

Exothermic self-interacting dark matter



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Based on HML, 2006.13183 ;

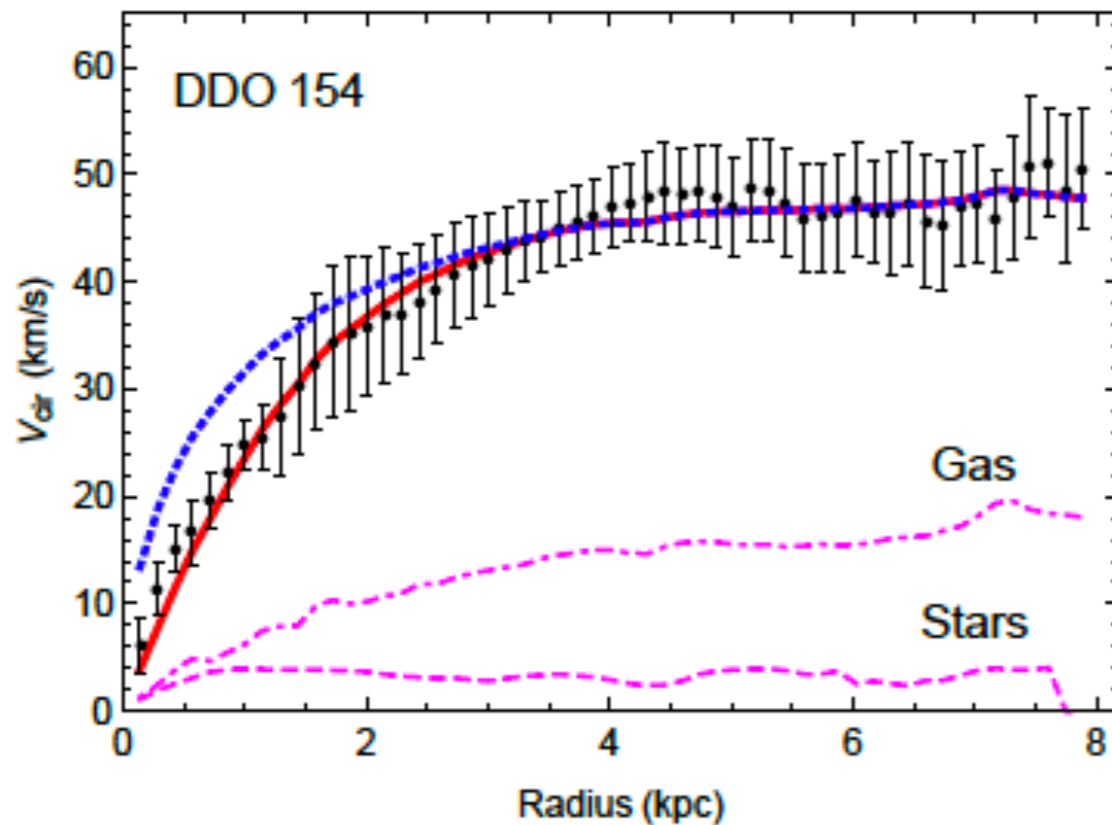
S.-M. Choi, HML, B. Zhu, to appear.

Outline

- Introduction
- Exothermic dark matter
- Microscopic models
- Conclusions

Core-Cusp problem

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Circular velocities:

$$v_{\text{cir}} \sim \sqrt{r}, \quad \rho_{\text{dm}} \sim r^{-1} \quad \text{“Cuspy”}$$

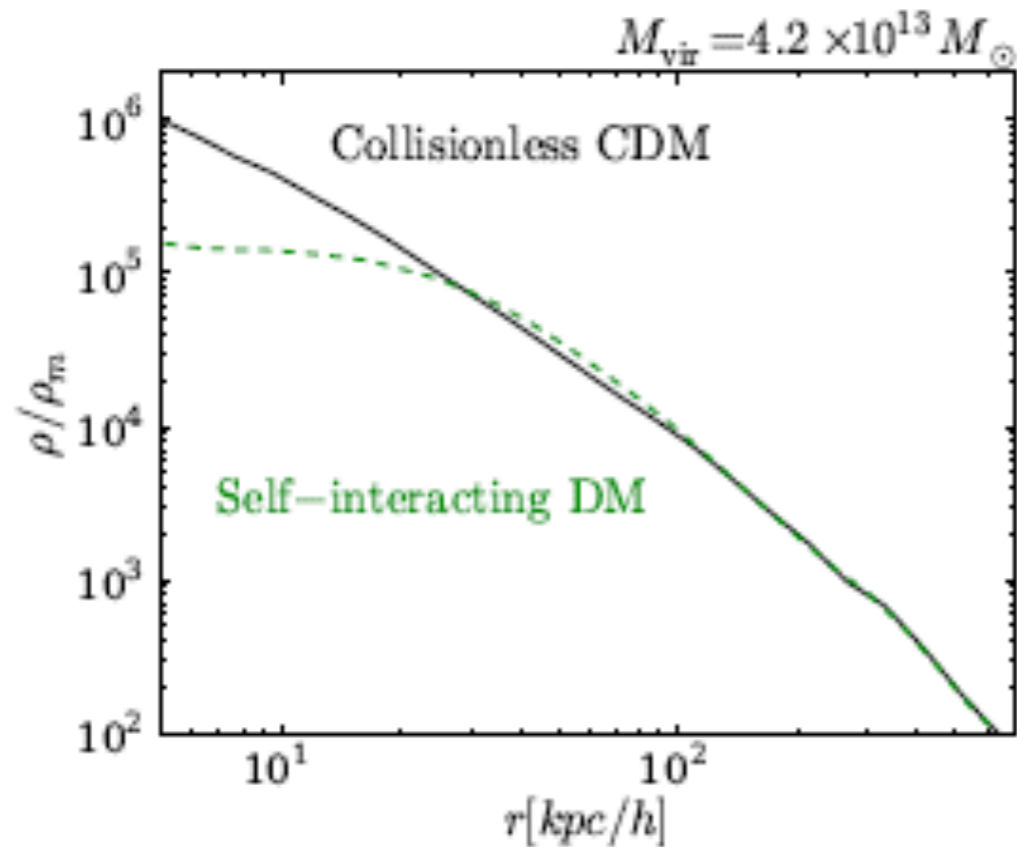
$$v_{\text{cir}} \sim r, \quad \rho_{\text{dm}} \sim r^0 \quad \text{“Cored”}$$

Overshoot at <1 kpc [Spergel, Steinhardt, 2000; Tulin, Yu, 2017]

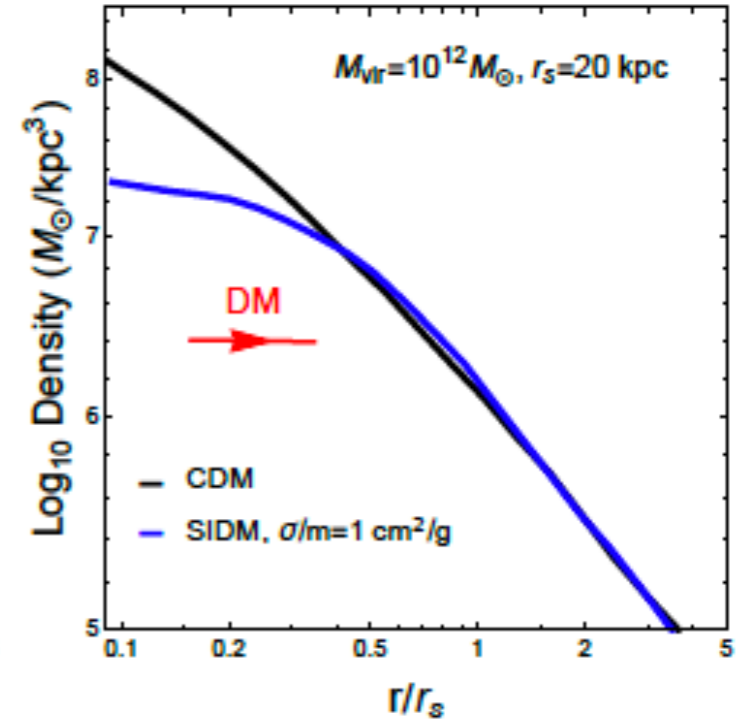
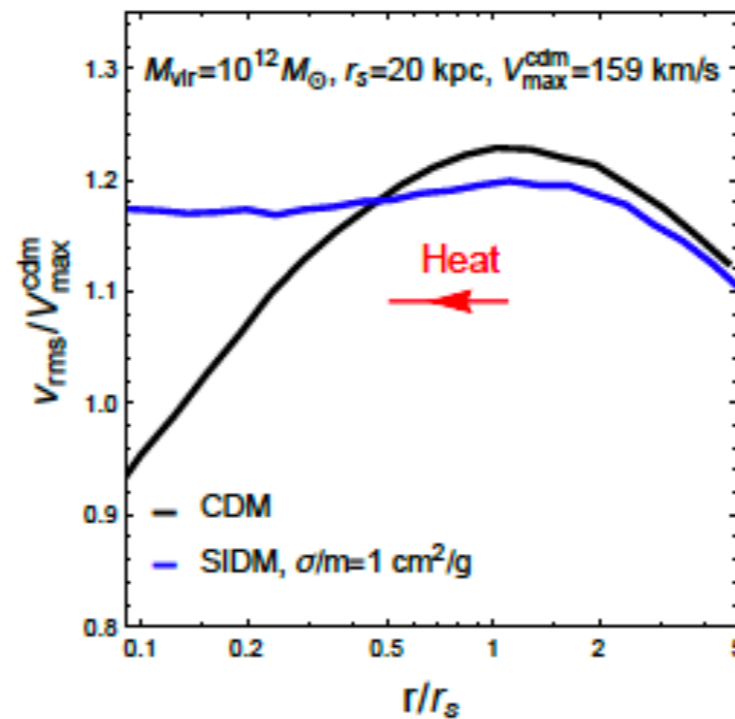
- **Core-Cusp problem:** CDM N-body simulation predicts cuspy DM profile (NFW), rendering rotation velocities larger at small scales (\rightarrow cored DM profile favored).

cf. Too-big-to-fail, Diversities for the same halo mass.

Self-Interacting dark matter -2-

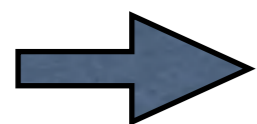


[Weinberg et al, 2013]



[Tulin, Yu, 2017]

Transport heat from outside makes DM profile cored.



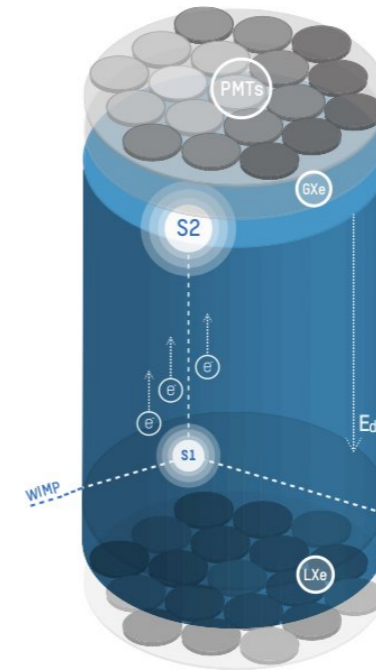
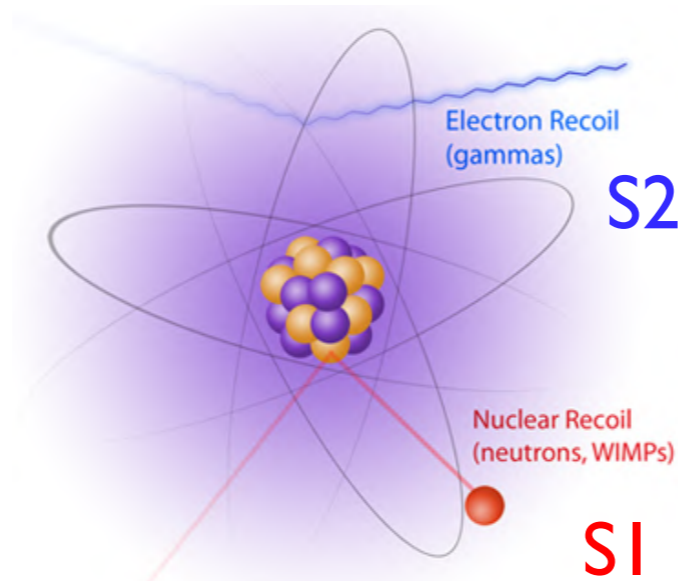
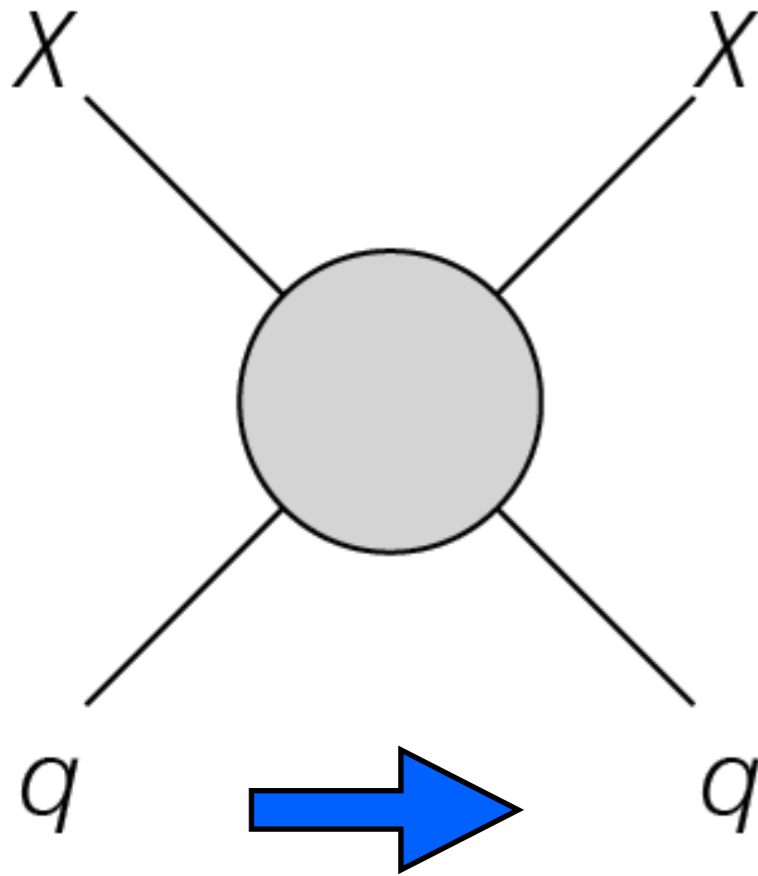
Self-Interacting cross section:

$$\frac{\sigma_{\text{self}}}{m_{\text{DM}}} \sim 0.1 - 10 \text{ cm}^2/\text{g}$$

cf. Baryons (SN feedback).

But, Bullet cluster bounds DM self-scattering. $\sigma/m \lesssim 0.7 \text{ cm}^2/\text{g}$

Dark matter detection -4-



e.g. XENONIT
S1: Scintillation (photons)
S2: Ionization (electrons)
 WIMP:
 $S1/S2 \gg (S1/S2)_Y$

Nucleus recoil E: $E_R = \frac{\vec{q}^2}{2m_N} = \frac{(\mu v)^2}{m_N} \lesssim 50\text{keV}$

Event rate: $\frac{dR}{dE_R} = \frac{\rho_\odot}{m_{\text{DM}}} \left\langle \frac{d\sigma}{dE_R} v \right\rangle \sim 1 \text{ event/kg/day}$

Experiment (Nucleus)	Z	A
LUX (Xe)	54	129
XENON1T (Xe)	54	131
PandaX-II (Xe)	54	136
SuperCDMS (Ge)	32	73
CDMSlite (Ge)	32	73
XENON10 (Xe)	54	131
DarkSide-50 (Ar)	18	39

Light dark matter such as SIDM

➔ Too small recoil energy below threshold.

Light DM detection

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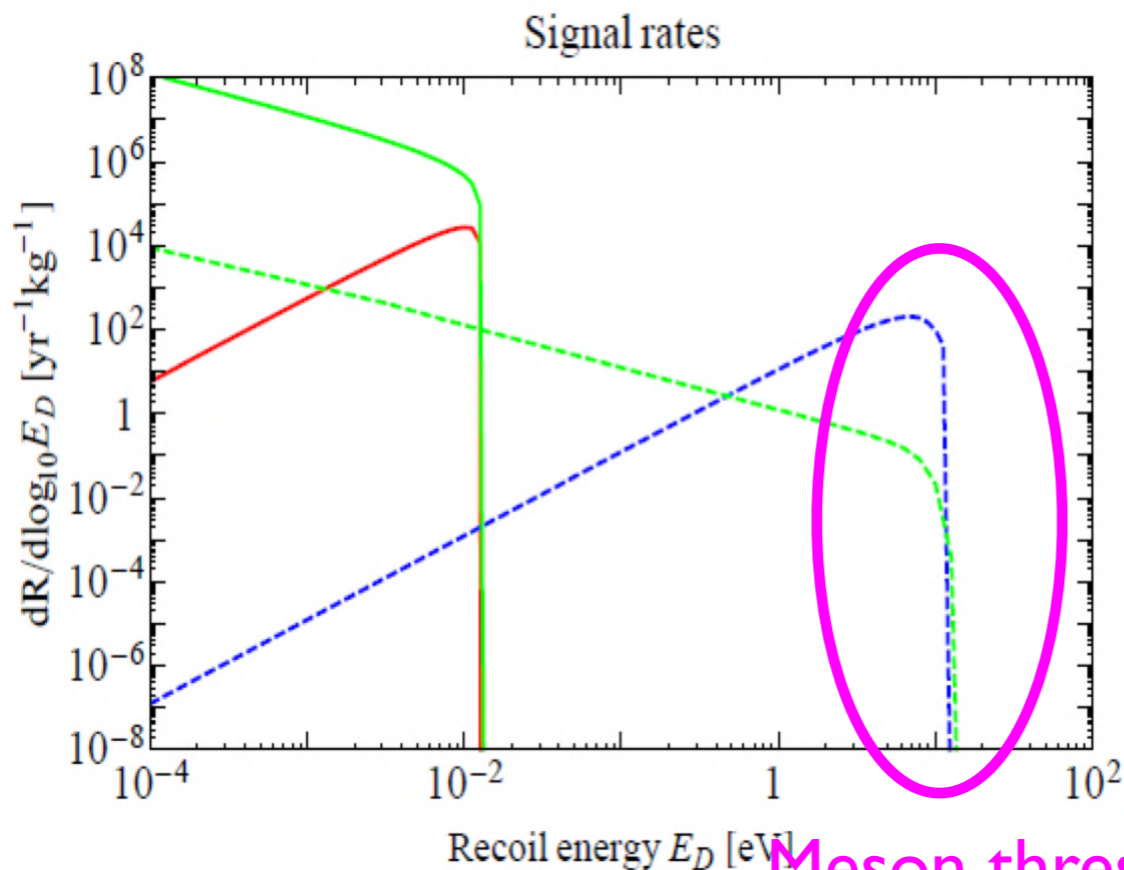
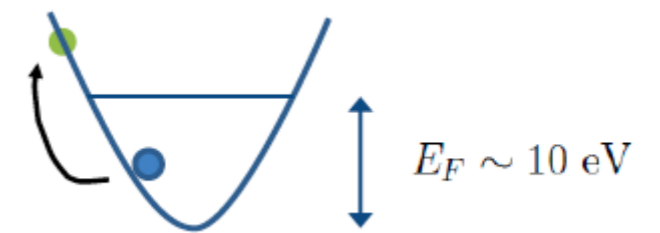
- DM-nucleon scattering => cryogenic semi-conductors.
e.g. CDMSlite: Ge, $E_{th}=56\text{eV}$ \longrightarrow $m_{\text{DM}} \gtrsim 1.6 \text{ GeV}$
- DM-electron scattering (semi-conductor, superconductor)

