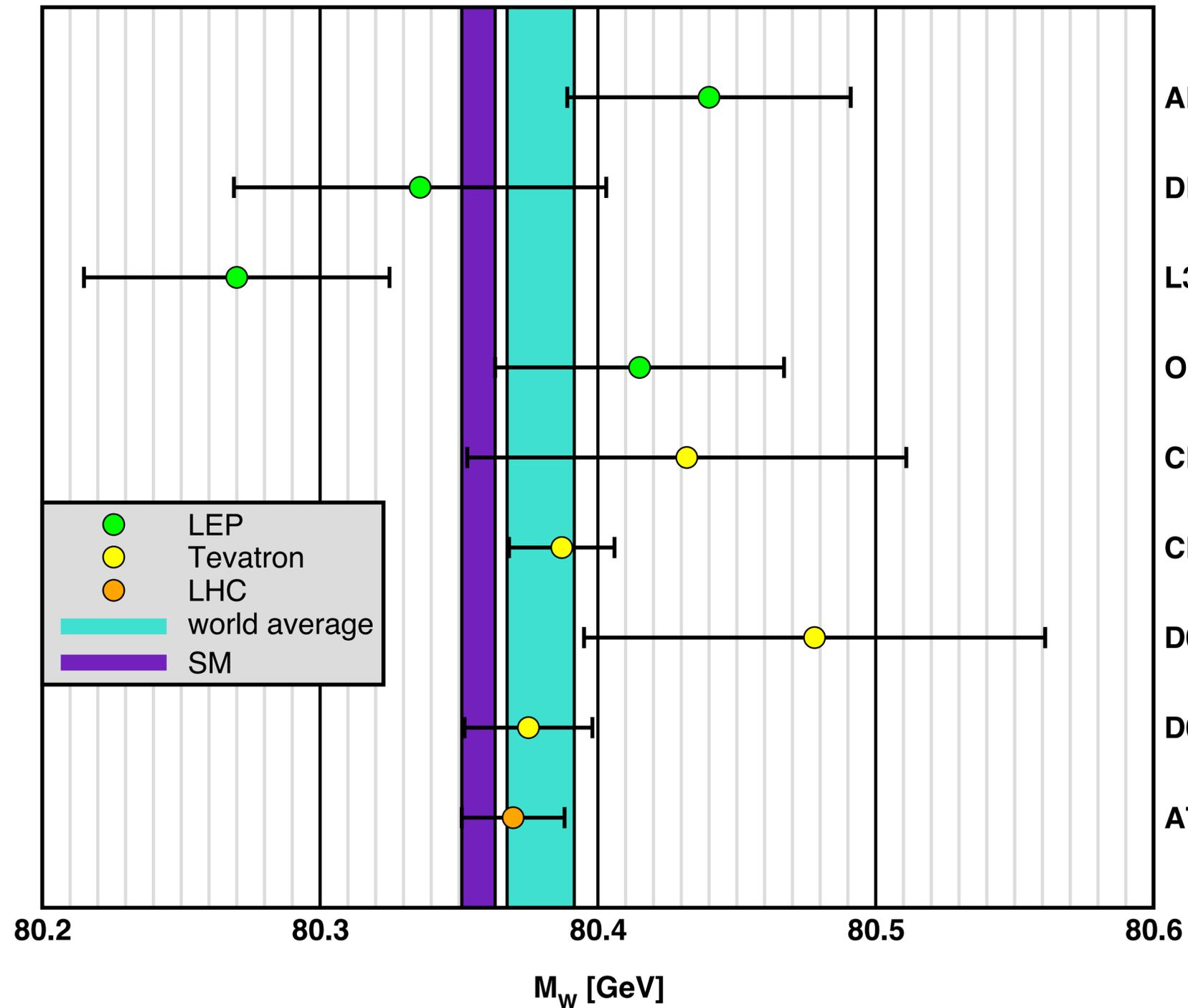
FFs from fit to ep asymmetries

[arXiv:1905.08283](https://arxiv.org/abs/1905.08283)



heavy weights

W boson mass measurements



average direct
 80.379 ± 0.012 GeV

indirect
 80.352 ± 0.006 GeV
(2.0 σ low)

including
 m_t^{pole} from X-sections

m_t^{MC} measurements

	central	statistical	systematic	total error	arXiv
Tevatron	174.30	0.35	0.54	0.64	1608.01881
ATLAS Run I	172.69	0.25	0.41	0.48	1810.01772
CMS Run I	172.43	0.13	0.46	0.48	1509.04044
CMS Run 2	172.26	0.07	0.61	0.61	1812.10534
average	172.8	0.11	0.29	0.31	

