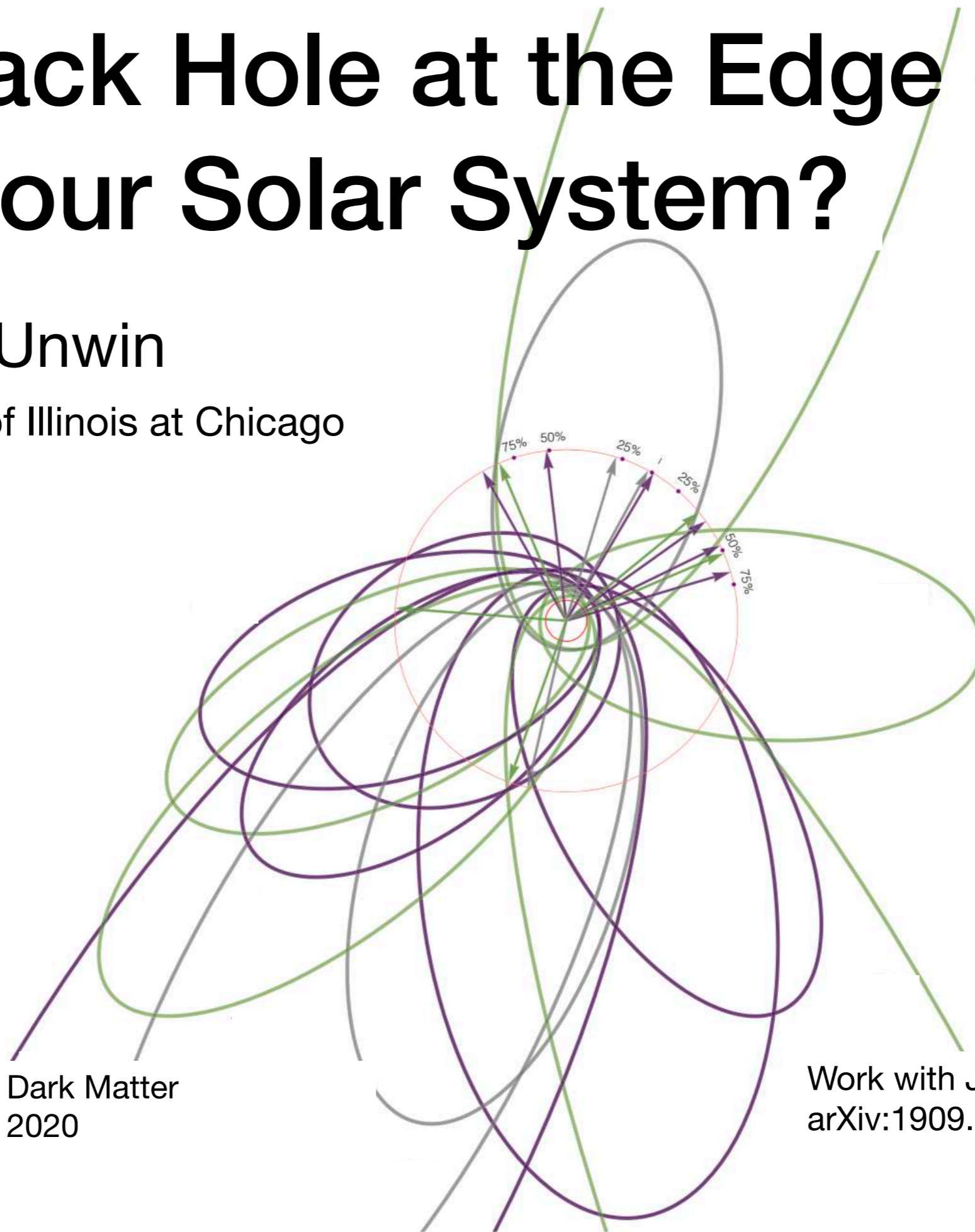


# A Black Hole at the Edge of our Solar System?

James Unwin

University of Illinois at Chicago



New Trends in Dark Matter  
8th December 2020

Work with Jakub Scholtz  
arXiv:1909.11090

# Outline

- 1. The Case for Planet 9**
- 2. Something in the Outer Solar System**
- 3. Dark Matter around PBHs**