$$m_{\text{DM}} v^2 \gtrsim \Delta \sim \text{meV}$$

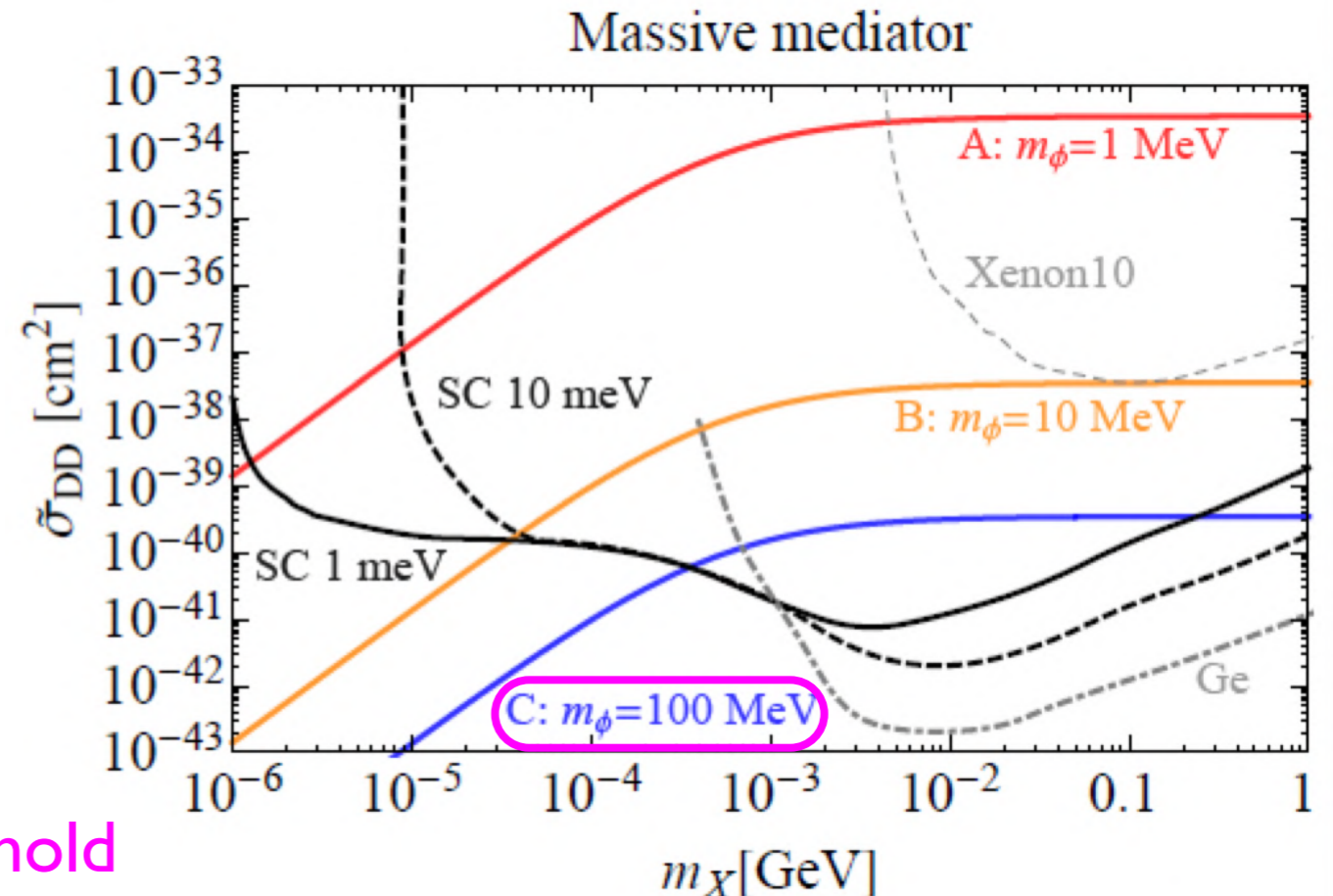
$$m_{\text{DM}} \gtrsim m_e : E_R \lesssim 20 \text{ eV}$$

e.g. Al: $E_F = 11.7 \text{ eV}$, $v_{\text{rel}} \sim v_F \sim 10^{-2}$

[Hochberg et al (2015)]



Meson threshold

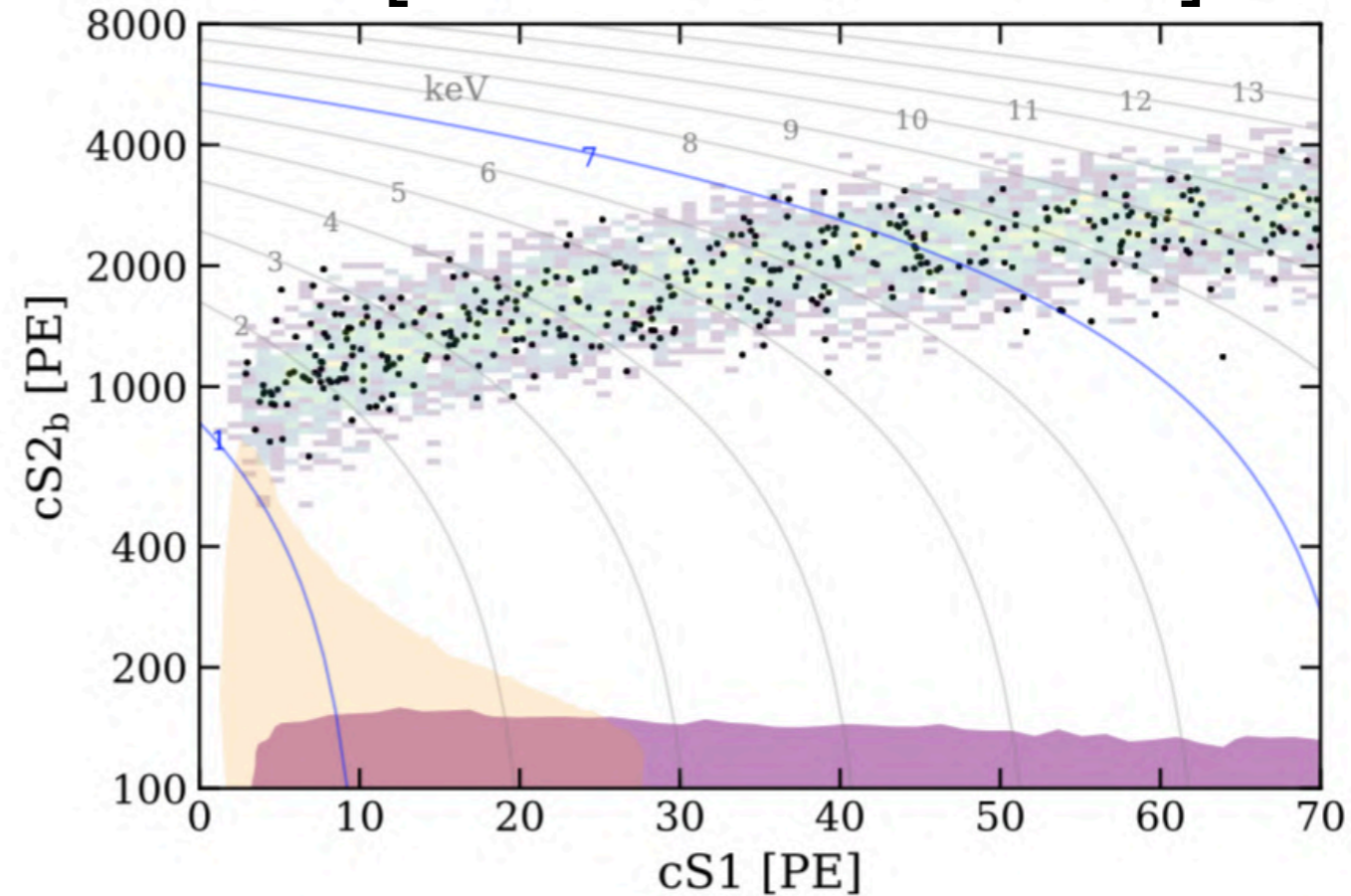
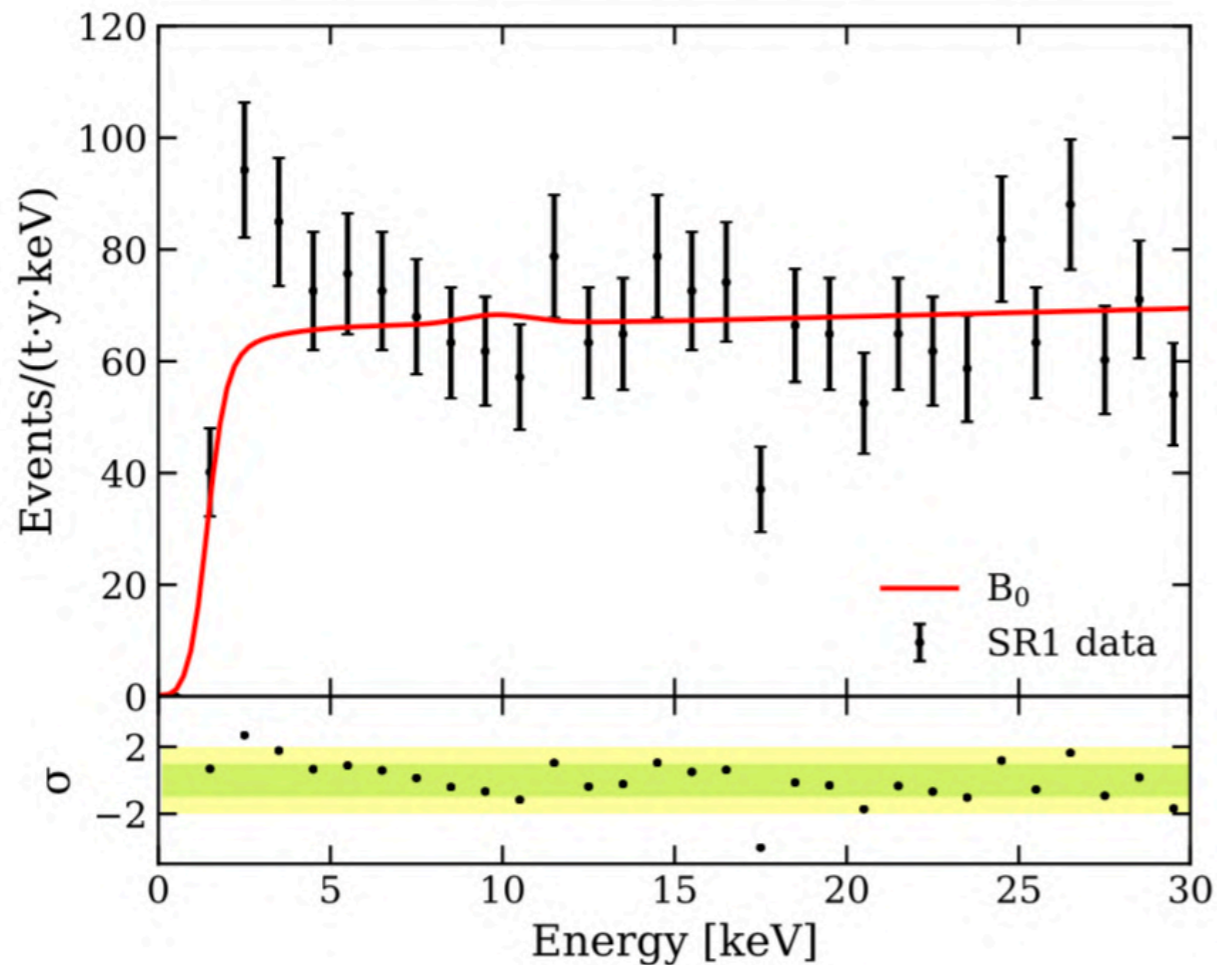


XENONIT electron recoil

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- Excess in electron recoil spectrum.

[XENONIT, 2006.09721]



$E_R = 1-7\text{keV}$: 285 events observed,
 232 ± 15 expected



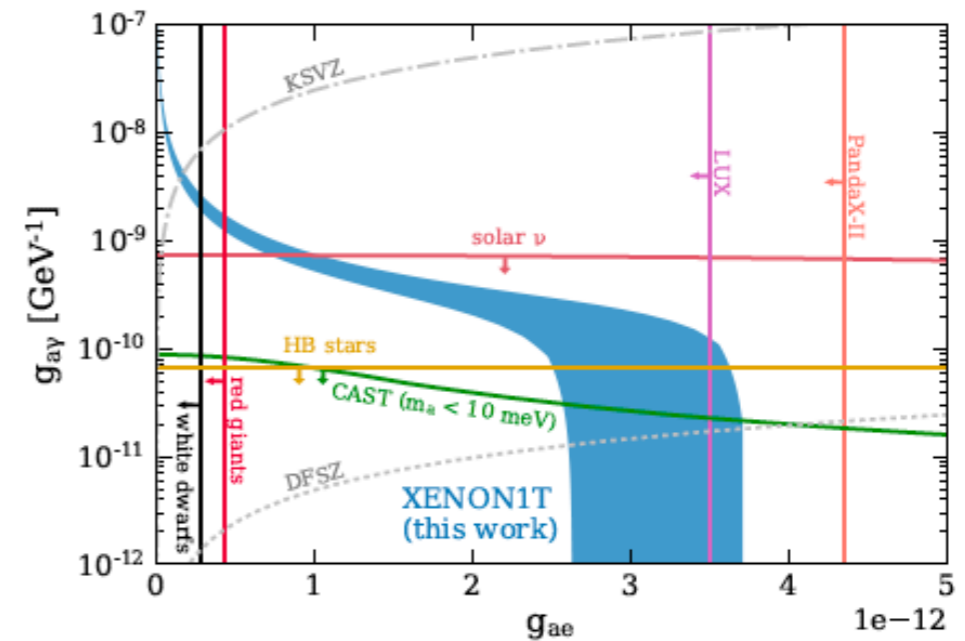
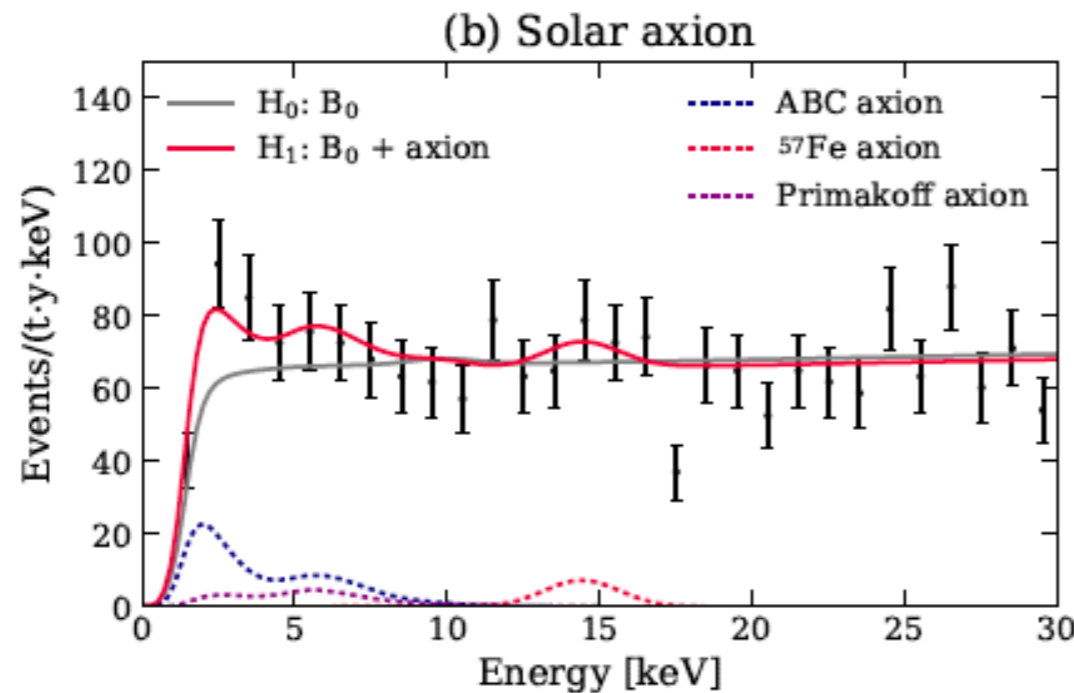
3.3σ deviation:
 most significant at
 $E_R = 2-3\text{keV}$

cf. Other backgrounds: Unknown Tritium, Ar37

New physics for Xelt excess

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- Solar axion** (or neutrino magnetic dipole moment)
 Solar axions produced by ABC, Promakoff, etc, favored at 3.5σ are absorbed by Xenon atoms.