* for stat.-syst. total error separation, see [JE, arXiv:1507.08210](#)

* 2.8 σ discrepancy between lepton + jet channels from DØ and CMS Run 2

* $m_t^{\text{pole}} = 172.80 \pm 0.25_{\text{uncorr.}} \pm 0.17_{\text{corr.}} \pm 0.32_{\text{QCD}} \text{ GeV} + \Delta_{\text{MC}} = 172.80 \pm 0.44 \text{ GeV} + \Delta_{\text{MC}}$

* Δ_{MC} : **uncertainty** & non-universal **shift** (?) of order $\alpha_s(Q_0) Q_0$; $Q_0 \simeq \Gamma_t \Rightarrow \Delta_{\text{MC}} \sim 0.54 \text{ GeV}$

* for a review, see [G. Corcella, arXiv:1903.06574](#)

m_t^{pole} measurements

	X-section	m_t^{pole} (GeV)	$\alpha_s(M_Z)$	corr.	arXiv
CMS Run 2	$t\bar{t}$	170.5 ± 0.8	$0.1135^{+0.0021}_{-0.0017}$	$\rho_{\alpha,m} = 0.3$	1904.05237
ATLAS Run I	$t\bar{t} + 1\text{-jet}$	$171.1^{+1.2}_{-1.1}$	0.119 ± 0.001		1905.02302

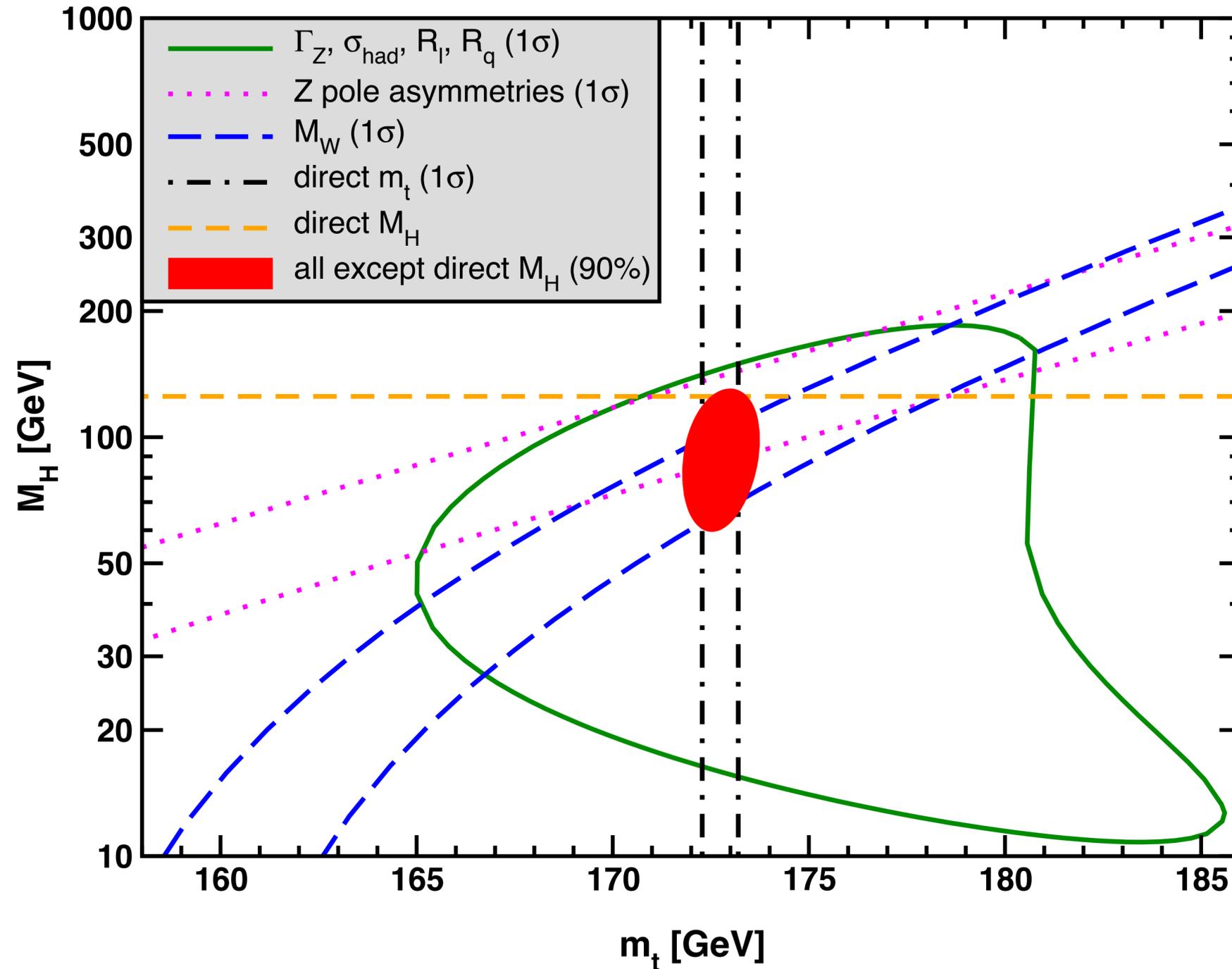
- * these are differential cross-section at NLO
- * total cross-sections currently give larger errors ≈ 2 GeV