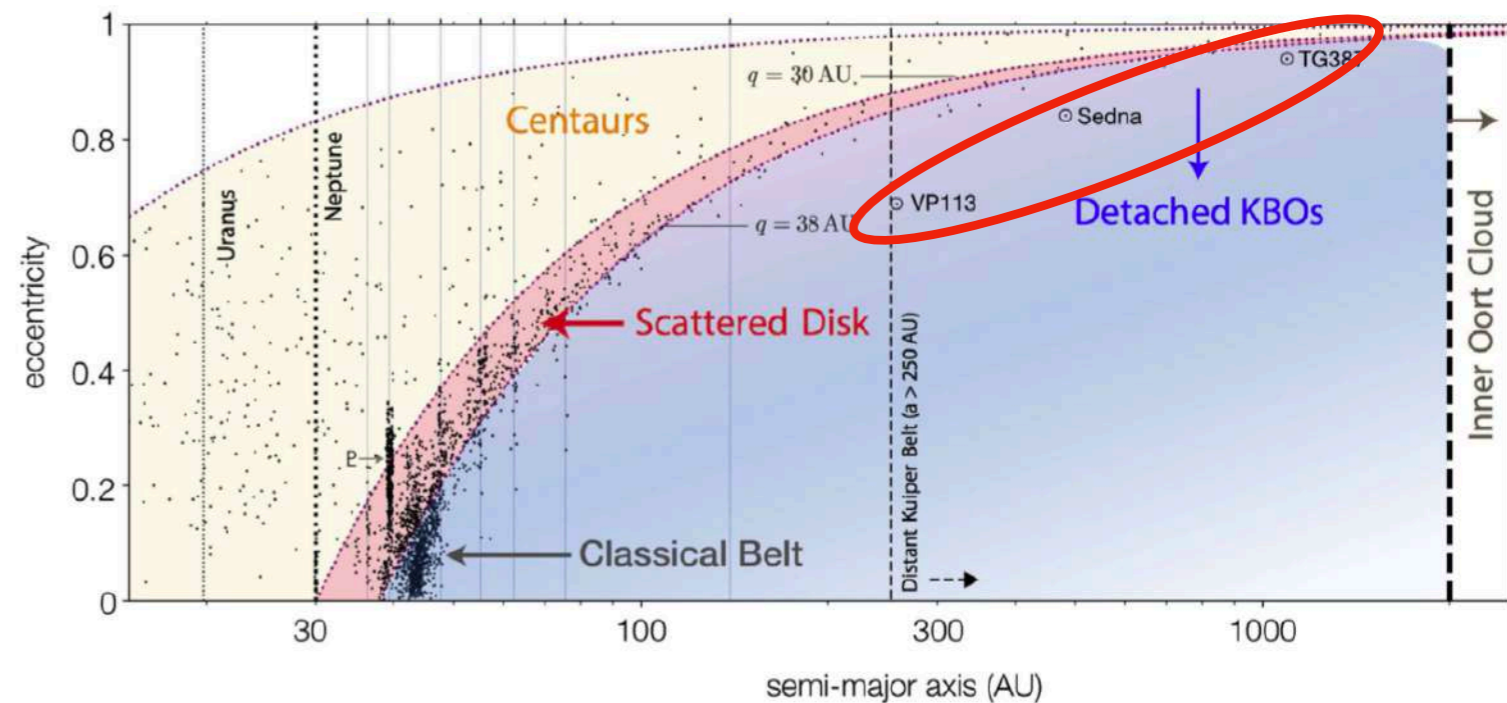
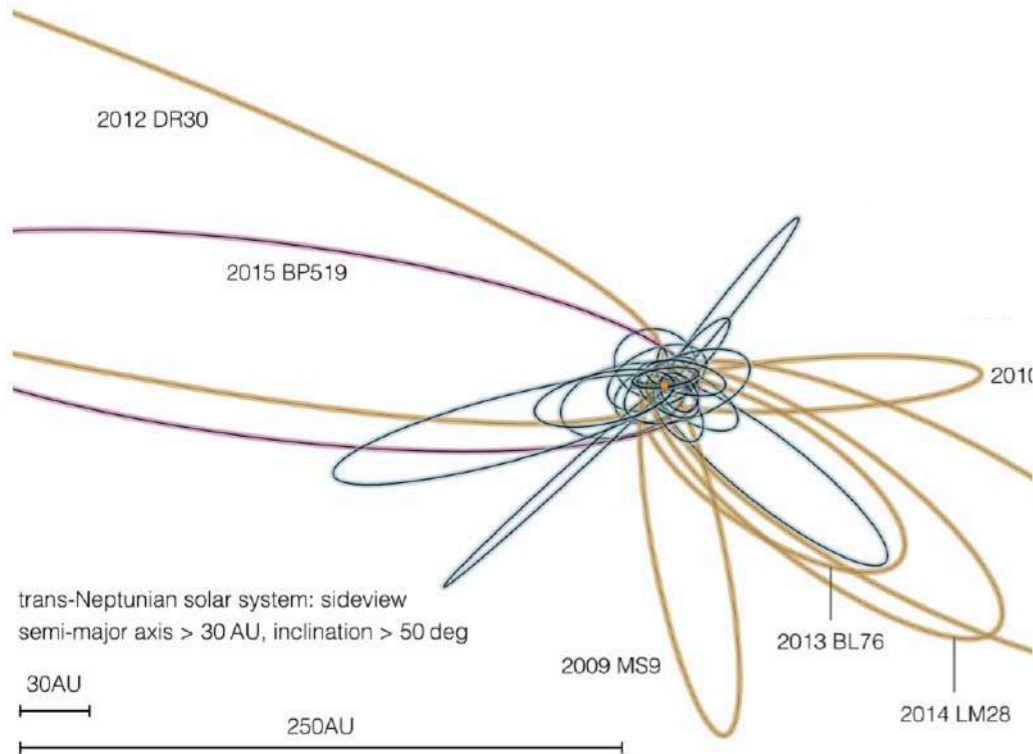