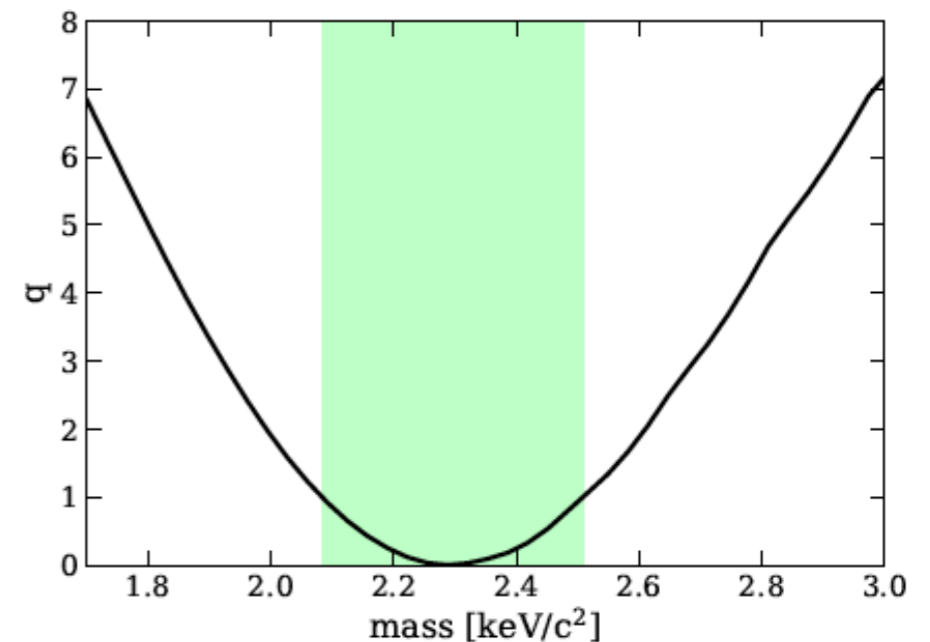


- keV-scale dark matter**

Axio-electric process for “cold axion-like particle”, dark photon, etc.

mono-chromatic recoil;

global(local) at $3.0(4.0)\sigma$



Elastic vs inelastic light DM

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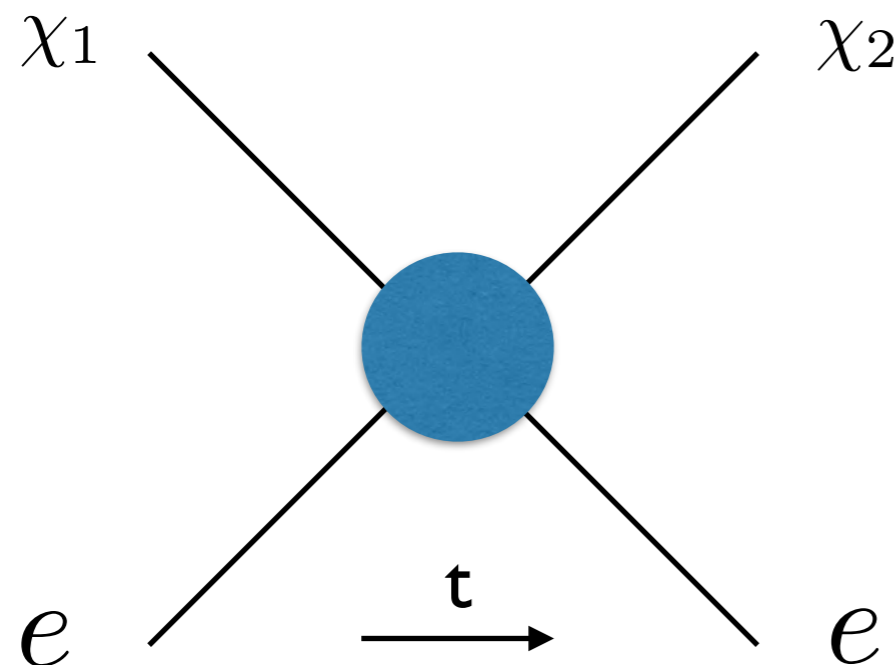
- Elastic scattering between light DM & electron.

$$E_R \sim \frac{\mu^2 v^2}{m_e} \sim m_e v^2 \sim 0.3 \text{ eV} - 20 \text{ eV} \quad : \quad \text{small recoil energy.}$$

$$m_\chi \gtrsim m_e, \quad v \sim 220 \text{ km/s} - 10^{-2} c$$

- Inelastic scattering between dark matter & electron.

[K. Harigaya et al; HML;
J. Bramante et al; Essig et al]



Down scattering with electron
for small mass splitting:

$$\Delta m = m_{\chi_1} - m_{\chi_2} \gg m_e v^2$$

➔ $E_R \sim \Delta m \sim 2.5 \text{ keV}$

“Exothermic (Exo) dark matter”

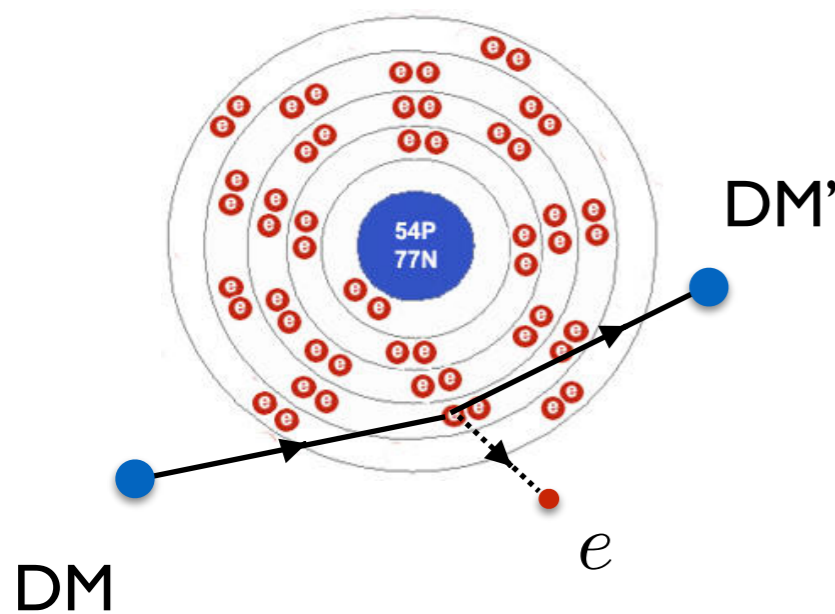
cf. P. Graham et al; R. Essig et al (2010)

Xenon excess is consistent
with standard DM halo model.

Inside Xenon atoms

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- Electrons are not isolated, bound to Xenon atoms.



$$\left\{ \begin{array}{l} \text{Electron velocity} \quad v_e \sim Z_{\text{eff}}\alpha \sim 10^{-2} \\ \text{Nuclear recoil} \quad \Delta E_N \sim \frac{1}{2}\mu_N v_{\text{DM}}^2 \\ \text{Ionization energy} \quad E_{\text{bound}} \lesssim 1 \text{ keV} \end{array} \right.$$

$$E_R = \Delta E_e - E_{\text{bound}} \quad [\text{Essig et al, 2015; HML, 2020}]$$

Xenon Binding Energies [eV]

$n \setminus l$	s	p	d	
O	5	25.7	12.4	–
N	4	213.8	163.5	75.6
M	3	1093.2	958.4	710.7
L	2	5152.19	4837.7	–
K	1	33317.4	–	–

$$\begin{aligned} \Delta E_e &= -\Delta E_{\text{DM}} - \Delta E_N \\ &= \Delta m \left(1 - \frac{1}{2} \left(\frac{m_{\chi_1}}{m_{\chi_2}} \right) v^2 \right) + \frac{m_{\chi_1}}{m_{\chi_2}} \vec{q} \cdot \vec{v} - \frac{\vec{q}^2}{2\mu_{\chi_2 N}} \end{aligned}$$

- Nuclear recoil energy:

$$q^2 \sim m_e \Delta m \gg q_{\text{typ}}^2 \sim m_e^2 v_e^2 :$$

$$\Delta E_N = \frac{q^2}{2\mu_{\chi_2 N}} \sim \frac{m_e}{m_{\chi_2}} (\Delta m) \ll \Delta m \quad \text{for } m_e \ll m_{\chi_2} < m_N$$

[Bunge et al, 1993; Dror et al, 2020]

Electron recoil energy

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- Assume no nuclear recoil but electron velocity.

Initial energies: $E_e = \frac{1}{2}m_e v_e^2$, $E_0 = \frac{1}{2}m_{\chi_1} v^2$

Energy conservation: $m_{\chi_2} + \frac{p^2}{2M_2} + \frac{p_{\text{cm}}^2}{2\mu_2} = m_{\chi_1} + E_0 + E_e$

→ Electron momentum in CM frame: $p_{\text{cm}} = \sqrt{2\mu_2 \left(\Delta m + E_0 + E_e - \frac{p^2}{2M_2} \right)}$

Total 3-momentum: $p^2 = 2m_{\chi_1} E_0 + 2m_e E_e + 4 \cos \alpha \sqrt{m_e m_{\chi_1} E_0 E_e}$

Electron recoil E:

[HML, 2020]

$$\begin{aligned} \Delta E_e &= \frac{1}{2m_e} \left(\frac{m_e}{M_2} \vec{p} - \vec{p}_{\text{cm}} \right)^2 - E_e \\ &= \frac{m_e}{2M_2^2} p^2 + \frac{\mu_2}{m_e} \left(\Delta m + E_0 + E_e \right) - \frac{\mu_2}{2m_e M_2} p^2 - E_e \\ &\quad - \frac{p}{M_2} \cos \theta \sqrt{2\mu_2 (\Delta m + E_0 + E_e) - \frac{\mu_2}{M_2} p^2}. \end{aligned}$$

Momentum transfer:

$$q^2 = 2m_e \Delta E_e + m_e^2 v_e^2 - 2m_e v_e \cos \psi \sqrt{m_e \Delta E_e}$$

Electron recoil energy

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- Initial electron momentum can be ignored for relatively heavy dark matter.

$$m_{\chi_1} E_0 \gtrsim m_e E_e \longrightarrow m_{\chi_1} \gtrsim m_e (v_e/v) \sim 10 \text{ MeV}$$

➔ Total 3-momentum: $p^2 \simeq 2m_{\chi_1} E_0$ due to DM energy.

$$\Delta m \ll m_e \ll m_{\chi_1}, \quad \kappa \simeq \frac{\Delta m}{\frac{1}{2}m_e v^2} \simeq 2.2 \times 10^4 \left(\frac{220 \text{ km/s}}{v} \right)^2 \left(\frac{\Delta m}{3 \text{ keV}} \right) \gg 1$$

Recoil E: $\Delta E_e \simeq \Delta m \left(1 - \frac{2}{\sqrt{\kappa}} \cos \theta \right),$ [HML, 2020]
“Monochromatic”

Momentum transfer: $q^2 \simeq 2m_e \Delta E_e \simeq 2m_e \Delta m \left(1 - \frac{2}{\sqrt{\kappa}} \cos \theta \right).$


➔ Mass splitting determines both recoil E & momentum transfer dominantly.

Moving electrons

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- Width of recoil energy depends on electron velocity for light dark matter.

$$m_{\chi_1} E_0 \lesssim m_e E_e \quad \longrightarrow \quad m_{\chi_1} \lesssim m_e (v_e/v) \sim 10 \text{ MeV}$$

 Total 3-momentum: $p^2 \simeq 2m_e E_e$ due to electron energy.

$$\Delta m \ll m_e \ll m_{\chi_1}, \quad \boxed{\tilde{\kappa} \simeq \frac{\Delta m}{\frac{1}{2}m_e v_e^2}} \simeq 10^2 \left(\frac{10^{-2}c}{v_e} \right)^2 \left(\frac{\Delta m}{3 \text{ keV}} \right) \gg 1$$

Recoil E: $\Delta E_e \simeq \Delta m \left(1 - \frac{2m_e}{m_{\chi_1}} \frac{1}{\sqrt{\tilde{\kappa}}} \cos \theta \right)$ [HML, 2020]
 “Monochromatic”

Momentum transfer:

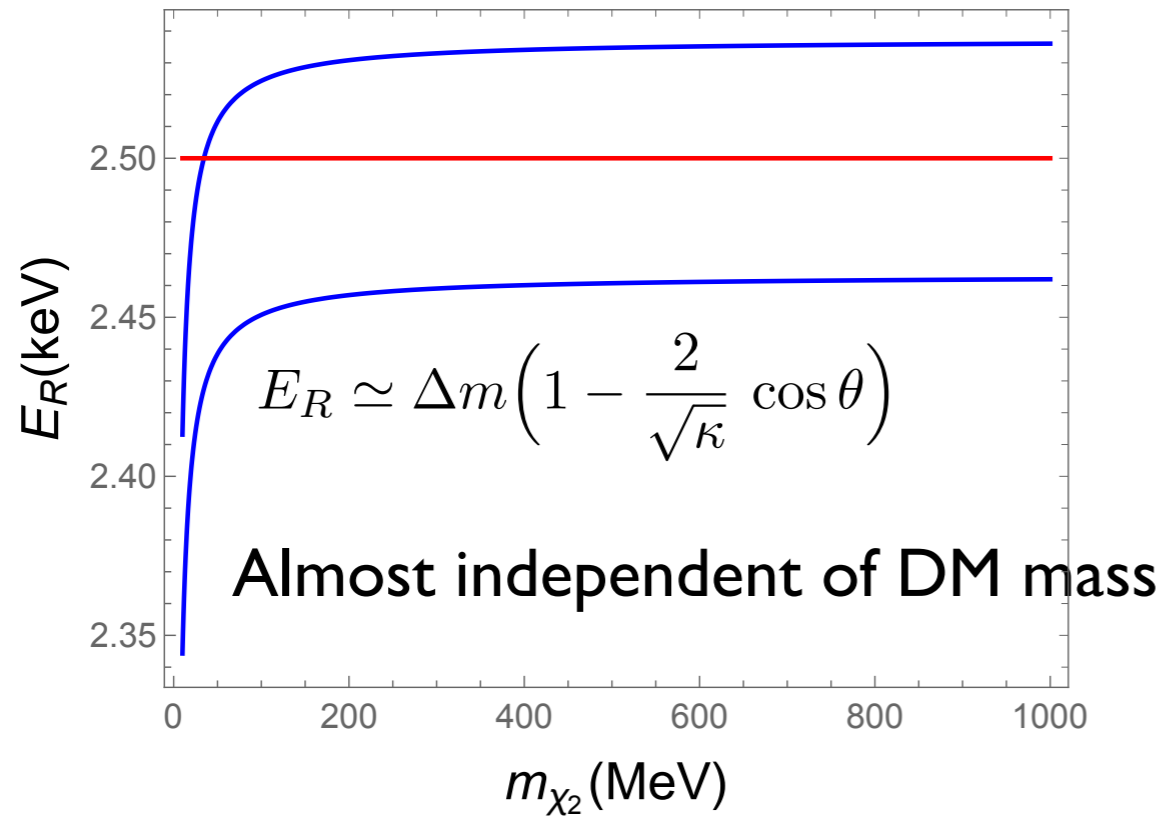
$$q^2 \simeq 2m_e \Delta E_e \simeq 2m_e \Delta m \left(1 - \frac{2m_e}{m_{\chi_1}} \frac{1}{\sqrt{\tilde{\kappa}}} \cos \theta \right)$$



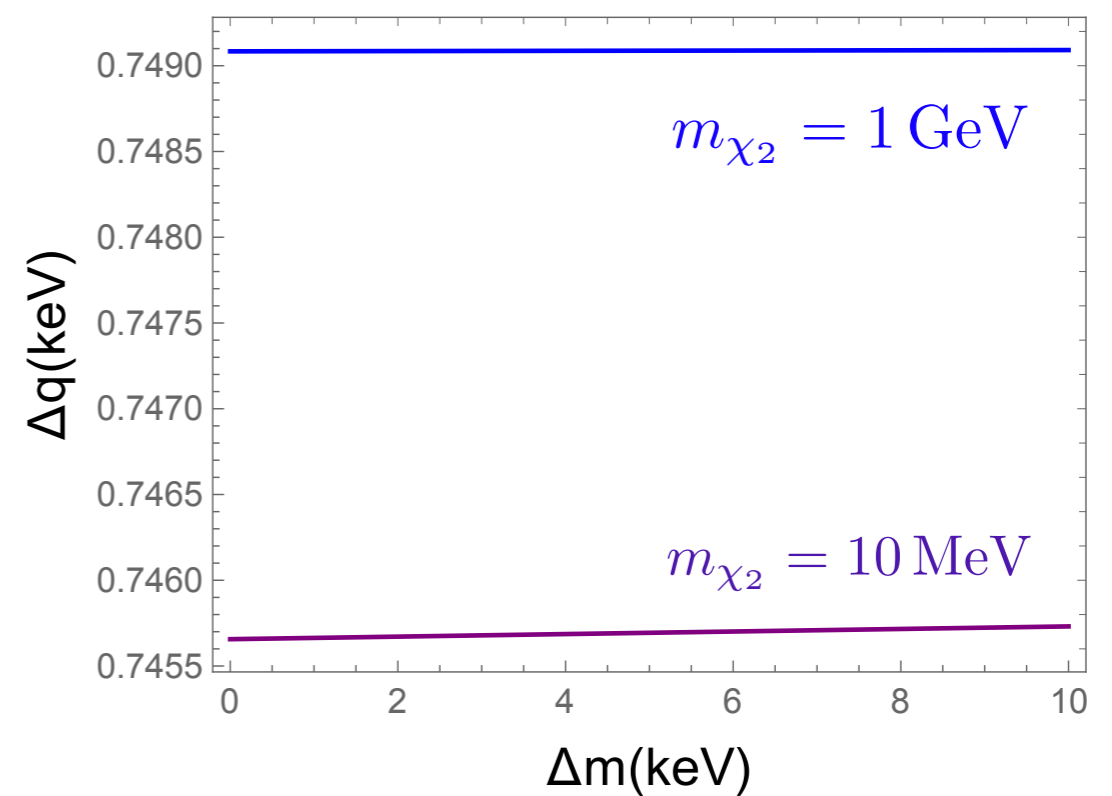
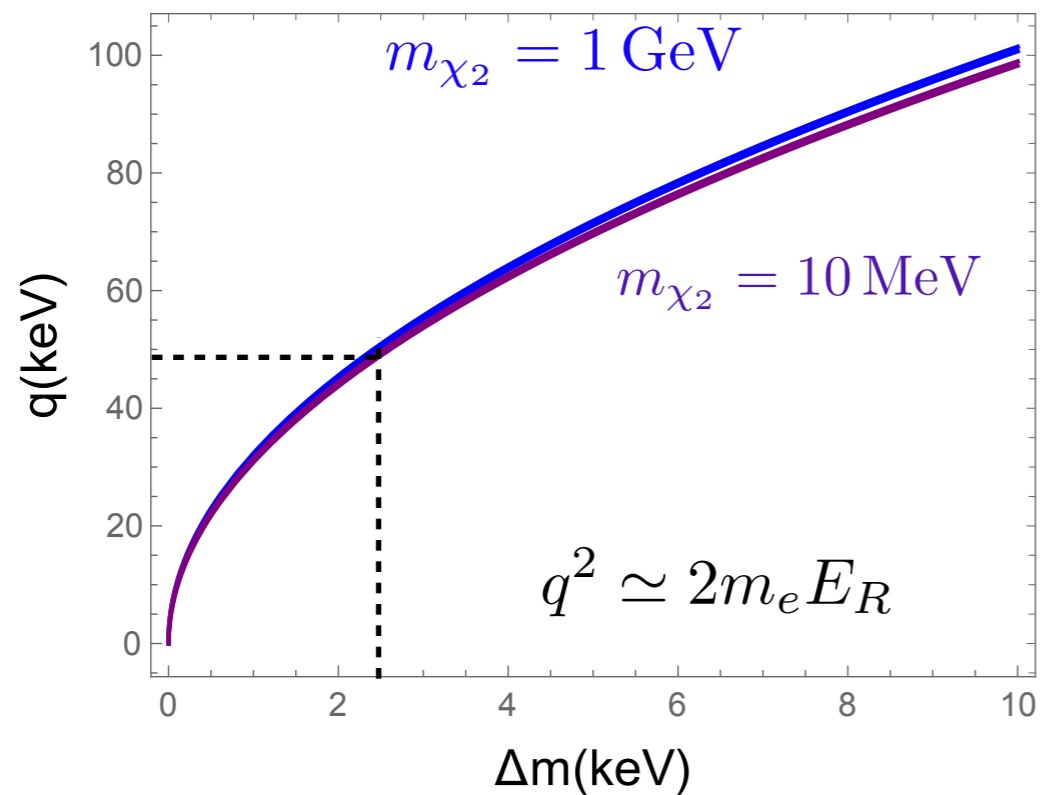
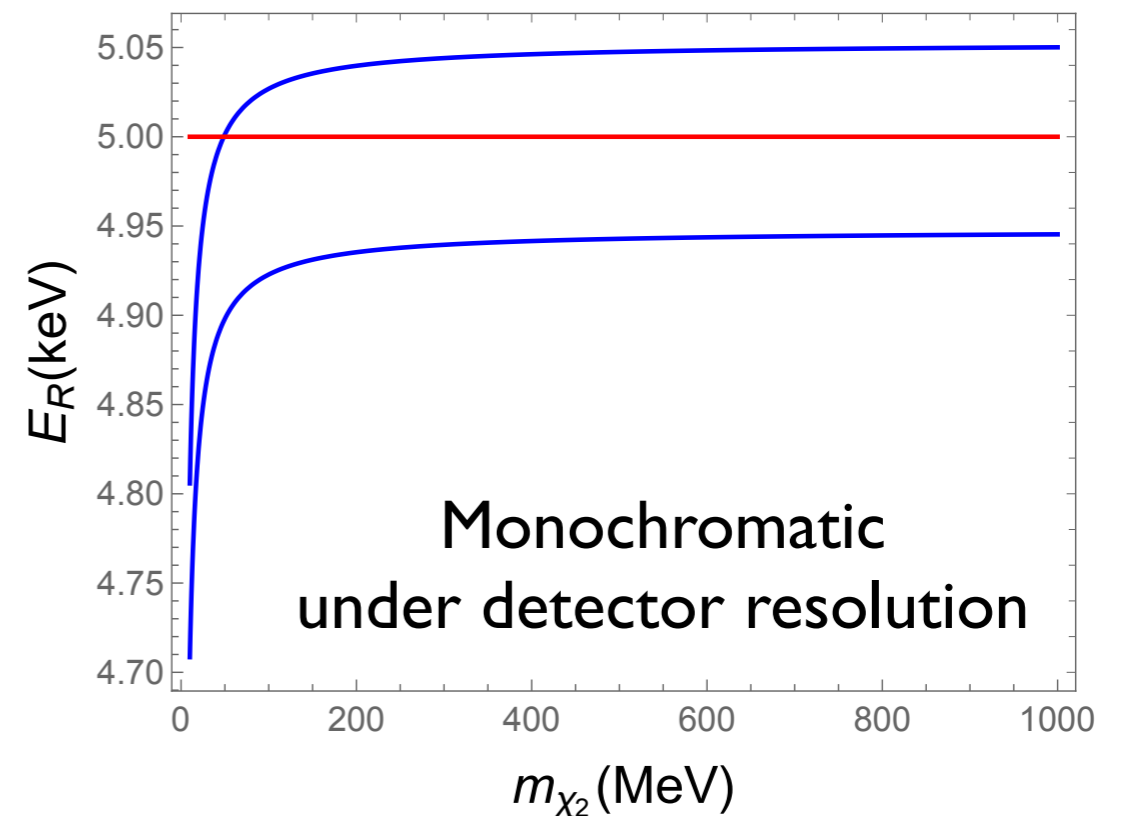
Mass splitting still determines kinematics dominantly