M_H fits

	m_t (GeV)	M_H (GeV)	$\chi^2/\text{d.o.f.}$
no external m_t	$174.3^{+6.8}_{-5.6}$	102^{+83}_{-43}	37.2 / 39
$m_t^{\text{MC}} (\Delta_{\text{MC}} = 0)$	172.8 ± 0.44	89^{+18}_{-15}	37.3 / 40
$m_t^{\text{MC}} (\Delta_{\text{MC}} = 0 \pm 0.54 \text{ GeV})$	172.8 ± 0.7	89^{+19}_{-16}	37.3 / 40
$m_t^{\text{MC}} (\Delta_{\text{MC}} = 0.54 \pm 0.54 \text{ GeV})$	173.4 ± 0.7	94^{+19}_{-17}	37.2 / 40
m_t^{pole}	171.0 ± 0.6	79^{+17}_{-14}	43.7 / 42
$m_t^{\text{MC}} (\Delta_{\text{MC}} = 0 \pm 0.54 \text{ GeV}) + m_t^{\text{pole}}$	171.8 ± 0.47	85^{+17}_{-15}	47.2 / 43
$m_t^{\text{MC}} (\Delta_{\text{MC}} = 0.54 \pm 0.54 \text{ GeV}) + m_t^{\text{pole}}$	172.1 ± 0.47	87^{+17}_{-16}	49.7 / 43

in the last fit: $\alpha_s(M_Z) = 0.1175 \pm 0.0011$

$M_H - m_t$



indirect m_t
 176.4 ± 1.9 GeV
(1.9 σ high)

including
correlated theory errors

α_s

α_s from the Z pole

for massless quarks

$$R_V^q = R_A^q = 1 + \frac{\alpha_s(M_Z)}{\pi} + 1.409 \frac{\alpha_s^2}{\pi^2} - 12.77 \frac{\alpha_s^3}{\pi^3} - 80.0 \frac{\alpha_s^4}{\pi^4} + Q_q^2 \left[\frac{3}{4} - \frac{\alpha_s}{4\pi} - \left(1.106 + \frac{3}{32} Q_q^2 \right) \frac{\alpha}{\pi} \right] \frac{\alpha(M_Z)}{\pi}$$

after large (top quark driven) **singlet corrections** (Z boson only) starting at order α_s

$$\Gamma_Z^{\text{had}} \propto \rho \left(1 + \frac{\alpha_s(M_Z)}{\pi} + 0.79 \frac{\alpha_s^2}{\pi^2} - 15.52 \frac{\alpha_s^3}{\pi^3} - 69.3 \frac{\alpha_s^4}{\pi^4} \right)$$

$$\delta_{\text{PQCD}} \approx \pm \frac{\alpha_s^5}{\pi^5} \frac{(80.0)^2}{12.77\pi - 80.0\alpha_s} = \pm 6 \times 10^{-5} \implies \delta_{\text{PQCD}} \alpha_s \approx \pm 0.0002$$

$$\mathcal{O}(\alpha_s^5) + \mathcal{O}(\alpha \alpha_s^5) + \mathcal{O}(\alpha^2 \alpha_s) \implies \delta_{\text{PQCD}+\text{mixed}} \alpha_s \approx \pm 0.0004 \text{ (negligible)}$$