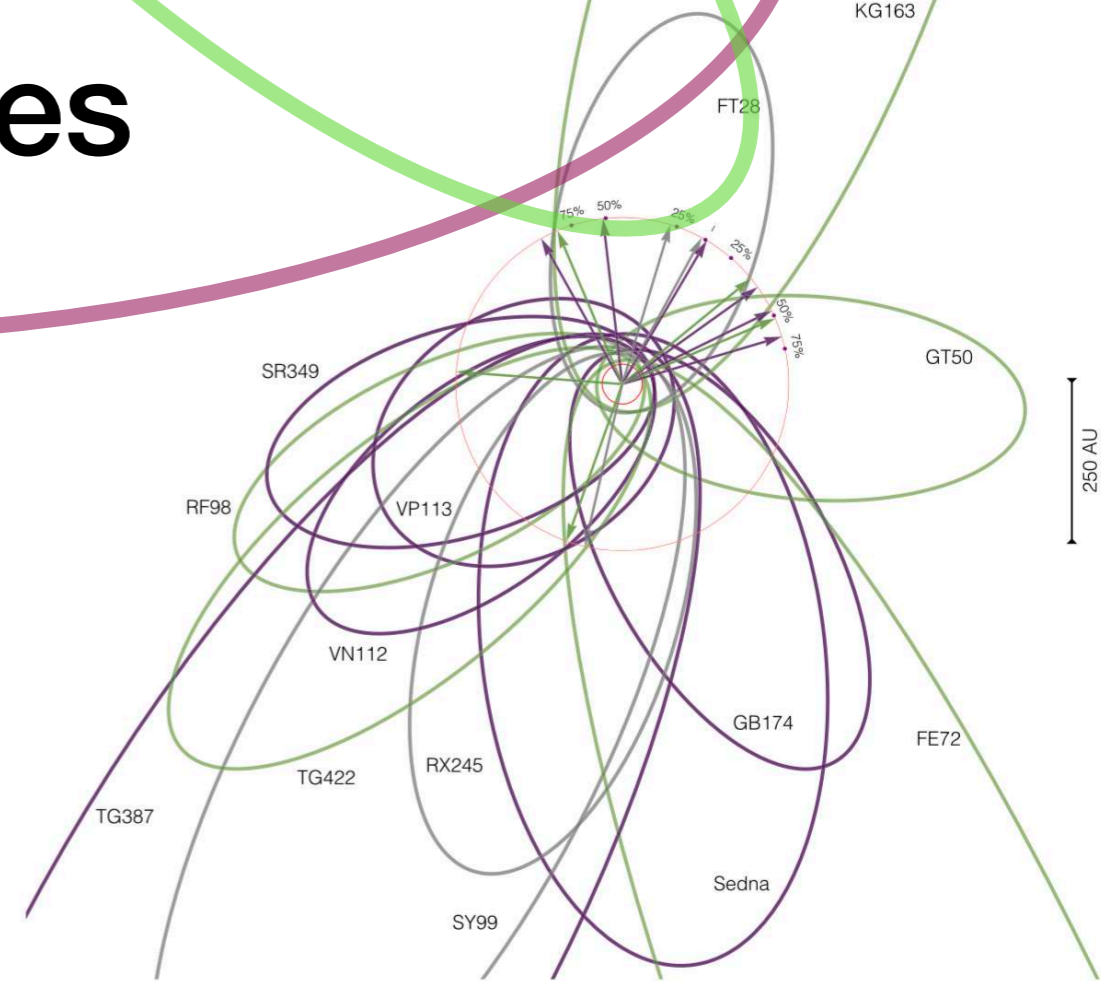
# I. The Case for Planet 9