Energy/momentum transfer -13-

$\Delta m = 2.5 \text{ keV}$



$\Delta m = 5 \text{ keV}$



ExoDM event rate

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- The general event rate per target mass is

$$dR = \frac{\rho_{\chi_1} v}{m_{\chi_1} m_T} d\sigma f_1(v) dv, \quad f_1(v) = \frac{4v^2}{v_0^3 \sqrt{\pi}} e^{-v^2/v_0^2} \text{ with } v_0 = 220 \text{ km/s}$$

- The total cross section for inelastic scattering:

$$\frac{d\sigma}{dE_R} = \frac{2m_e \bar{\sigma}_e}{q_+^2 - q_-^2} \int_{q_-}^{q_+} a_0^2 q' dq' K(E_R, q') P^2(v). \quad [\text{HML, 2020}]$$

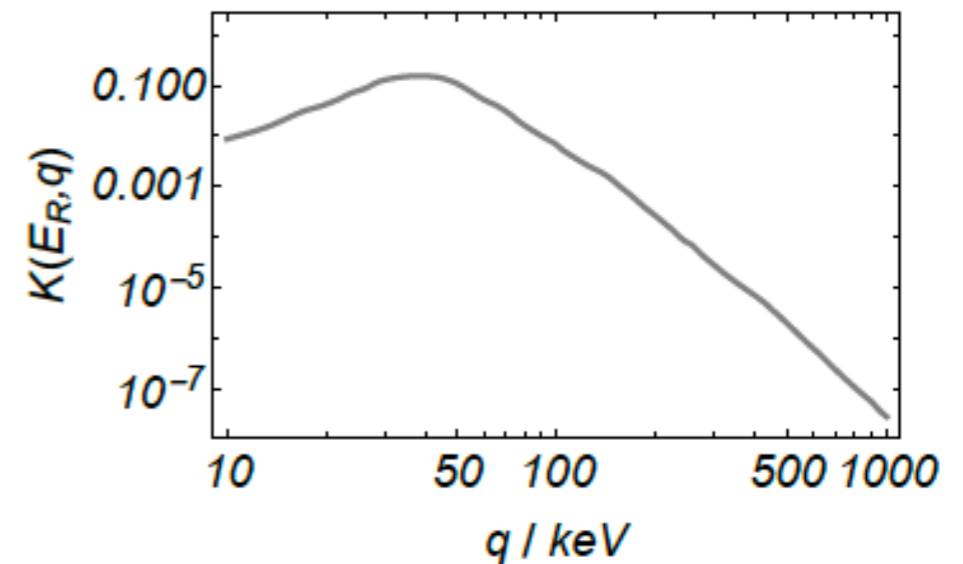
Atomic enhancement factor:

$$K_{\text{int}}(E_R) = \int_{q_-}^{q_+} a_0^2 q' dq' K(E_R, q')$$

Phase space factor:

$$P^2(v) = \frac{\left(1 - \frac{(m_{\chi_2} + m_e)^2}{E_{\text{cm}}^2}\right)^{1/2} \left(1 - \frac{(m_{\chi_2} - m_e)^2}{E_{\text{cm}}^2}\right)^{1/2}}{\left(1 - \frac{(m_{\chi_1} + m_e)^2}{E_{\text{cm}}^2}\right)^{1/2} \left(1 - \frac{(m_{\chi_1} - m_e)^2}{E_{\text{cm}}^2}\right)^{1/2}} \approx \sqrt{1 + \frac{2\Delta m}{\mu_1 v^2}}$$

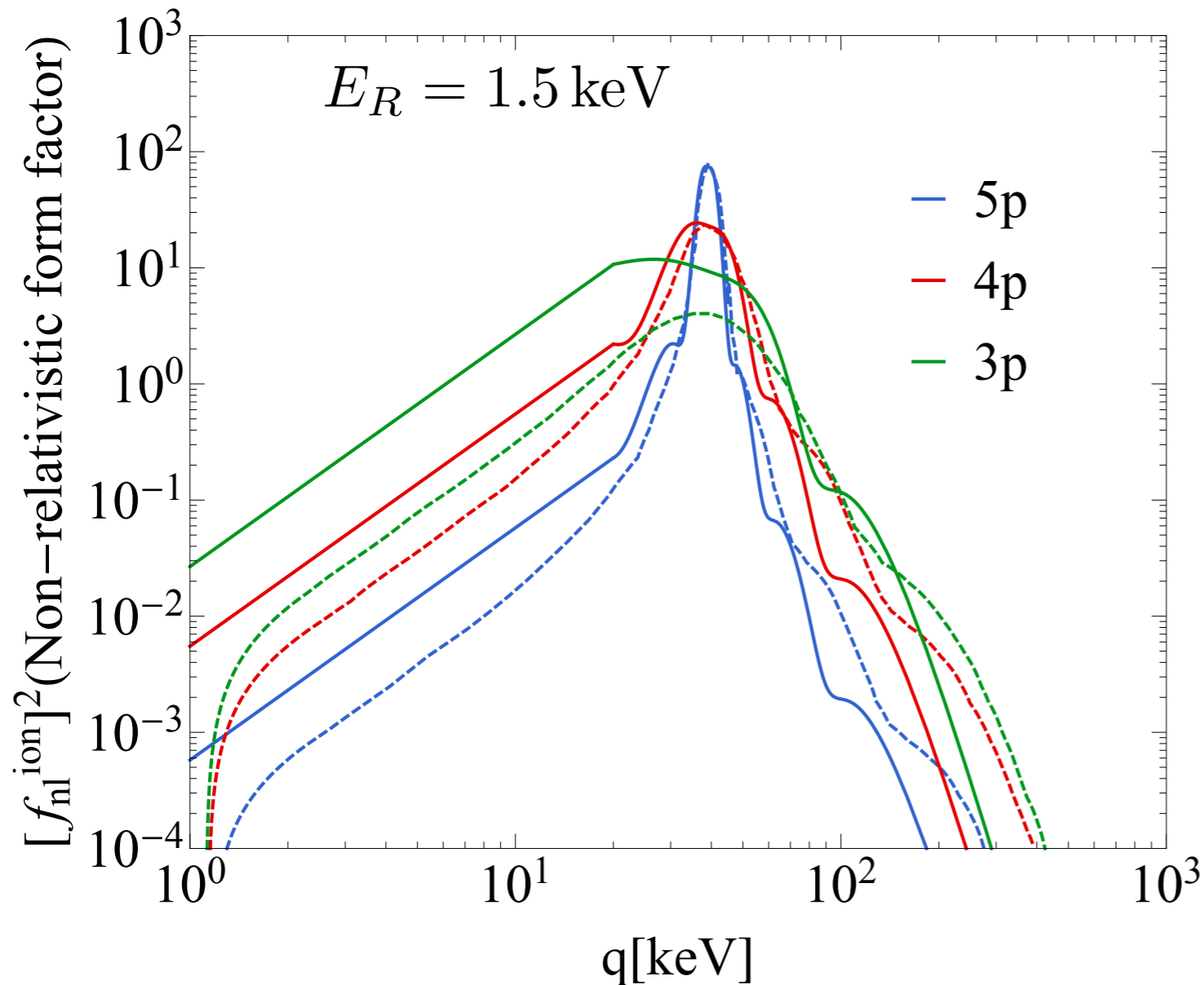
$$E_{\text{cm}} = (m_{\chi_1} + m_e)^2 + m_e m_{\chi_1} v^2$$



[K. Kannike et al;
K. Harigaya et al]

Atomic form factors

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Solid: S. Choi, HML, Zhu, to appear.

cf. Dashed: Bloch et al, 2006. 14521

Both results are consistent,
in particular, near the peak.

Outer-shell electrons are
more easily ionized.

$$K(E_R, q) = \frac{\alpha^2 m_e (m_e + m_{\chi_1})^2}{4E_R m_{\chi_1}^2} \sum_{n,l} |f_{nl}(p_e, q)|^2, \quad p_e = \sqrt{2m_e E_R}$$

ExoDM event rate

-16-

- Differential event rate per target mass:

$$q_{\pm}^2 \simeq 2m_e \Delta m \left(1 \pm \frac{2}{\sqrt{\kappa}}\right), \quad E_- < E_R < E_+ \text{ with } E_{\pm} = \Delta m \left(1 \pm \frac{2}{\sqrt{\kappa}}\right)$$

Peaked at $q \simeq \sqrt{2m_e \Delta m} \simeq 50 \text{ keV}$, $E_R \simeq \Delta m = 2.5 \text{ keV}$.

➔
$$\frac{dR}{dE_R} = \frac{2m_e \bar{\sigma}_e \rho_{\chi_1}}{m_{\chi_1} m_T} K_{\text{int}}(E_R) \int_{v_{\text{min}}}^{\infty} \frac{v P^2(v)}{q_+^2 - q_-^2} f_1(v) dv \theta(E_R - E_-) \theta(E_+ - E_R),$$

with
$$K_{\text{int}}(E_R) = \int_{q_-}^{q_+} a_0^2 q' dq' K(E_R, q')$$

- Total event rate per detector: [HML, 2020]

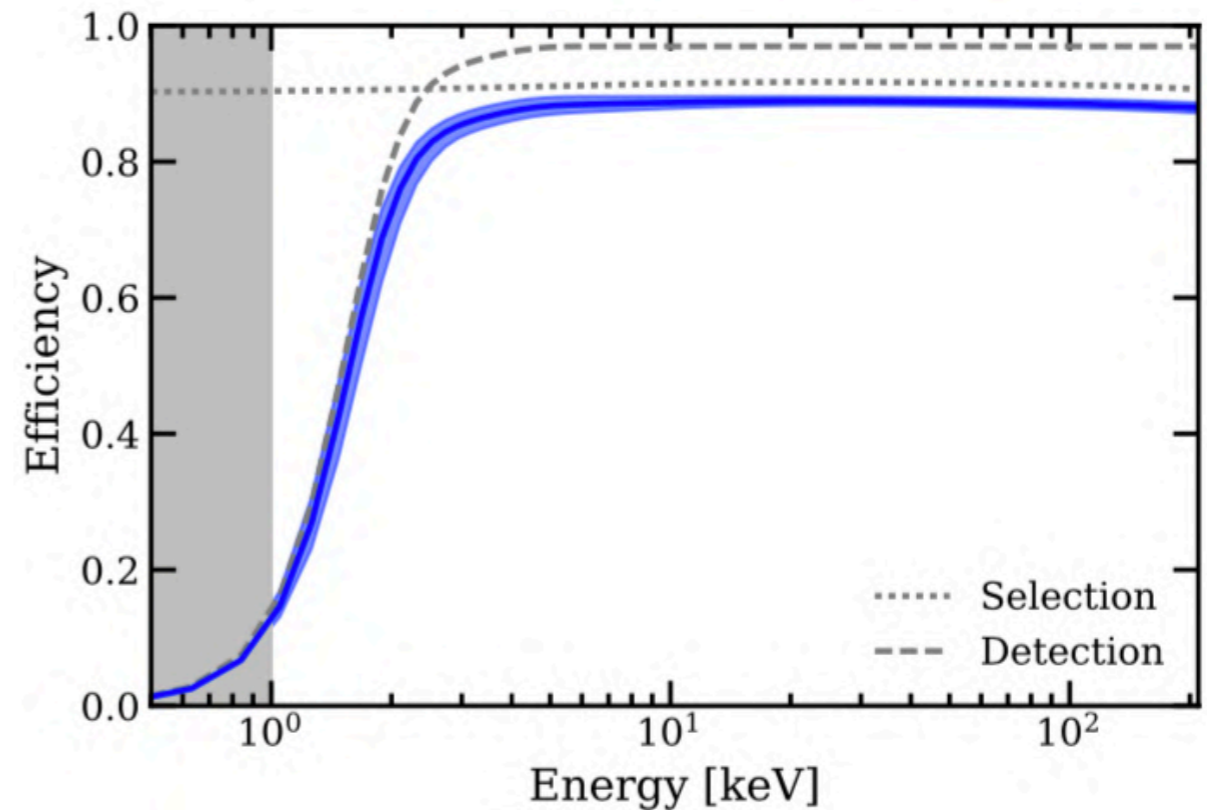
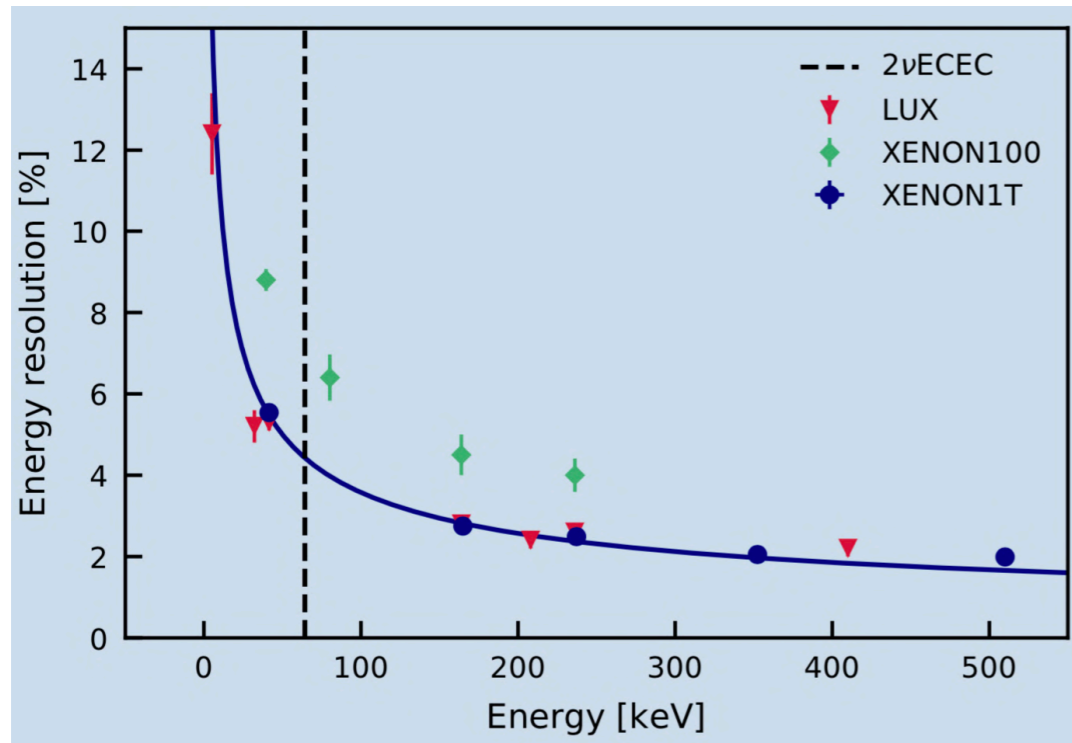
$$R_D = M_T \int_{E_T}^{\infty} \frac{dR}{dE_R} dE_R \simeq 50 \left(\frac{M_T}{\text{tonne} - \text{yrs}} \right) \left(\frac{K_{\text{int}}(\Delta m)}{2.6} \right) \left(\frac{\rho_{\chi_1}}{0.4 \text{ GeV cm}^{-3}} \right) \times \left(\frac{\bar{\sigma}_e / m_{\chi_1}}{1.2 \times 10^{-43} \text{ cm}^2 / \text{GeV}} \right) \left(\frac{\Delta m}{2.5 \text{ keV}} \right)^{1/2}$$

ExoDM event rate

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- The event is convoluted with detector resolution and efficiency.

$$\frac{dR_D}{dE_R} = \frac{R_D}{\sqrt{2\pi}\sigma} e^{-(E_R - \Delta m)^2 / (2\sigma^2)} \alpha(E)$$