Schott & JE, arXiv:1902.05142

α_s from the Z pole

observable	$\alpha_s(M_Z)$	change	$\chi^2/\text{d.o.f.}$
$\Gamma_Z = 2495.5 \pm 2.3 \text{ MeV}$	0.1215 ± 0.0047	+0.0006	
$\sigma_{\text{had}} = 41.501 \pm 0.037 \text{ nb}$	0.1148 ± 0.0073	+0.0078	
$R_e = 20.804 \pm 0.050$	0.1295 ± 0.0082	—	
$R_\mu = 20.785 \pm 0.033$	0.1264 ± 0.0054	—	
$R_\tau = 20.764 \pm 0.045$	0.1157 ± 0.0072	—	
combination	0.1221 ± 0.0028	+0.0014	3.3/4
Z-pole + M_H	0.1219 ± 0.0027	+0.0012	19.1/23
global fit ex. τ decays	0.1207 ± 0.0026	+0.0012	40.4/40

change: $\Delta\sigma_{\text{had}} = -40 \text{ pb}$, $\Delta\Gamma_Z = +0.3 \text{ MeV}$ **Voutsinas et al., arXiv:1908.01704**

α_s from τ decays

$$\tau_\tau = \hbar \frac{1 - \mathcal{B}_\tau^s}{\Gamma_\tau^e + \Gamma_\tau^\mu + \Gamma_\tau^{ud}} = 290.75 \pm 0.36 \text{ fs (includes leptonic BRs)}$$

$$\Gamma_\tau^{ud} = \frac{G_F^2 m_\tau^5 |V_{ud}|^2}{64\pi^3} S(m_\tau, M_Z) \left(1 + \frac{3}{5} \frac{m_\tau^2 - m_\mu^2}{M_W^2} \right) \times$$

$$\left[1 + \frac{\alpha_s^{(3)}(m_\tau)}{\pi} + 5.202 \frac{\alpha_s^2}{\pi^2} + 26.37 \frac{\alpha_s^3}{\pi^3} + 127.1 \frac{\alpha_s^4}{\pi^4} + \frac{\hat{\alpha}^{(3)}(m_\tau)}{\pi} \left(\frac{85}{24} - \frac{\pi^2}{2} \right) + \delta_{\text{NP}} \right]$$

* charm, bottom and strange mass effects not shown but included
Larin, van Ritbergen & Vermaseren, hep-ph/9411260

* $\mathcal{B}_\tau^s = 0.0292 \pm 0.0004$ ($\Delta S = -1$) **PDG 2018**

* $S(m_\tau, M_Z) = 1.01907 \pm 0.0003$ **JE, hep-ph/0211345**

α_s from τ decays

- * $\delta_{\text{NP}} = 0.003 \pm 0.009$ (both within OPE & OPE breaking) based on (FOPT)
- * $\delta_{\text{NP}} = -0.004 \pm 0.012$ (OPAL data) **Boito et al., arXiv:1203.3146**
- * $\delta_{\text{NP}} = 0.020 \pm 0.009$ (ALEPH data) **Boito et al., arXiv:1410.3528**
- * $\delta_{\text{NP}} = -0.0064 \pm 0.0013$ (ALEPH data) **Davier et al., arXiv:1312.1501**
- * $\delta_{\text{NP}} = -0.006 \pm 0.009$ (ALEPH data) **Pich & Rodríguez-Sánchez, arXiv:1605.06830**
- * dominant error from PQCD truncation (FOPT vs. CIPT vs. geometric continuation)
 - * $\alpha_s^{(3)}(m_\tau) = 0.317^{+0.013}_{-0.011}$ (PQCD) $\pm 0.009 = 0.317^{+0.016}_{-0.014}$
 - * $\alpha_s^{(4)}(m_\tau) = 0.323^{+0.014}_{-0.011}$ (PQCD) $\pm 0.009 = 0.323^{+0.017}_{-0.014}$
 - * **$\alpha_s^{(5)}(M_Z) = 0.1184^{+0.0017}_{-0.0014}$ (PQCD) $\pm 0.0011 = 0.1184^{+0.0020}_{-0.0018}$**
 - * updated from **Luo & JE, hep-ph/0207114** in **Freitas & JE, PDG 2018**
 - * **global electroweak fit: $\alpha_s^{(5)}(M_Z) = 0.1192^{+0.0017}_{-0.0015}$ (m_t^{MC} only)**