$\sigma : 20\% - 6\%, E_R = 2 - 30 \text{ keV},$

$\alpha(E) = 0.7 - 0.9, E_R = 2 - 10 \text{ keV}$

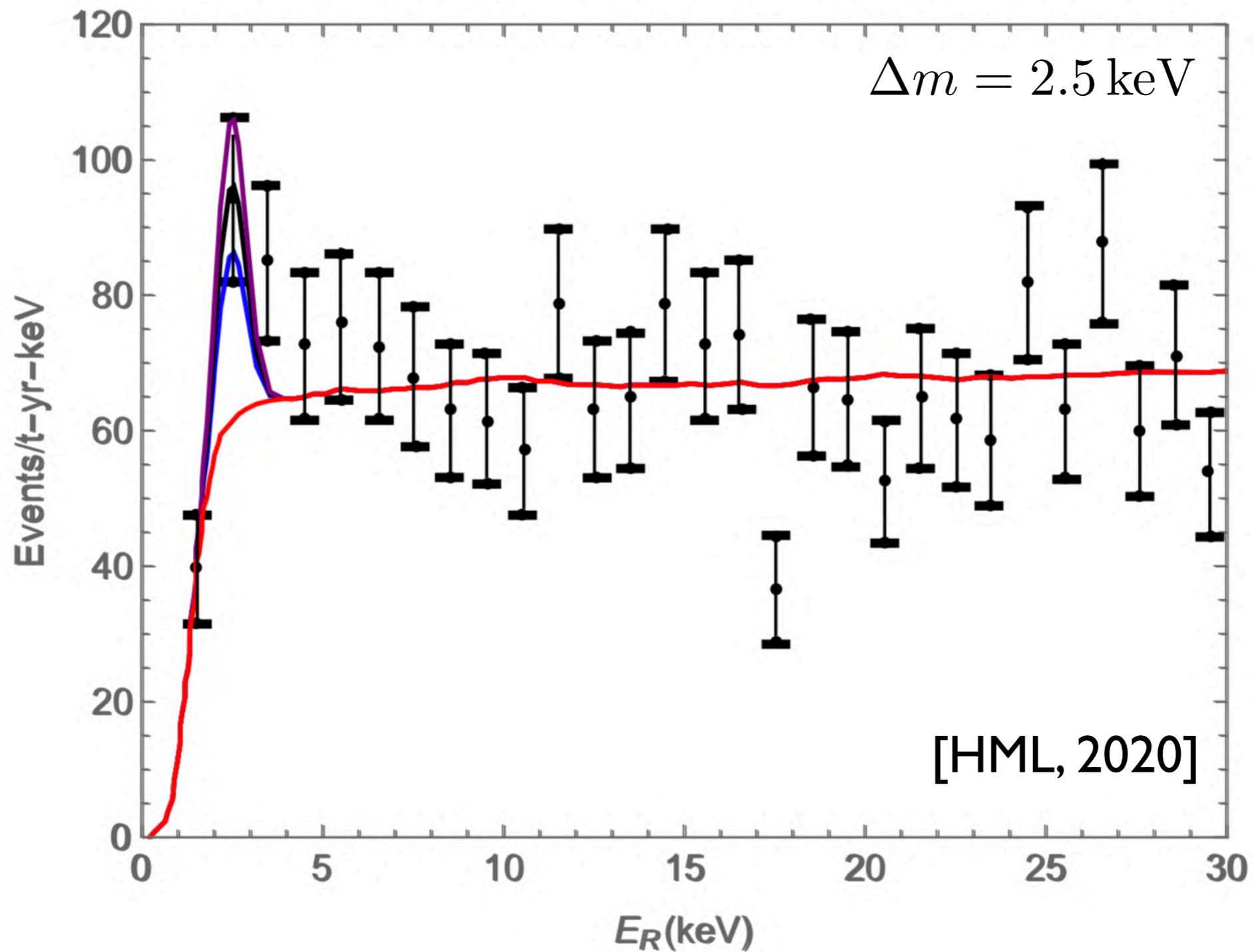
$E_R = 2.5 \text{ keV}$



$\sigma = 0.4 \text{ keV}, \alpha \gtrsim 0.8$

XENONIT electron recoil

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Bottom to top: $(\bar{\sigma}_e/m_{\chi_1})/(10^{-43} \text{ cm}^2/\text{GeV}) \simeq 1.0, 1.4, 1.8$

Red line: Background model

EFT for ExoDM

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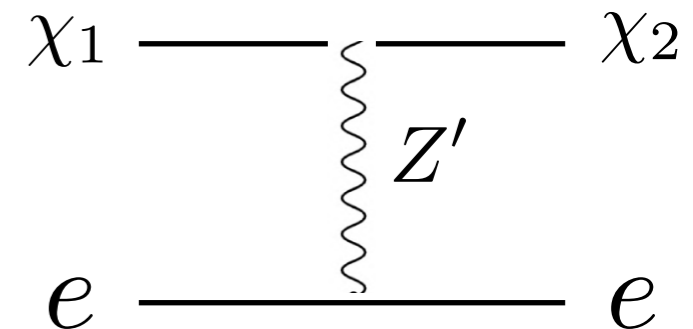
- Effective interactions between EDM and electron with massive Z' mediator: [HML, 2020]

$$\mathcal{L}_{\text{eff}} = \left(g_{Z'} Z'_\mu \bar{\chi}_2 \gamma^\mu (v_\chi + a_\chi \gamma^5) \chi_1 + \text{h.c.} \right) + g_{Z'} Z'_\mu \bar{e} (v_e + a_e \gamma^5) e + g_{Z'} Z'_\mu \bar{\nu} \gamma^\mu (v_\nu + a_\nu \gamma^5) \nu$$

- DM-electron inelastic cross section:

$$\bar{\sigma}_e \simeq \frac{v_\chi^2 v_e^2 g_{Z'}^4 \mu_1^2}{\pi m_{Z'}^4}$$

$$\simeq \left(\frac{v_\chi g_{Z'}}{0.6} \right)^2 \left(\frac{v_e g_{Z'}}{10^{-4} e} \right)^2 \left(\frac{600 \text{ MeV}}{m_{Z'}} \right)^4 \left(\frac{\mu_1}{m_e} \right)^2 \times 10^{-43} \text{ cm}^2$$



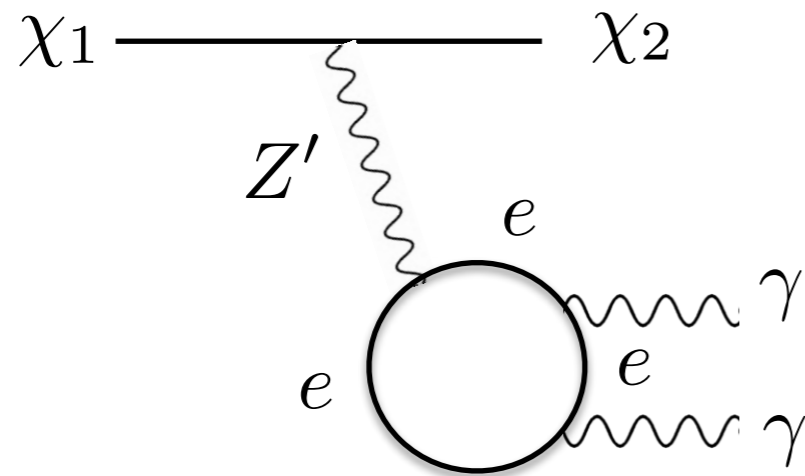
Light dark matter and mediator below GeV scale are favored for XENONIT excess.

- Astrophysics bounds on lifetime of heavier state.
- DM relic abundances & terrestrial bounds.

Bounds on ExoDM

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- The axial vector coupling for electron can lead the heavier state to decay into two photons:

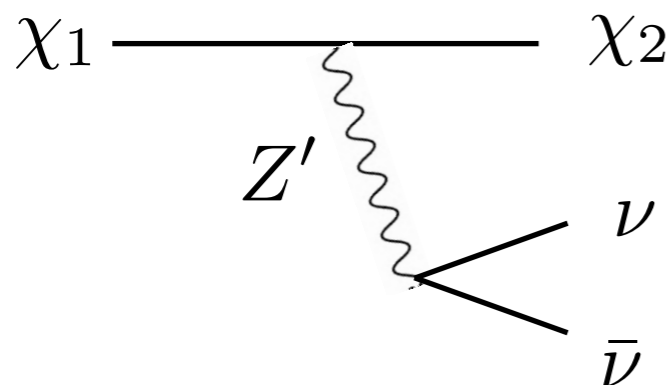


$$\Gamma(\chi_1 \rightarrow \chi_2 \gamma \gamma) \simeq \frac{a_e^2 (v_\chi^2 + a_\chi^2) e^4 g_{Z'}^2 (\Delta m)^5}{2560 \pi^7 m_{Z'}^4}$$

Diffuse X-ray: $\tau_{\chi_1} \gtrsim 10^{24}$ sec

$$|a_e| g_{Z'} \sqrt{v_\chi^2 + a_\chi^2} < 2.5 \times 10^{-6} \left(\frac{2.5 \text{ keV}}{\Delta m} \right)^{5/2} \left(\frac{m_{Z'}}{1 \text{ GeV}} \right)^2$$

- Accompanying neutrino coupling opens up neutrino decay channels: $E_\nu \sim \text{keV}$



$$\Gamma(\chi_1 \rightarrow \chi_2 \nu \bar{\nu}) \simeq \frac{N_\nu G_F'^2 (\Delta m)^5}{30 \pi^3} (v_\chi^2 + 3a_\chi^2) (v_\nu^2 + a_\nu^2)$$

$\tau_{\chi_1} > t_U :$

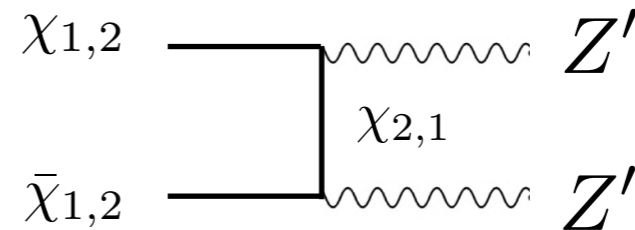
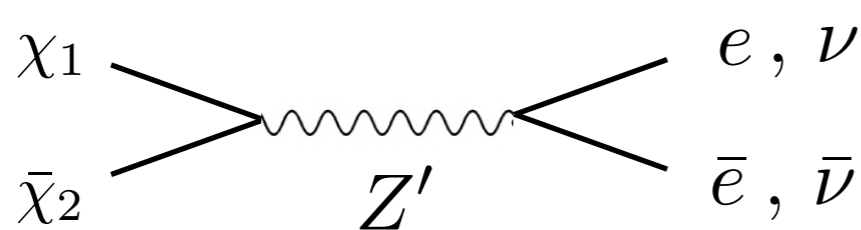
$$G_F' \sqrt{N_\nu (v_\nu^2 + a_\nu^2)} < 2.4 \times 10^{-6} \text{ GeV}^{-2}$$

cf. Super-K: $\tau_{\chi_1} \gtrsim 10^{24}$ sec, $E_\nu \gtrsim 0.1$ GeV

Dark matter relic density

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- ExoDM can annihilate into a pair of electrons or neutrinos, and a pair of Z' gauge bosons.

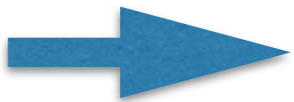


$$\langle\sigma v\rangle = \frac{1}{2}\langle\sigma v\rangle_{\chi_1\bar{\chi}_2\rightarrow e\bar{e},\nu\bar{\nu}} + \frac{1}{2}\langle\sigma v\rangle_{\chi_1\bar{\chi}_2\rightarrow Z'Z'}$$

$$\langle\sigma v\rangle_{\chi_1\bar{\chi}_2\rightarrow e\bar{e},\nu\bar{\nu}} = \frac{g_{Z'}^4 v_\chi^2}{\pi} \left[v_e^2 + a_e^2 + N_\nu (v_\nu^2 + a_\nu^2) \right] \frac{m_{\chi_1}^2}{(m_{Z'}^2 - 4m_{\chi_1}^2)^2 + \Gamma_{Z'}^2 m_{Z'}^2},$$

$$\langle\sigma v\rangle_{\chi_1\bar{\chi}_1,\chi_2\bar{\chi}_2\rightarrow Z'Z'} = \begin{cases} \frac{g_{Z'}^4}{4\pi} \left[v_\chi^4 + a_\chi^4 + 2v_\chi^2 a_\chi^2 \left(4\frac{m_{\chi_1}^2}{m_{Z'}^2} - 3 \right) \right] \frac{m_{\chi_1}^2}{(m_{Z'}^2 - 2m_{\chi_1}^2)^2} \left(1 - \frac{m_{Z'}^2}{m_{\chi_1}^2} \right)^{3/2}, & m_{\chi_1} > m_{Z'}, \\ \frac{(n_{Z'}^{\text{eq}})^2}{n_{\chi_1}^{\text{eq}} n_{\chi_2}^{\text{eq}}} \langle\sigma v\rangle_{Z'Z'\rightarrow\chi_1\bar{\chi}_1,\chi_2\bar{\chi}_2}, & m_{\chi_1} < m_{Z'}. \end{cases}$$

“forbidden channels”

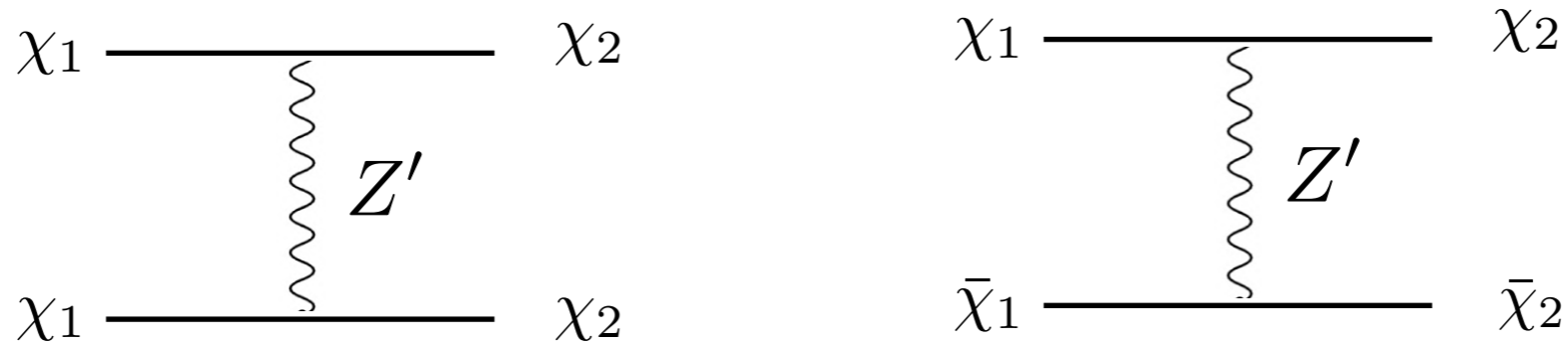


$$\Omega_{\text{DM}} h^2 = 0.12 \left(\frac{10.75}{g_*(T_f)} \right)^{1/2} \left(\frac{x_f}{20} \right) \left(\frac{4.3 \times 10^{-9} \text{ GeV}^{-2}}{x_f \int_{x_f}^{\infty} x^{-2} \langle\sigma v\rangle} \right) \simeq 2 \Omega_{\chi_1} h^2$$

Late chemical decoupling

-22-

- Heavier DM keeps annihilating into lighter DM.



$$\langle\sigma v\rangle_{\chi_1\chi_1\rightarrow\chi_2\chi_2} = \frac{\sqrt{2}}{16\pi} \frac{g_{Z'}^4 m_{\chi_1}^2}{m_{Z'}^4} \sqrt{\frac{\Delta m}{m_{\chi_1}}} (v_\chi^4 + 6a_\chi^2 v_\chi^2 + 9a_\chi^4), \quad \langle\sigma v\rangle_{\chi_1\bar{\chi}_1\rightarrow\chi_2\bar{\chi}_2} = \frac{\sqrt{2}}{8\pi} \frac{g_{Z'}^4 m_{\chi_1}^2}{m_{Z'}^4} \sqrt{\frac{\Delta m}{m_{\chi_1}}} (v_\chi^4 + 3a_\chi^4)$$

Heavier component must be decoupled at $T_\chi \gtrsim \Delta m$.

$$n_{\chi_1} \langle\sigma v\rangle_{\chi_1\bar{\chi}_1\rightarrow\chi_2\bar{\chi}_2} = H, \quad \text{at } T_\chi > \Delta m$$

Otherwise, Boltzmann suppressed: $n_{\chi_1} = e^{-\Delta m/T_\chi} n_{\chi_2}$

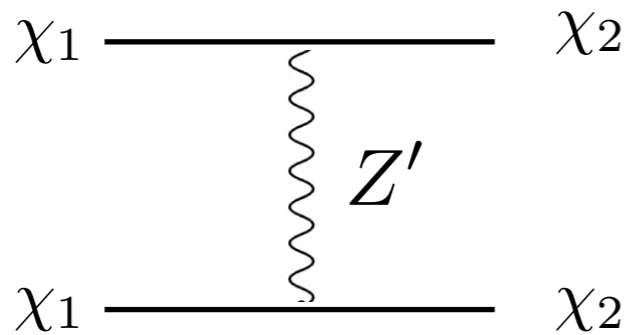
Here, $T_\chi = \frac{T^2}{T_{\text{kd}}}$, $T_{\text{kd}} \sim \text{MeV}$. “Kinetic decoupling temp”

➔ $\frac{|v_\chi| g_{Z'} m_{\chi_1}}{m_{Z'}} \lesssim 0.035 \left(\frac{\Omega_{\text{DM}}/2}{\Omega_{\chi_1}}\right)^{1/4} \left(\frac{m_{\chi_1}}{100 \text{ MeV}}\right)^{1/2} \left(\frac{m_{\chi_1}/\Delta m}{4 \times 10^4}\right)^{3/8} \left(\frac{\Delta m/(2.5 \text{ keV})}{T_{\text{kd}}/(10 \text{ MeV})}\right)^{1/8}$

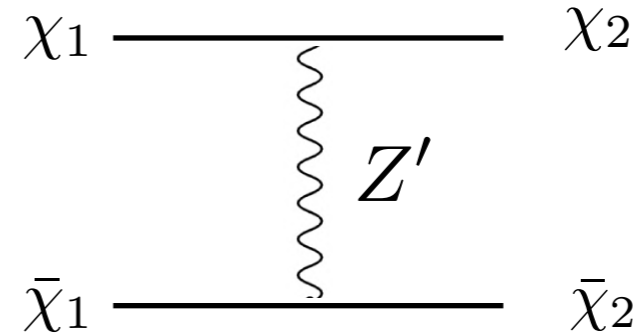
Dark matter self-scattering

-23-

- Inelastic self-scattering.