N_ν

	from σ_{had}	global fit	development
2006	2.984 ± 0.008 LEPEWWG hep-ex/0509008	2.986 ± 0.007	CIPT for τ_τ
2010		2.991 ± 0.007	FOPT for τ_τ
2014		2.990 ± 0.007	Higgs discovery
2019	2.992 ± 0.008 Voutsinas et al. arXiv:1908.01704	2.998 ± 0.007	luminosity update
		3.001 ± 0.007	precise $t\bar{t}$ X-sections

Global electroweak fit (incl. m_t^{pole} from X-sections)

M_H	$125.14 \pm 0.15 \text{ GeV}$			
M_Z	$91.1884 \pm 0.0020 \text{ GeV}$			
$\bar{m}_b(\bar{m}_b)$	$4.180 \pm 0.021 \text{ GeV}$			
$\Delta\alpha_{\text{had}}^{(3)}(2 \text{ GeV})$	$(59.0 \pm 0.5) \times 10^{-4}$			
$\bar{m}_t(\bar{m}_t)$	$162.53 \pm 0.43 \text{ GeV}$	1.00	-0.04	-0.10
$\bar{m}_c(\bar{m}_c)$	$1.272 \pm 0.009 \text{ GeV}$	-0.04	1.00	0.35
$\alpha_s(M_Z)$	0.1173 ± 0.0011	-0.10	0.35	1.00

$$\chi^2/\text{d.o.f.} = 51.9/44$$

outlook

Parity Violating e⁻ Scattering (PVES) — Elastic

Qweak @ CEBAF (JLab)

hydrogen (completed)

$$E_e = 1149 \text{ MeV}$$

$$|Q| = 158 \text{ MeV}$$

$$A_{PV} = 2.3 \times 10^{-7}$$

$$\Delta A_{PV} = \pm 4.1\%$$

$$\Delta Q_W(p) = \pm 6.25\%$$

$$\underline{\sin^2\theta_W = 0.2383 \pm 0.0011}$$

FFs from fit to ep asymmetries

[arXiv:1905.08283](https://arxiv.org/abs/1905.08283)

P2 @ MESA (JGU Mainz)

hydrogen (CDR)

$$E_e = 155 \text{ MeV}$$

$$|Q| = 68 \text{ MeV}$$

$$A_{PV} = 4 \times 10^{-8}$$

$$\Delta A_{PV} = \pm 1.4\%$$

$$\Delta Q_W(p) = \pm 1.83\%$$

$$\Delta \sin^2\theta_W = \pm 0.00033$$

FFs from backward angle data

[arXiv:1802.04759](https://arxiv.org/abs/1802.04759)

Parity Violating e⁻ Scattering (PVES) — Møller

E158 @ SLC (SLAC)

hydrogen (completed)

$$E_e = 45 \text{ \& \ 48 GeV}$$

$$|Q| = 161 \text{ MeV}$$

$$A_{PV} = 1.31 \times 10^{-7}$$

$$\Delta A_{PV} = \pm 13\%$$

$$\Delta Q_W(e) = \pm 13\%$$

$$\underline{\sin^2\theta_W = 0.2397 \pm 0.0013}$$

[hep-ex/0504049](https://arxiv.org/abs/hep-ex/0504049)

MOLLER @ CEBAF (JLab)

hydrogen (proposal)