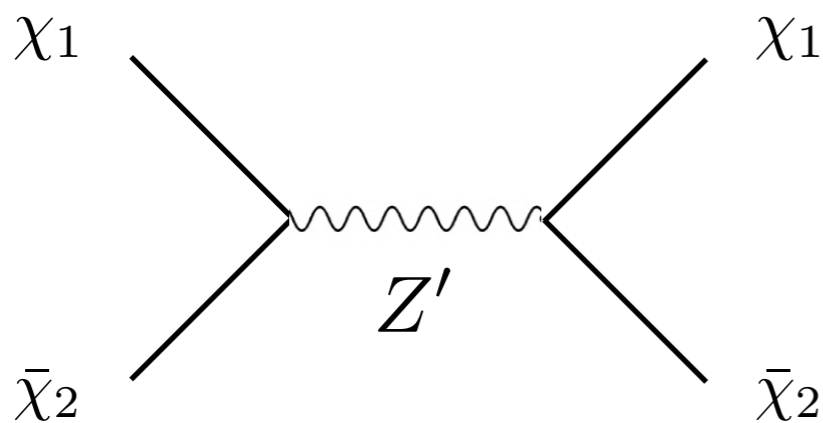


$$\sigma_{\chi_1\chi_1 \rightarrow \chi_2\chi_2} = \frac{1}{16\pi} \frac{g_{Z'}^4 m_{\chi_1}^2}{m_{Z'}^4} (v_\chi^4 + 6a_\chi^2 v_\chi^2 + 9a_\chi^4),$$



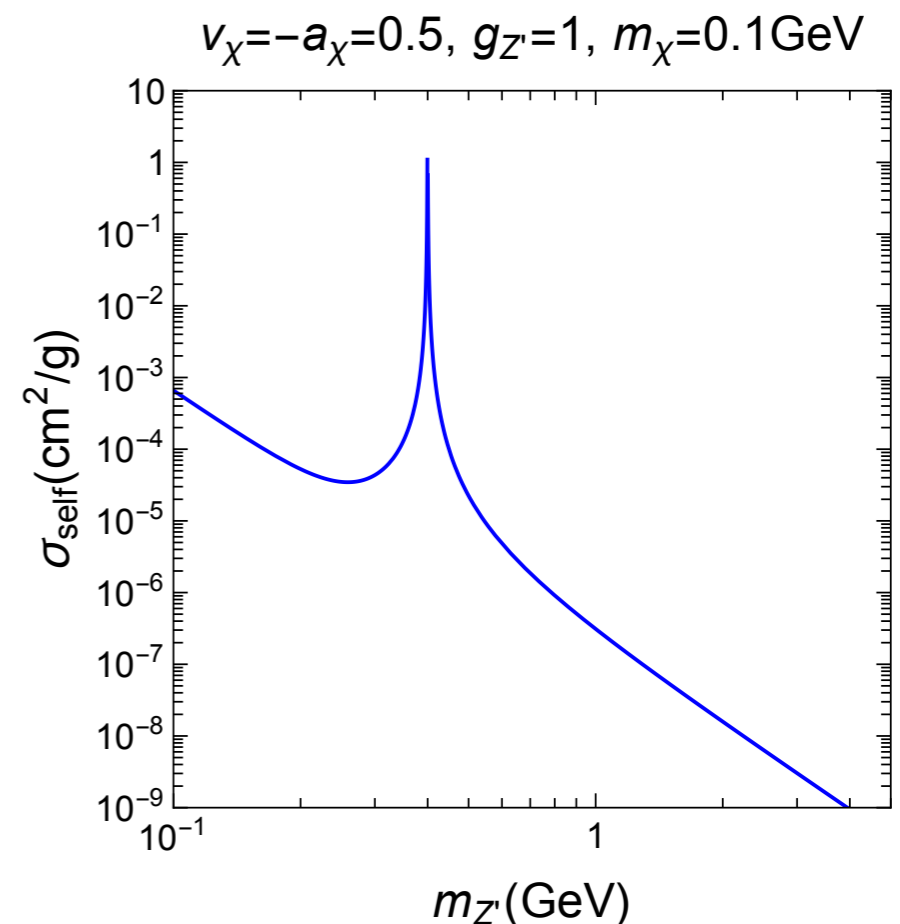
$$\sigma_{\chi_1\bar{\chi}_1 \rightarrow \chi_2\bar{\chi}_2} = \frac{1}{8\pi} \frac{g_{Z'}^4 m_{\chi_1}^2}{m_{Z'}^4} (v_\chi^4 + 3a_\chi^4)$$

- Elastic self-scattering.



$$\sigma_{\chi_1\bar{\chi}_2 \rightarrow \chi_1\bar{\chi}_2} = \frac{g_{Z'}^4 v_\chi^2 (v_\chi^2 + a_\chi^2)}{\pi} \frac{m_{\chi_1}^2}{(m_{Z'}^2 - 4m_{\chi_1}^2 (1 + v^2/4))^2 + \Gamma_{Z'}^2 m_{Z'}^2}$$

Velocity-dependent self-scattering!



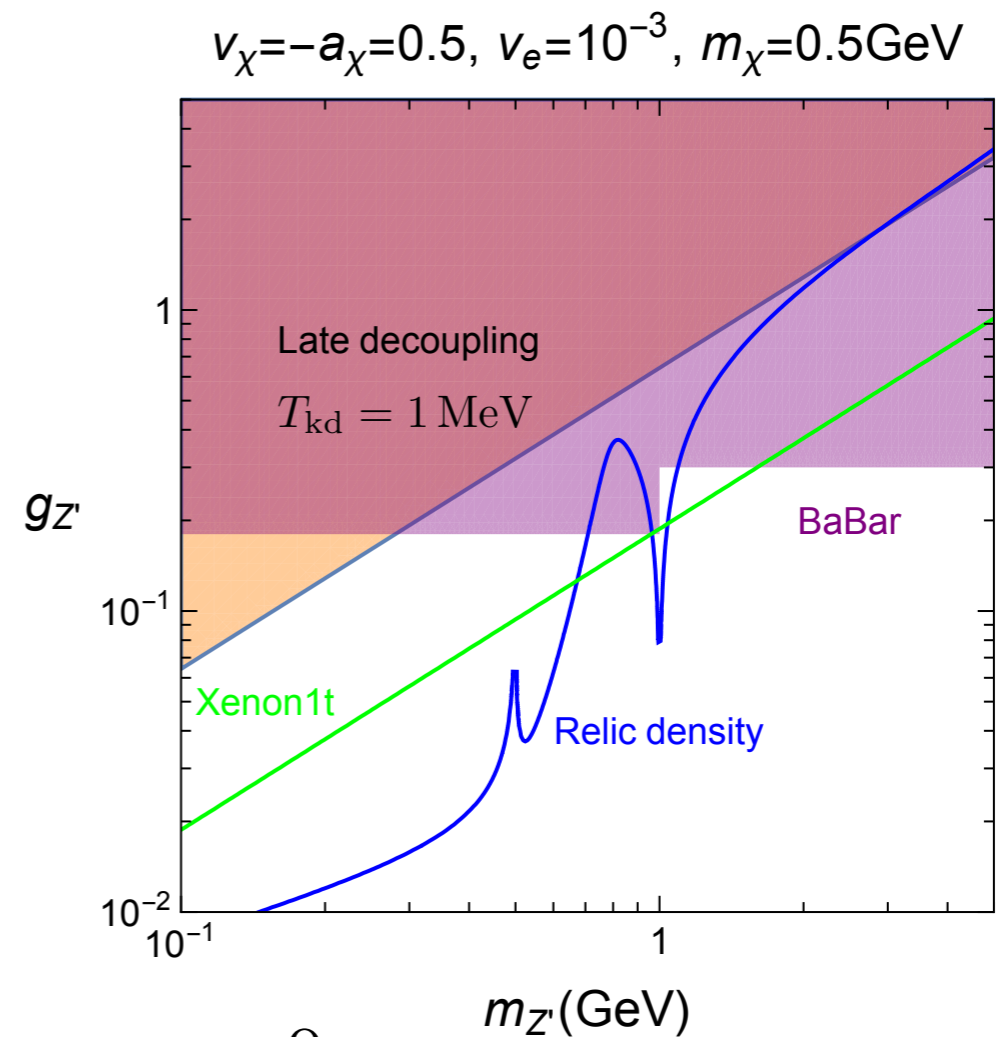
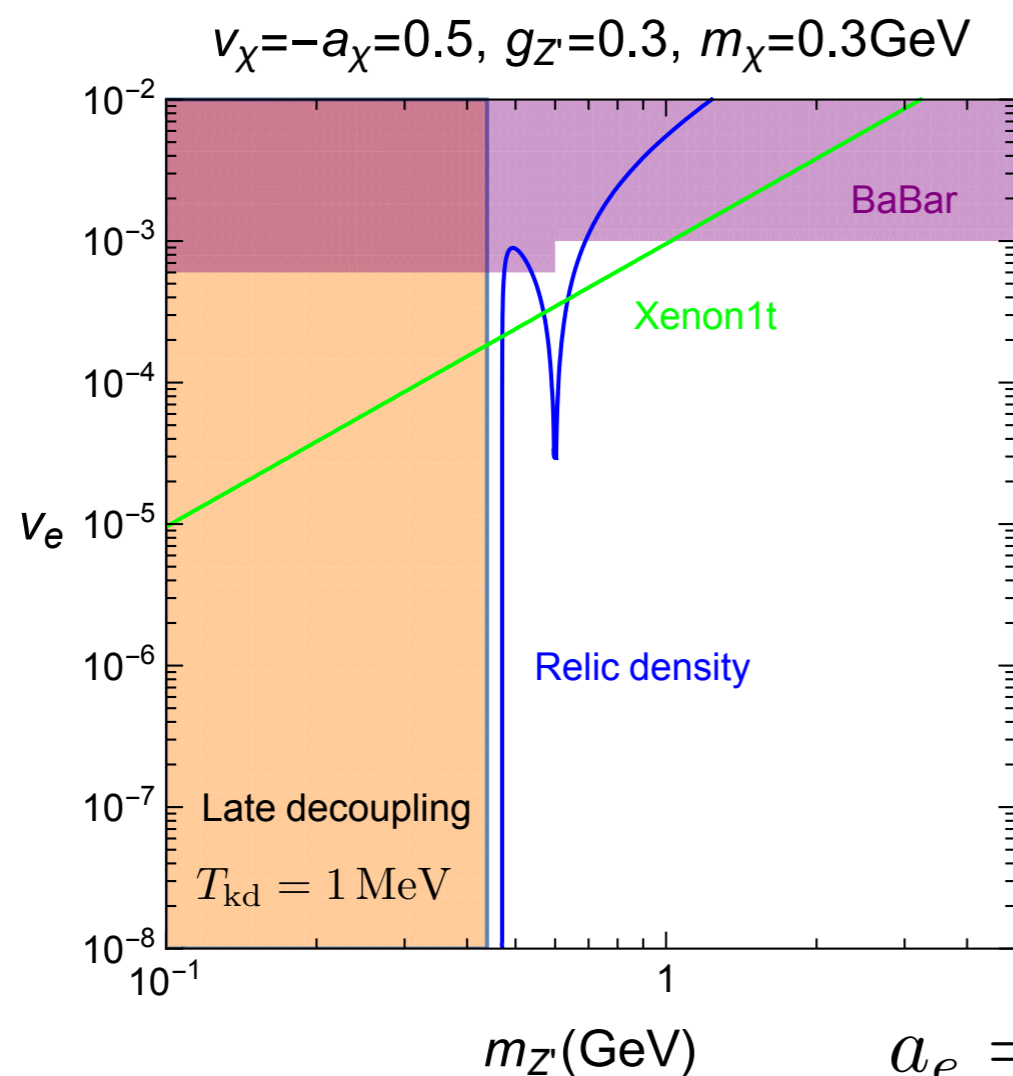
XENONIT + relic

-24-

- Electron couplings are constrained by visible/invisible searches at BaBar, beam dump, meson decays, Belle-2.

$$m_{Z'} \lesssim 10 \text{ GeV} \quad \longrightarrow \quad |v_e|g_{Z'} \lesssim (10^{-4} - 10^{-3}) e$$

- DM relic density & decoupling condition can be satisfied.



$$a_e = v_\nu = a_\nu = 0$$

Pseudo-Dirac dark matter

-25-

- Dark matter = singlet Dirac fermion, vector-like under Z' , which is broken by dark Higgs VEV v_ϕ .

$$\mathcal{L} = -\frac{1}{4}F'_{\mu\nu}F'^{\mu\nu} + |D_\mu\phi|^2 - V(\phi, H) \\ + i\bar{\psi}_{1L}\gamma^\mu D_\mu\psi_{1L} + i\bar{\psi}_{2L}\gamma^\mu D_\mu\psi_{2L} \\ - \underbrace{m_\psi\psi_1\psi_2}_{\text{“Dirac mass”}} - \underbrace{y_1\phi\psi_1\psi_1 + y_2\phi^*\psi_2\psi_2}_{\text{“Majorana masses”}} + \text{h.c.}$$

Mass eigenvalues: $m_{\chi_{1,2}}^2 = m_\psi^2 + 2(y_1^2 + y_2^2)v_\phi^2 \pm 2\sqrt{(y_1^2 - y_2^2)^2v_\phi^4 + (y_1 + y_2)^2v_\phi^2m_\psi^2}$,

Mixing angle: $\sin 2\theta = -\frac{4(y_1 + y_2)v_\phi m_\psi}{m_{\chi_2}^2 - m_{\chi_1}^2}$.

$y_1 = y_2$: $m_{\chi_{1,2}} = m_\psi \pm 2y_1v_\phi$, $\theta = \frac{\pi}{4}$.

“Technically natural splitting” $\Delta m = 4|y_1|v_\phi = 2.5 \text{ keV}$



Z' -DM int:


$$\mathcal{L}_{\text{DM}} = g_{Z'}Z'_\mu \left(\bar{\chi}_1\gamma^\mu P_L\chi_2 + \bar{\chi}_2\gamma^\mu P_L\chi_1 \right).$$

Z'-portal for ExoDM

-26-

- Z' mediates to the SM by gauge kinetic mixing,

$$\mathcal{L}_{\text{kin-mix}} = -\frac{1}{2} \sin \xi B_{\mu\nu} F'^{\mu\nu}$$


$$\mathcal{L}_{\text{eff,I}} = -e\varepsilon Z'_\mu \left(\bar{e}\gamma^\mu e + \frac{m_{Z'}^2}{2c_W^2 m_Z^2} \bar{\nu}\gamma^\mu P_L \nu \right) + \dots$$

$$\varepsilon \equiv \xi \cos \theta_W \ll 1$$

$v_e = -\frac{e\varepsilon}{g_{Z'}}, \quad a_e = 0, \quad v_\nu = -a_\nu = -\frac{e\varepsilon m_{Z'}^2}{4c_W^2 g_{Z'} m_Z^2}.$

- Completely safe from diffuse X-ray bounds.
- ExoDM decays dominantly into neutrinos.

$$\tau_{\chi_1} = \frac{1}{\Gamma(\chi_1 \rightarrow \chi_2 \nu \bar{\nu})} = \left(\frac{10^{-4} e}{\varepsilon g_{Z'}} \right)^2 \left(\frac{2.5 \text{ keV}}{\Delta m} \right)^5 8.9 \times 10^{24} \text{ sec}$$

: Consistent with lifetime bound.

Vector-like lepton portal

-27-

- Vector-like lepton E with nonzero Z' charge.

$$\mathcal{L}_{\text{VL}} = -M_E \bar{E} E - (y_E \phi \bar{E} e_R + \text{h.c.})$$



Mass matrix:

$$M_e = \begin{pmatrix} m_e & 0 \\ y_E v_\phi & M_E \end{pmatrix}$$

Mass eigenvalues: $m_{f_{1,2}}^2 = \frac{1}{2} \left(m_e^2 + M_E^2 + y_E^2 v_\phi^2 \mp \sqrt{(m_e^2 + y_E^2 v_\phi^2 - M_E^2)^2 + 4y_E^2 v_\phi^2 M_E^2} \right)$

Mixing angles:

$$\sin(2\theta_R) = -\frac{2y_E v_\phi M_E}{m_{f_1}^2 - m_{f_2}^2},$$

$$\sin(2\theta_L) = \frac{m_e^2}{m_{f_1} m_{f_2}} \sin(2\theta_R).$$

$$m_e, y_E v_\phi \ll M_E : \quad \theta_R \sim \frac{2y_E v_\phi}{M_E}, \quad \theta_L \sim \frac{m_e}{M_E} \theta_R.$$

$$m_{f_1} \sim m_e, \quad M_E \gtrsim 100 \text{ GeV} : \quad \theta_R \lesssim \sqrt{\frac{m_e}{M_E}} \lesssim 2.2 \times 10^{-3},$$