$$E_e = 11.0 \text{ GeV}$$

$$|Q| = 76 \text{ MeV}$$

$$A_{PV} = 3.3 \times 10^{-8}$$

$$\Delta A_{PV} = \pm 2.4\%$$

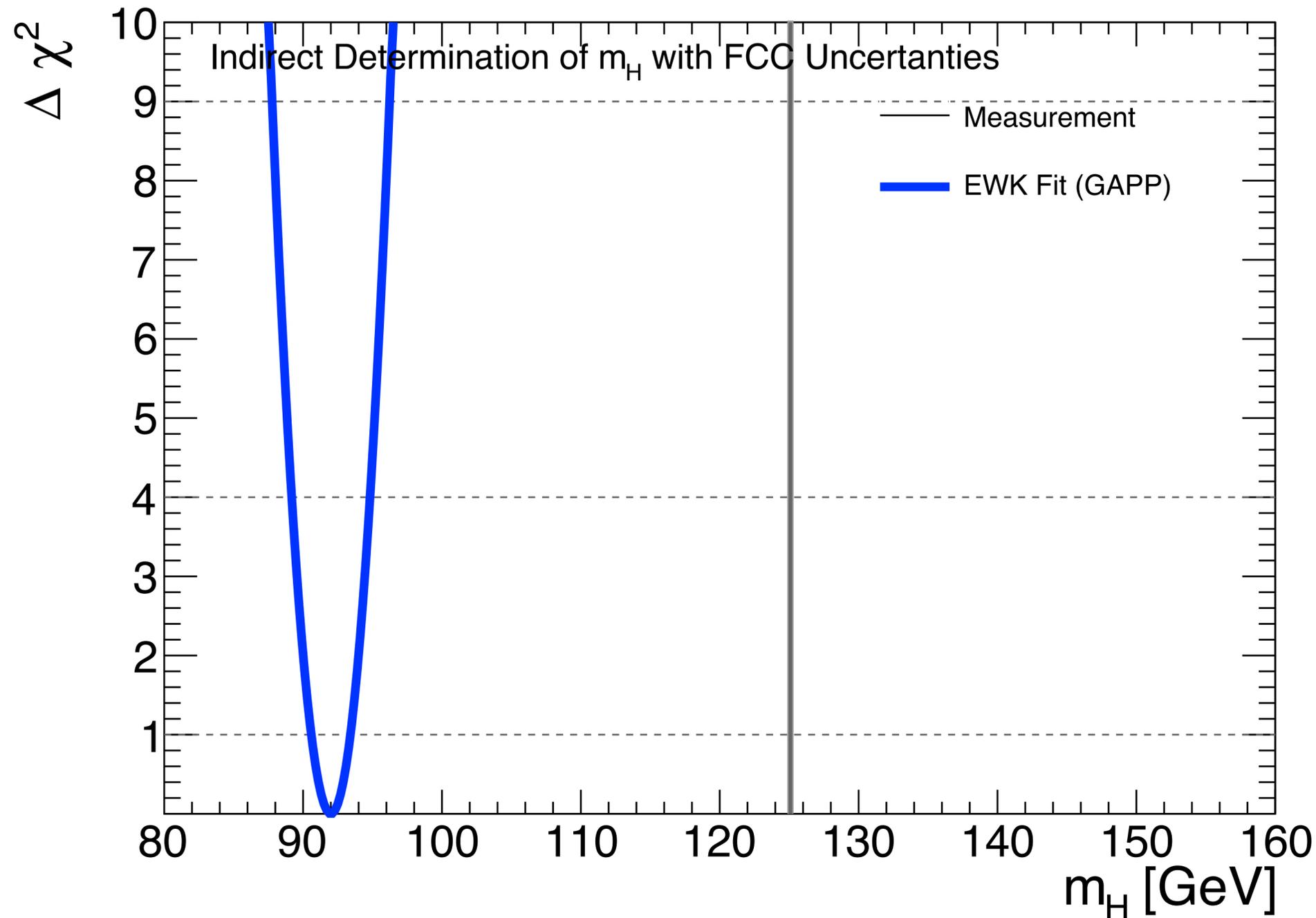
$$\Delta Q_W(e) = \pm 2.4\%$$

$$\Delta \sin^2\theta_W = \pm 0.00027$$

[arXiv:1411.4088](https://arxiv.org/abs/1411.4088)



M_H at the FCC-ee



indirect

$$\Delta M_H = \pm 1.4 \text{ GeV}$$

$$\Delta M_W = \pm 0.2 \text{ MeV}$$

(theory errors ignored)

Blondel et al.
arXiv:1905.05078

Summary

- * *new developments:*

- * changes in $A_{\text{FB}}(b)$ from LEP and $Q_{\text{W}}(Cs)$ from APV
- * high precision PVES
- * LEP luminosity update
- * precise m_t from $t\bar{t}$ production X-sections

- * *future developments:*

- * ultra-high precision PVES (MOLLER and P2)
- * a leap in precision is to be expected from future lepton colliders