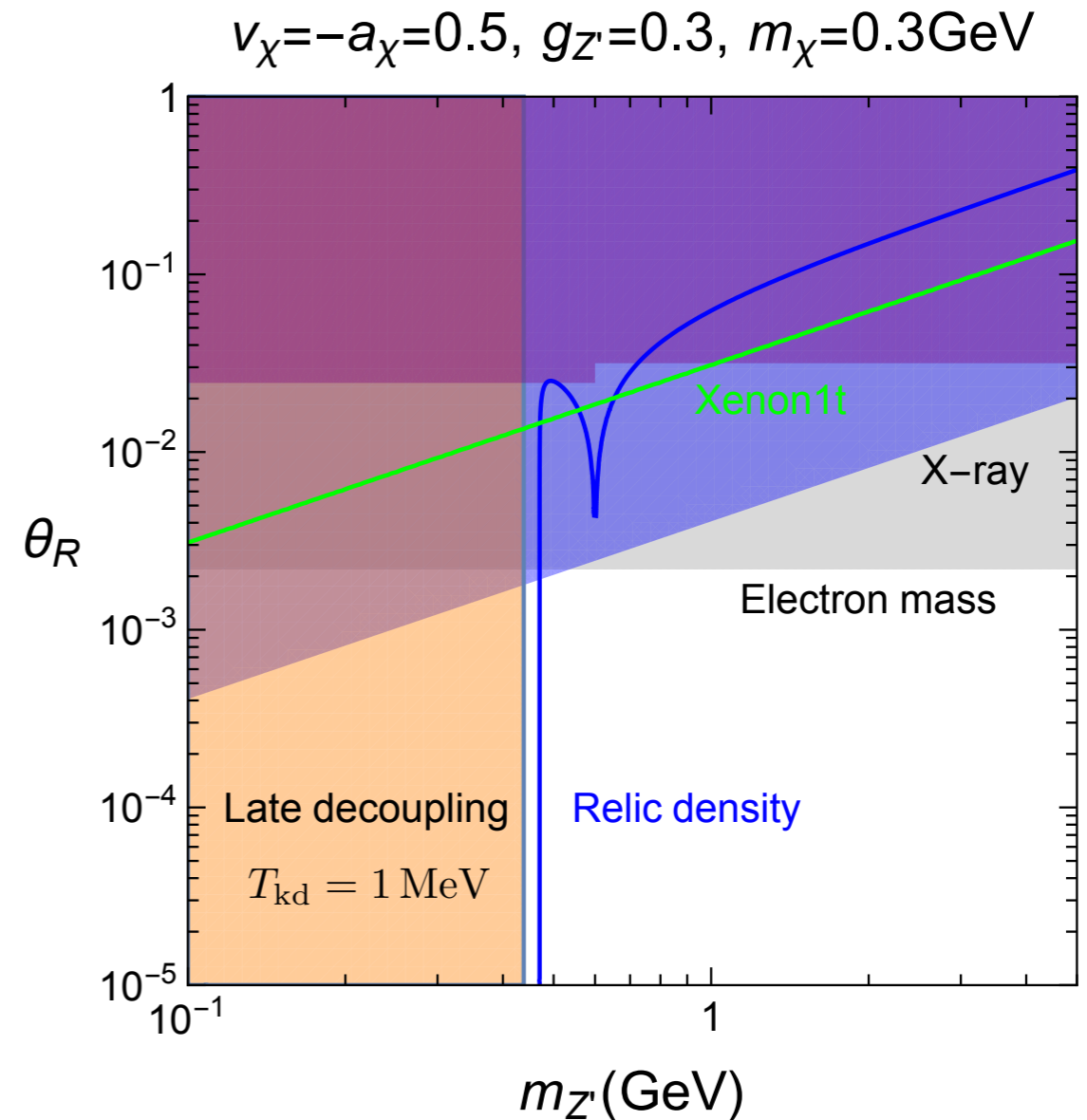
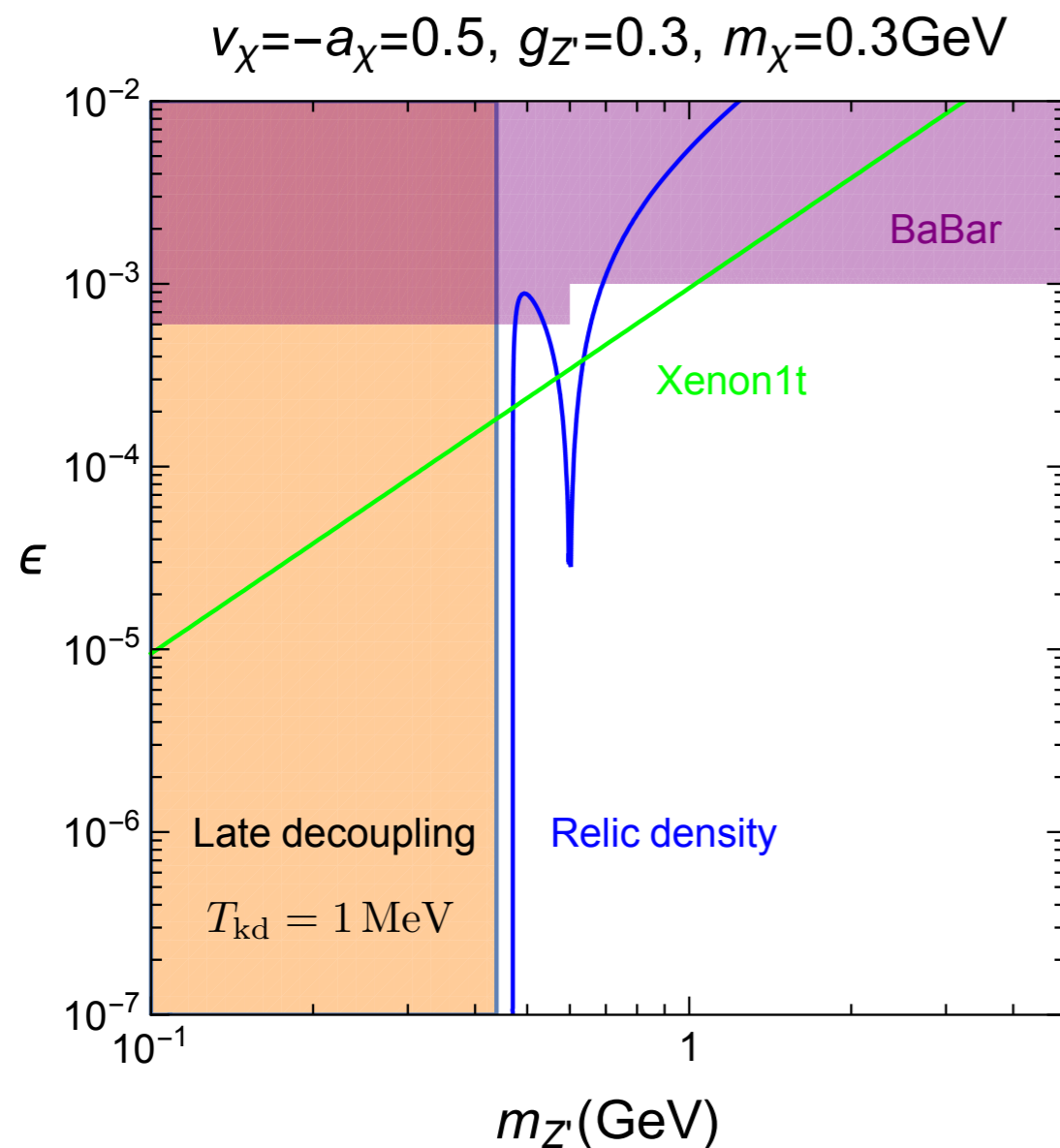
Z' -DM int:

$$v_e = a_e = -\theta_R^2, \quad v_\nu = a_\nu = 0.$$

Portals & XENON1T

-28-

- Z' portal is consistent with Xenon1t excess; VL portal is highly constrained by X-ray bounds.



Dark mesons

Dark light fermions
 $G = \text{SU}(N_f)_L \times \text{SU}(N_f)_R$



$N_f = 3 :$

$$M_{\text{diag}} = \text{diag}(m'_1, m'_2, m'_3)$$

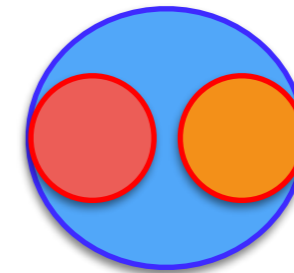
Meson masses:

$$\begin{aligned} m_{\tilde{\pi}^\pm}^2 &= \mu(m'_1 + m'_2), \\ m_{\tilde{K}^\pm}^2 &= \mu(m'_1 + m'_3), \\ m_{\tilde{K}^0}^2 &= \mu(m'_2 + m'_3), \end{aligned}$$

Condensate
 in dark QCD
 $\langle \bar{q}q \rangle = \mu^3 \neq 0$



Dark mesons
 $H = \text{SU}(N_f)_V$ flavor sym.




$$\pi = \frac{1}{\sqrt{2}} \begin{pmatrix} \frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta^0 & \pi^+ & K^+ \\ \pi^- & -\frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta^0 & K^0 \\ K^- & \bar{K}^0 & -\frac{2}{\sqrt{6}}\eta^0 \end{pmatrix}$$

$$M_0^2 = \mu \begin{pmatrix} m'_1 + m'_2 & \frac{1}{\sqrt{3}}(m'_1 - m'_2) \\ \frac{1}{\sqrt{3}}(m'_1 - m'_2) & \frac{1}{3}(m'_1 + m'_2 + 4m'_3) \end{pmatrix}$$

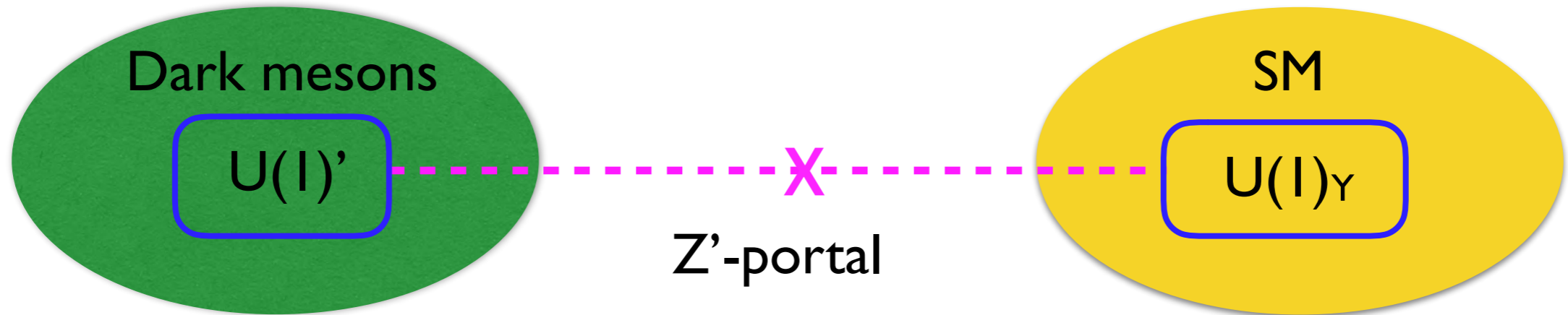
$\tilde{\pi}^0, \tilde{\eta}^0$ mix

$\text{SU}(3)_V$ dark flavor symmetry: $m'_1 = m'_2 = m'_3$

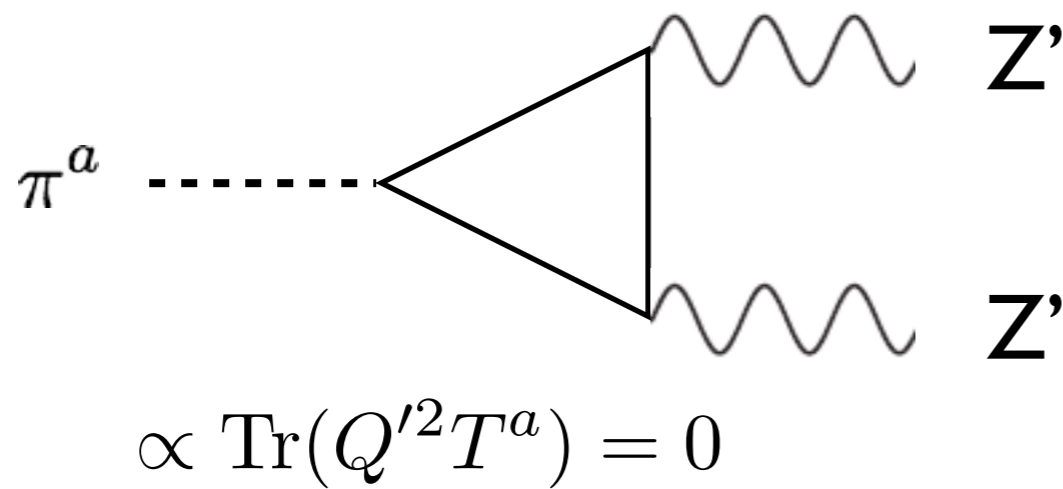

 $\left\{ \begin{array}{l} m_{\tilde{\pi}}^2 = 2\mu m'_1 : \text{common masses for dark mesons} \\ \text{Stability of dark mesons} \end{array} \right.$

Z'-portal for dark mesons

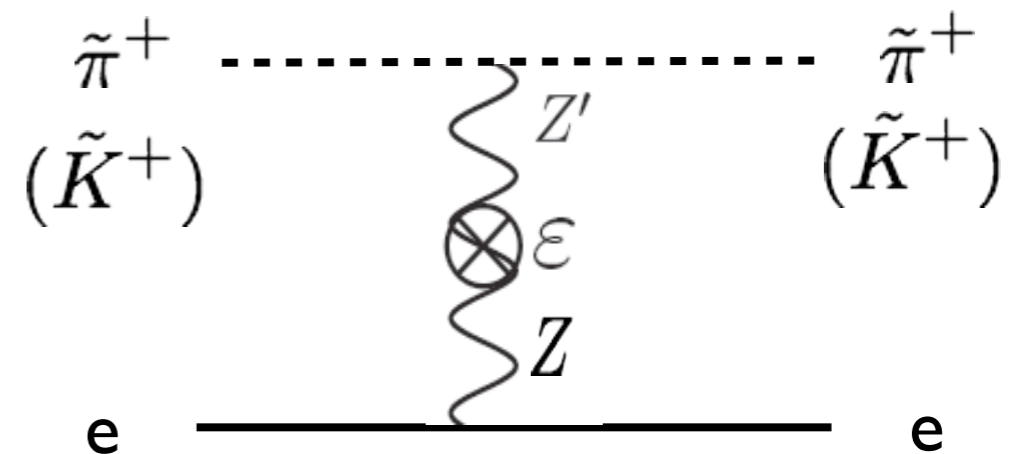
-30-



- Z' with no dark chiral anomalies ensure stable mesons. [HML, M. Seo, 2015]



→ $Q' = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$



$$\mathcal{L}_{\text{mix}} = -\frac{\epsilon}{2 \cos \theta_W} F'_{\mu\nu} F^{\mu\nu}$$

- Kinetic equilibrium: $|\epsilon|g_{Z'} \gtrsim 1.1 \times 10^{-8} \left(\frac{m_{Z'}}{1 \text{ GeV}}\right)^2 \left(\frac{x_f}{15}\right)^3 \left(\frac{300 \text{ MeV}}{m_\pi}\right)^{3/2}$

Split masses for dark mesons

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- Mass splitting due to flavor mixing [S.Choi, HML, B. Zhu, to appear]

Mixings due to broken U(1)'

$$\mathcal{L}_{\text{mix}} = -y_{12} \phi \bar{u}' d' - y_{13} \phi \bar{u}' s' - \text{h.c.}$$

$$\longrightarrow M = \begin{pmatrix} m_1 & \epsilon & \epsilon' \\ \epsilon & m_1 & 0 \\ \epsilon' & 0 & m_1 \end{pmatrix}$$

$$\begin{aligned} & \xrightarrow{\text{blue arrow}} \begin{cases} m_{\tilde{\pi}^\pm}^2 = m_\pi^2, \\ m_{\tilde{\pi}^0}^2 = m_\pi^2 \left(1 - \frac{2\Delta m}{\sqrt{3}m_\pi}\right), \end{cases} & \begin{cases} m_{\tilde{K}^\pm}^2 = m_\pi^2 \left(1 - \frac{\Delta m}{m_\pi}\right), \\ m_{\tilde{K}^0}^2 = m_\pi^2 \left(1 + \frac{\Delta m}{m_\pi}\right), \end{cases} & m_{\tilde{\eta}^0}^2 = m_\pi^2 \left(1 + \frac{2\Delta m}{\sqrt{3}m_\pi}\right) \\ m_\pi^2 \equiv 2\mu m_1 & & & & & \\ \Delta m \equiv \mu \sqrt{\epsilon^2 + \epsilon'^2} / m_\pi & & & & & \end{aligned}$$

Meson mass splitting:

$$m_{\tilde{K}^0} - m_{\tilde{K}^\pm} \simeq \Delta m, \quad m_{\tilde{\pi}^\pm} - m_{\tilde{\pi}^0} \simeq \frac{1}{\sqrt{3}} \Delta m.$$

- Mass corrections due to Z'

$$m_{K_{1,2}}^2 = m_{\tilde{\pi}}^2 - \delta \pm \sqrt{\delta^2 + m_{\tilde{\pi}}^2 (\Delta m)^2}$$

$$\delta = c g_{Z'}^2 f_\pi^2, \quad c \sim \frac{1}{16\pi^2} \frac{\mu^2}{m_{Z'}^2}$$

$$m_{\tilde{\pi}^0}^2 = m_{\tilde{\pi}}^2 \left(1 - \frac{2\Delta m}{\sqrt{3}m_{\tilde{\pi}}}\right) - 2\delta,$$

$$m_{\tilde{\pi}^1}^2 = m_{\tilde{\pi}}^2,$$

$$m_{\tilde{\pi}^2}^2 = m_{\tilde{\pi}}^2 - 2\delta.$$

Negligible Z' corrections for $m_{Z'} \gtrsim 0.6\mu \left(\frac{g_{Z'}}{0.01}\right) \left(\frac{0.2}{m_{\tilde{\pi}}/f_\pi}\right) \left(\frac{m_{\tilde{\pi}}/100 \text{ MeV}}{\Delta m/4 \text{ keV}}\right)^{1/2}$

Exothermic dark mesons

-32-

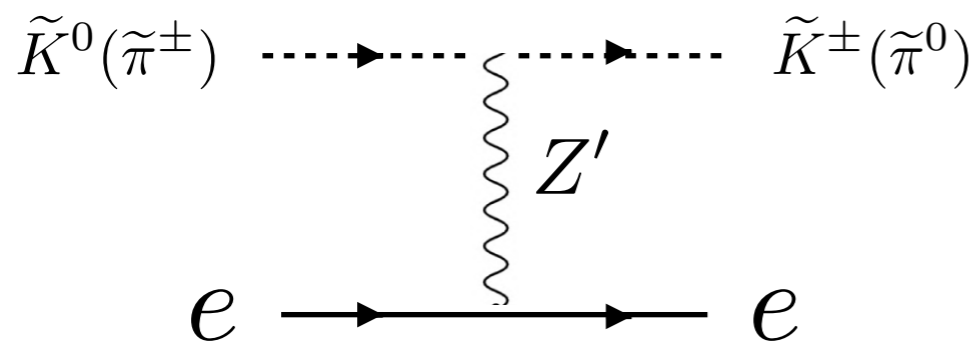
- Non-universal dark U(1)’: $[Q', M] \neq 0$

$$\mathcal{L}_{Z', 2\pi} = 2ig_{Z'} Z'_\mu \left(K^+ \partial^\mu K^- - K^- \partial^\mu K^+ + \pi^+ \partial^\mu \pi^- - \pi^- \partial^\mu \pi^+ \right) + 4g_{Z'}^2 Z'_\mu Z'^\mu (K^+ K^- + \pi^+ \pi^-).$$



Flavor mixing

$$\begin{aligned} \mathcal{L}_{Z', \text{int}} = & ig_{Z'} Z'_\mu \left[(\tilde{K}^0 + \tilde{K}^+) \partial^\mu (\overline{\tilde{K}^0} + \tilde{K}^-) - (\overline{\tilde{K}^0} + \tilde{K}^-) \partial^\mu (\tilde{K}^0 + \tilde{K}^+) \right. \\ & \left. + \sqrt{2}(\tilde{\pi}^- - \tilde{\pi}^+) \partial^\mu \tilde{\pi}^0 - \sqrt{2}\tilde{\pi}^0 \partial^\mu (\tilde{\pi}^- - \tilde{\pi}^+) \right] \\ & + g_{Z'}^2 Z'_\mu Z'^\mu \left[2(\tilde{K}^0 + \tilde{K}^+) (\overline{\tilde{K}^0} + \tilde{K}^-) + 2(\tilde{\pi}^0)^2 - (\tilde{\pi}^- - \tilde{\pi}^+)^2 \right]. \end{aligned}$$



Meson-changing Z' interactions



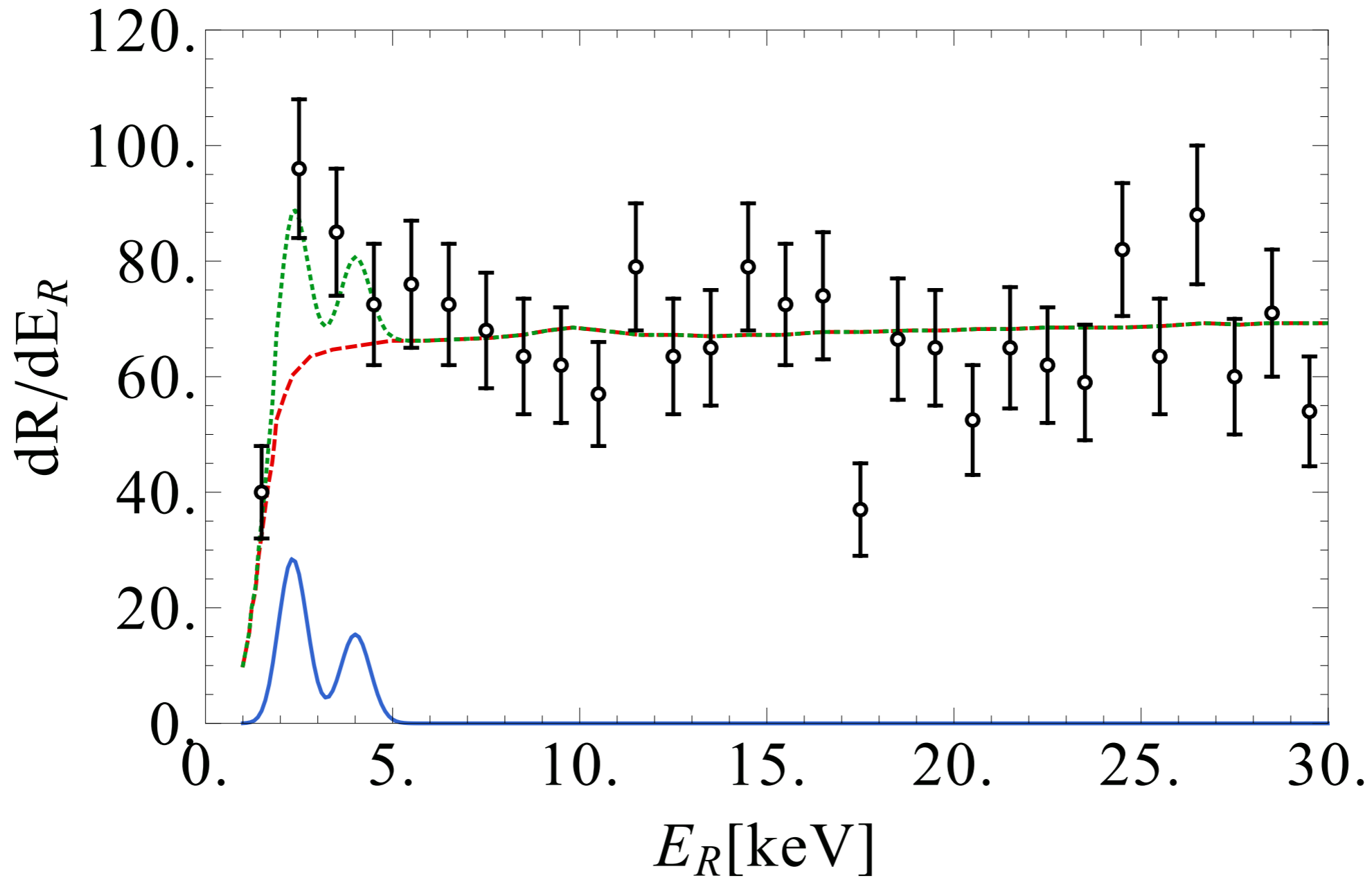
Exothermic DM-e scattering

[S.Choi, HML, B. Zhu, to appear]

Double peaks in electron E_R

[S.Choi, HML, B. Zhu, to appear]

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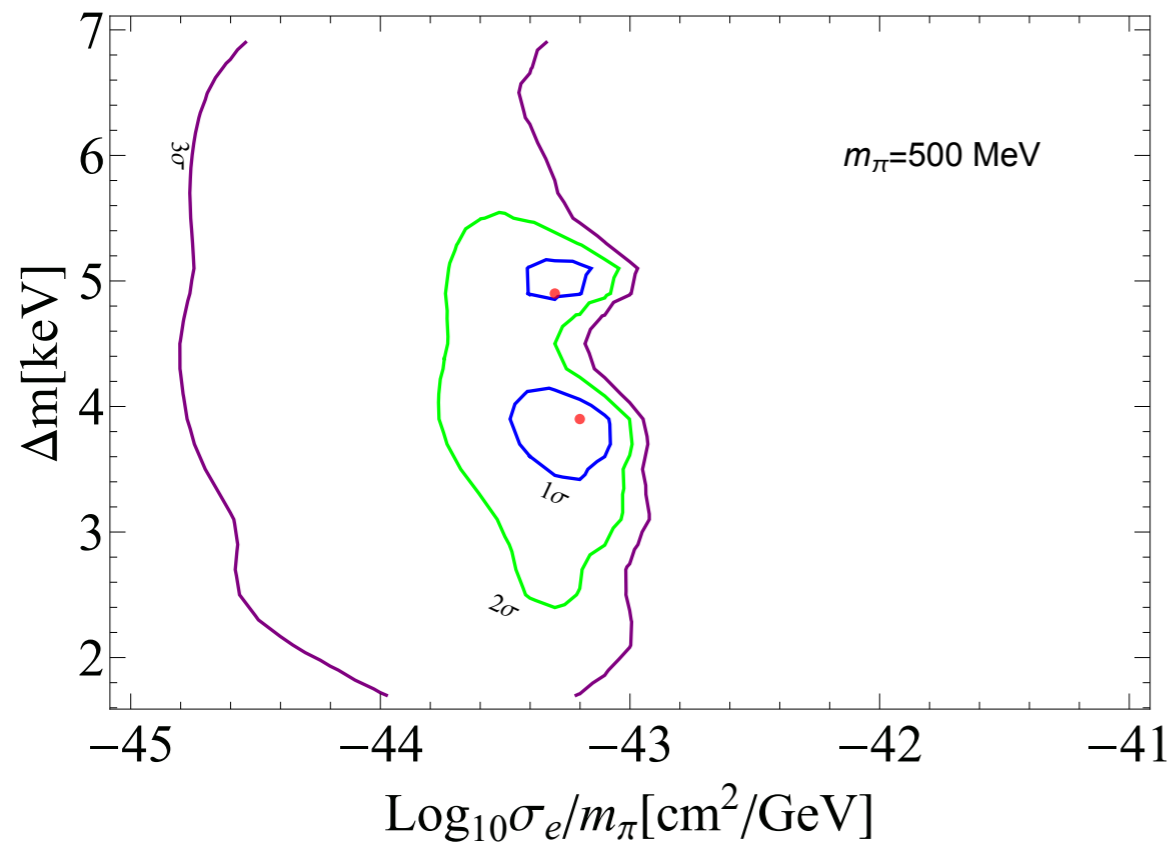


$$m_{\tilde{\pi}^\pm} - m_{\tilde{\pi}^0} = \Delta m = 2.3 \text{ keV}, \quad m_{\tilde{K}^0} - m_{\tilde{K}^\pm} = \sqrt{3}\Delta m = 4.0 \text{ keV}.$$

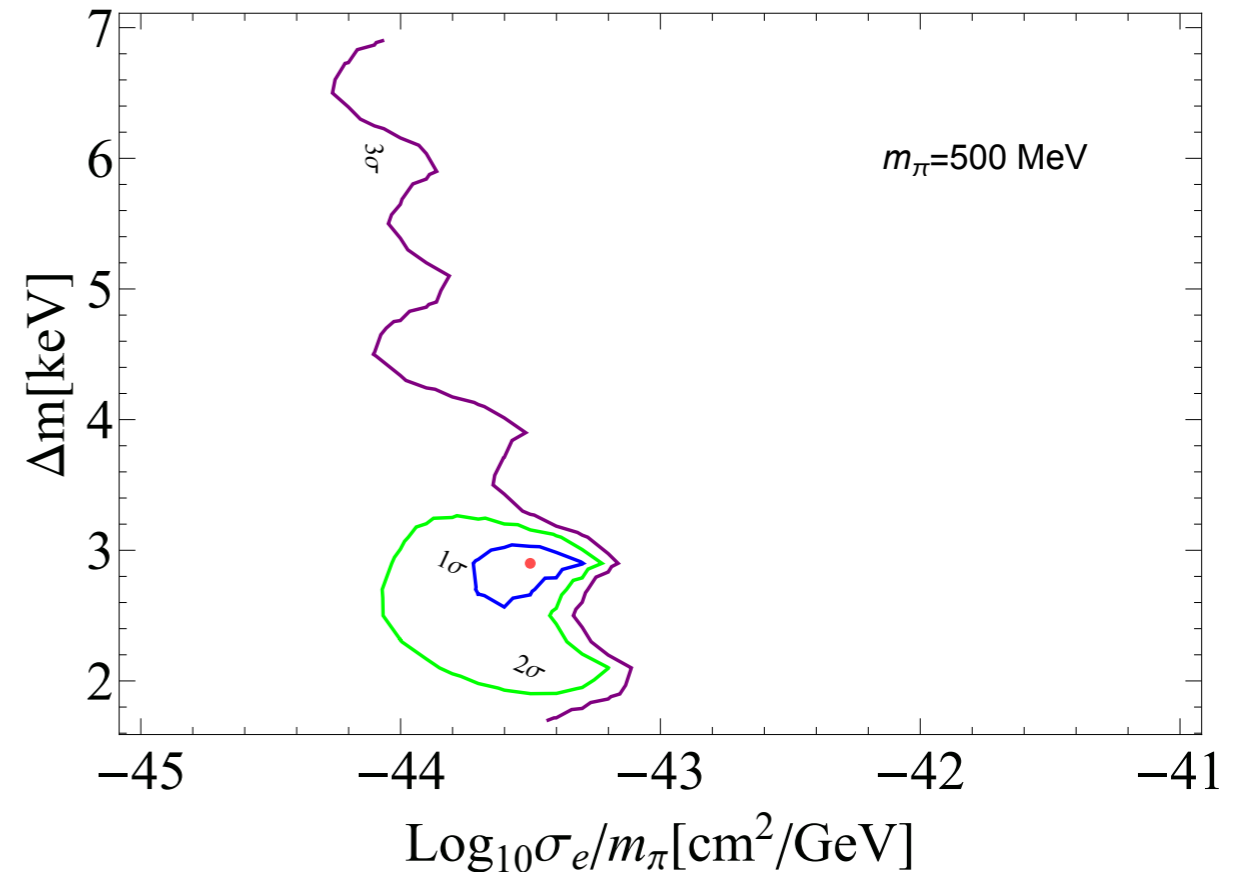
Double peaks vs single peak

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Two-Peak Fit



One-Peak Fit



[S.Choi, HML, B. Zhu, to appear]

Double-peak best-fit:

$$[\Delta m = 3.9 \text{ keV}, \bar{\sigma}_e/m_{\bar{\pi}} = 2 \times 10^{-43} \text{ cm}^2/\text{GeV}],$$

$$\chi_{\min}^2 = 1.48$$

One-peak best-fit:

$$[\Delta m = 2.9 \text{ keV}, \bar{\sigma}_e/m_{\bar{\pi}} = 1.3 \times 10^{-43} \text{ cm}^2/\text{GeV}],$$

$$\chi_{\min}^2 = 2.43$$

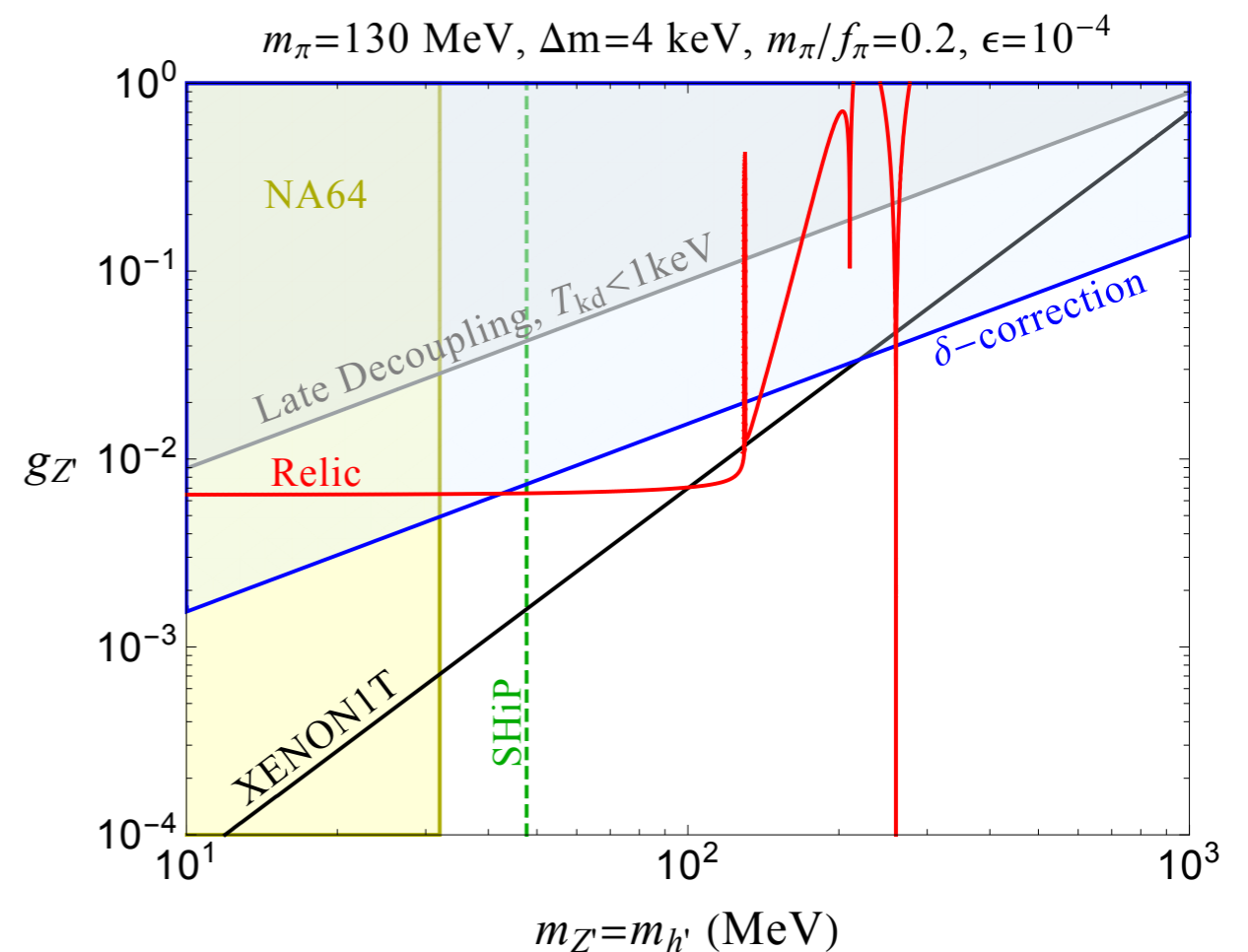
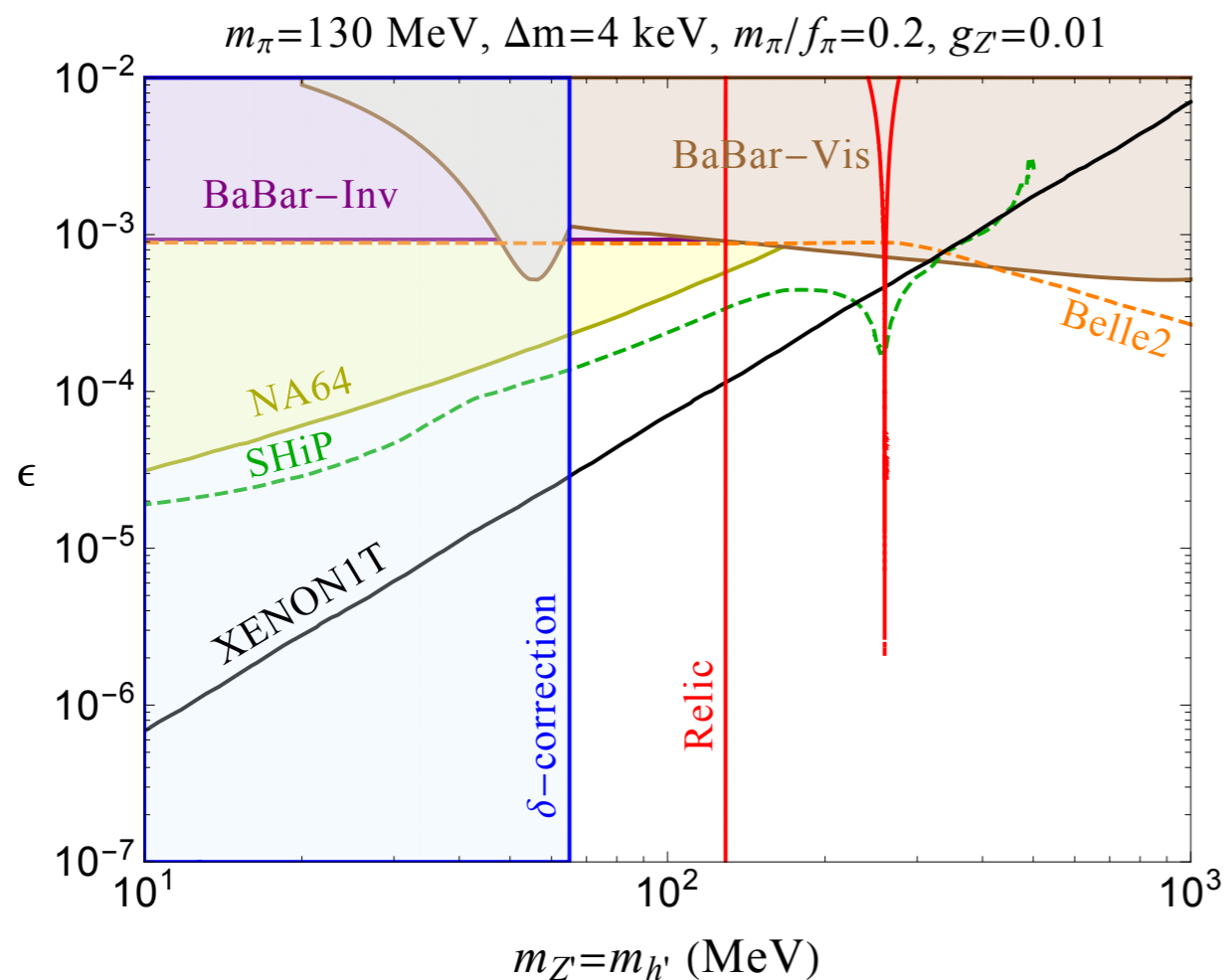


Double-peak case fits better than one-peak case.

Dark mesons & XENONIT

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- Strong bounds from late decoupling & Z' mass corrections \Rightarrow new light fermions, protection symmetry?
- Resonance and forbidden regions can be searched for in intensity & beam dump experiments.



Conclusions

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- The Xenon electron excess can be explained by **down-scattering of exothermic dark matter** for standard halo model.
- **Light dark matter and mediator** favored by Xenon excess can have large self-scattering cross section to solve small-scale problems.
- **Pseudo-Dirac dark fermion** are natural candidates for exothermic dark matter with Z' portal and self-interacting with velocity dependence.
- **Dark mesons with approximate flavor symmetry** lead to testable signatures with two peaks in electron recoil energy and fit better to Xenon excess.