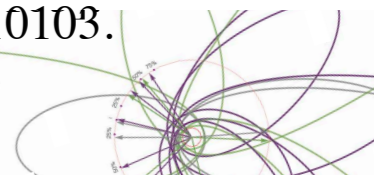
# TNO Anomalies

There are several Trans-Neptunian anomalies:

- i) Unexpected clustering in eTNO orbits
- ii) The existence of high perihelia ( $q \sim 70$  AU) TNOs, such as Sedna, collectively called Sednoids
- iii) TNOs moving roughly perpendicularly to the planetary plane (with inclination  $i \gtrsim 50^\circ$ )



Batygin, Adams, Brown, & Becker, *Phys. Rep.* (2019), arXiv:1902.10103.



# Planet 9

Chance of **random alignment** of TNOs  $\sim 1$  in 15,000.

Batygin & Brown [1601.05438].

Observational bias is claimed to be accounted for.

Brown [1706.04175].

All of the TNO anomalies can be **simultaneously explained** by a new gravitational source in the outer Solar System: Planet 9.

From simulations **best fits**:

Benchmark	$a$ (AU)	$e$	$i$ (deg)
$5M_{\oplus}$	450	0.2	20
$10M_{\oplus}$	700	0.4	15

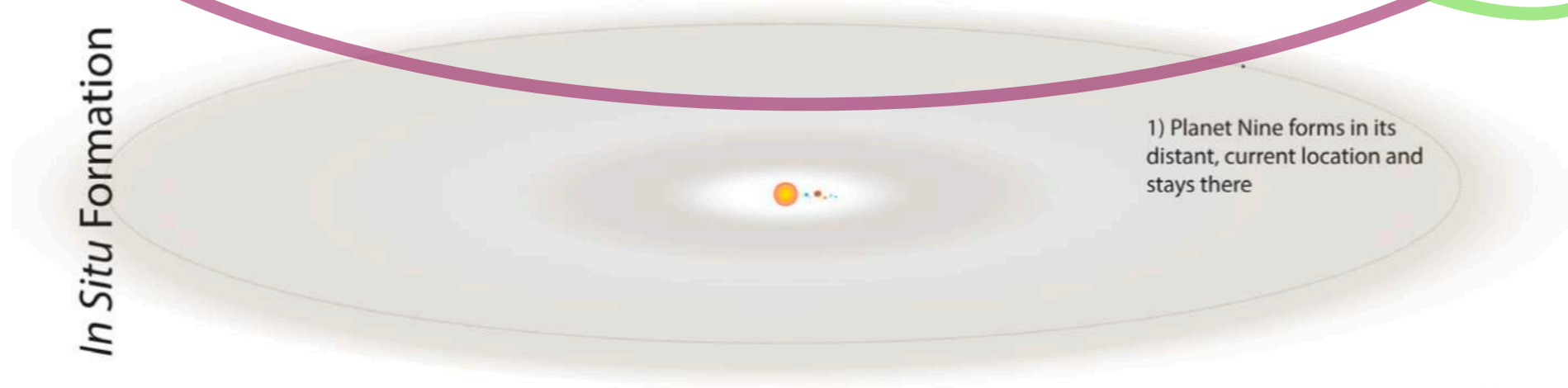


## II. Something in the Outer Solar System



# Origins of Planet 9

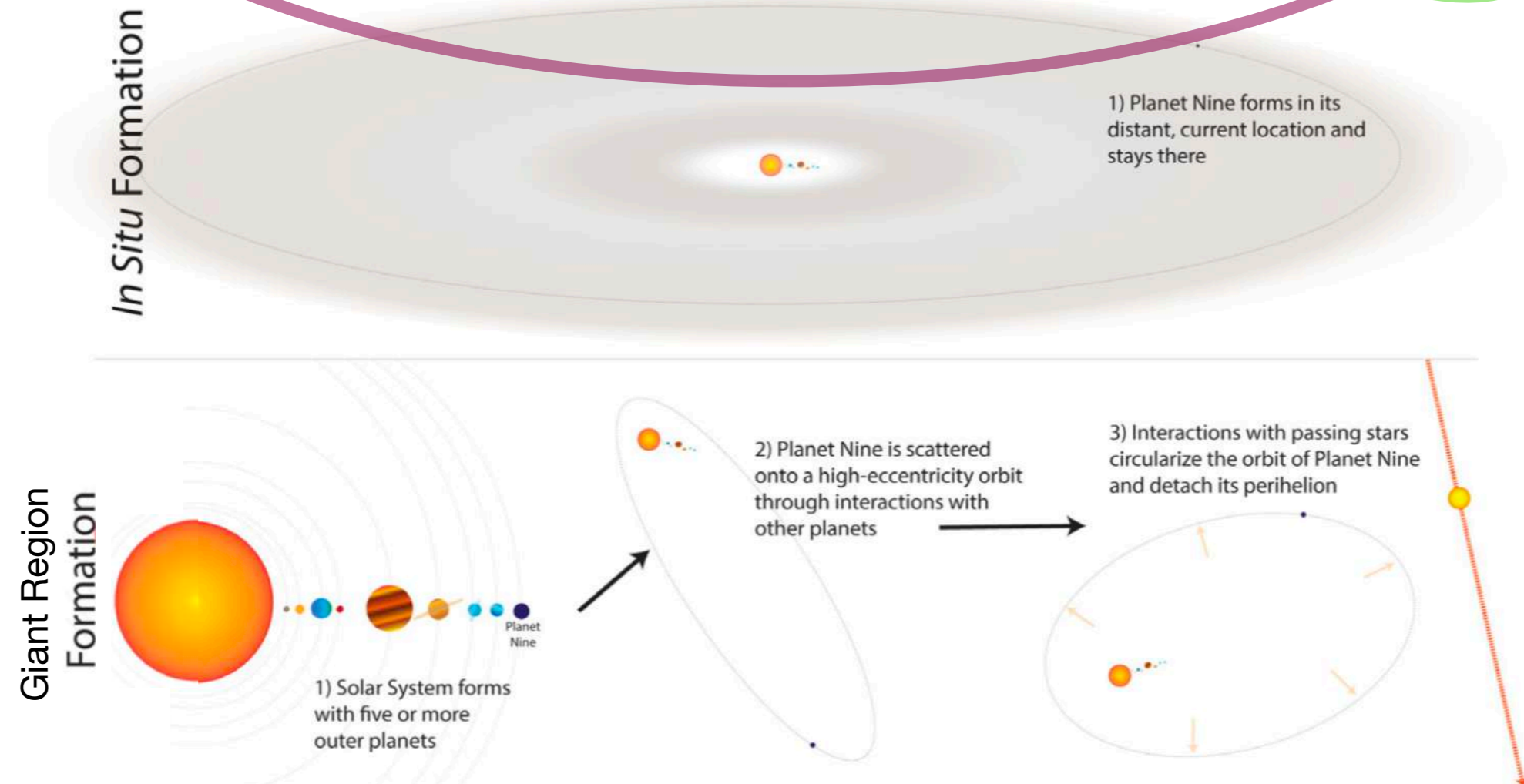
*In Situ Formation*



1) Planet Nine forms in its distant, current location and stays there



# Origins of Planet 9

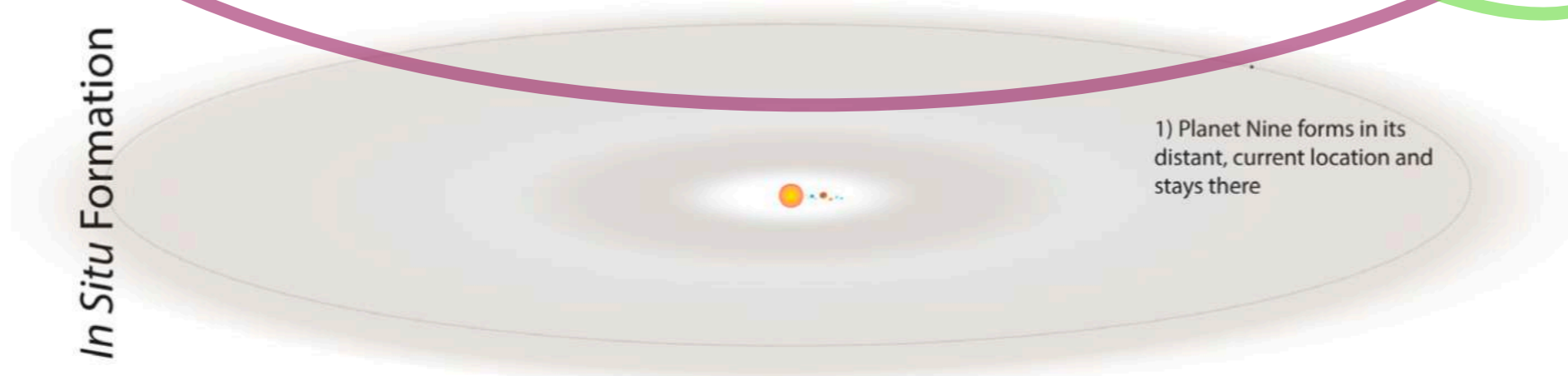


Batygin, et al [arXiv:1902.10103].

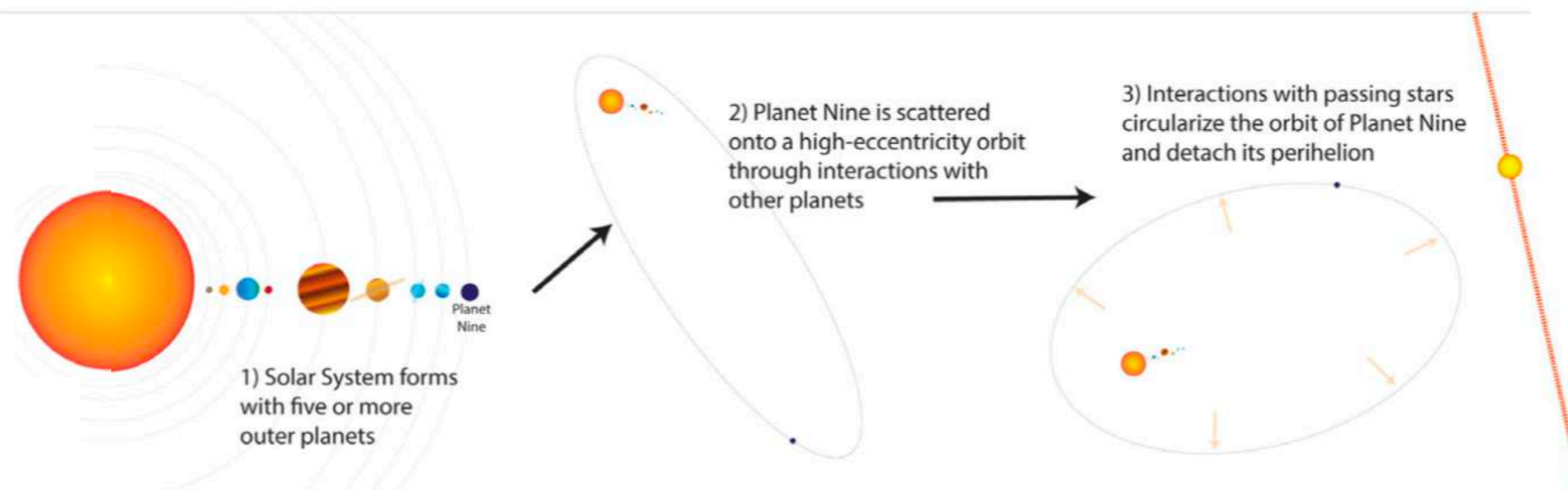


# Origins of Planet 9

In Situ Formation



Giant Region Formation



Capture



Batygin, et al [arXiv:1902.10103].



# “Something” Out There?

The evidence is quite compelling... But the claim is extraordinary.

Not least because it's **HIGHLY** unlikely to get a large planet into that orbit.

Raises the question: **Does it need to be a planet?**



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Alternatives:

- A compact dark matter microhalo.
- An axion minicluster
- Exotic Bose/Fermi/Dark Matter star
- Or perhaps, a Primordial Black Hole.

Mechanism of **gravitational capture** for planet or more “exotic” massive object similar, except for relevant parameter values.



# Primordial Black Holes

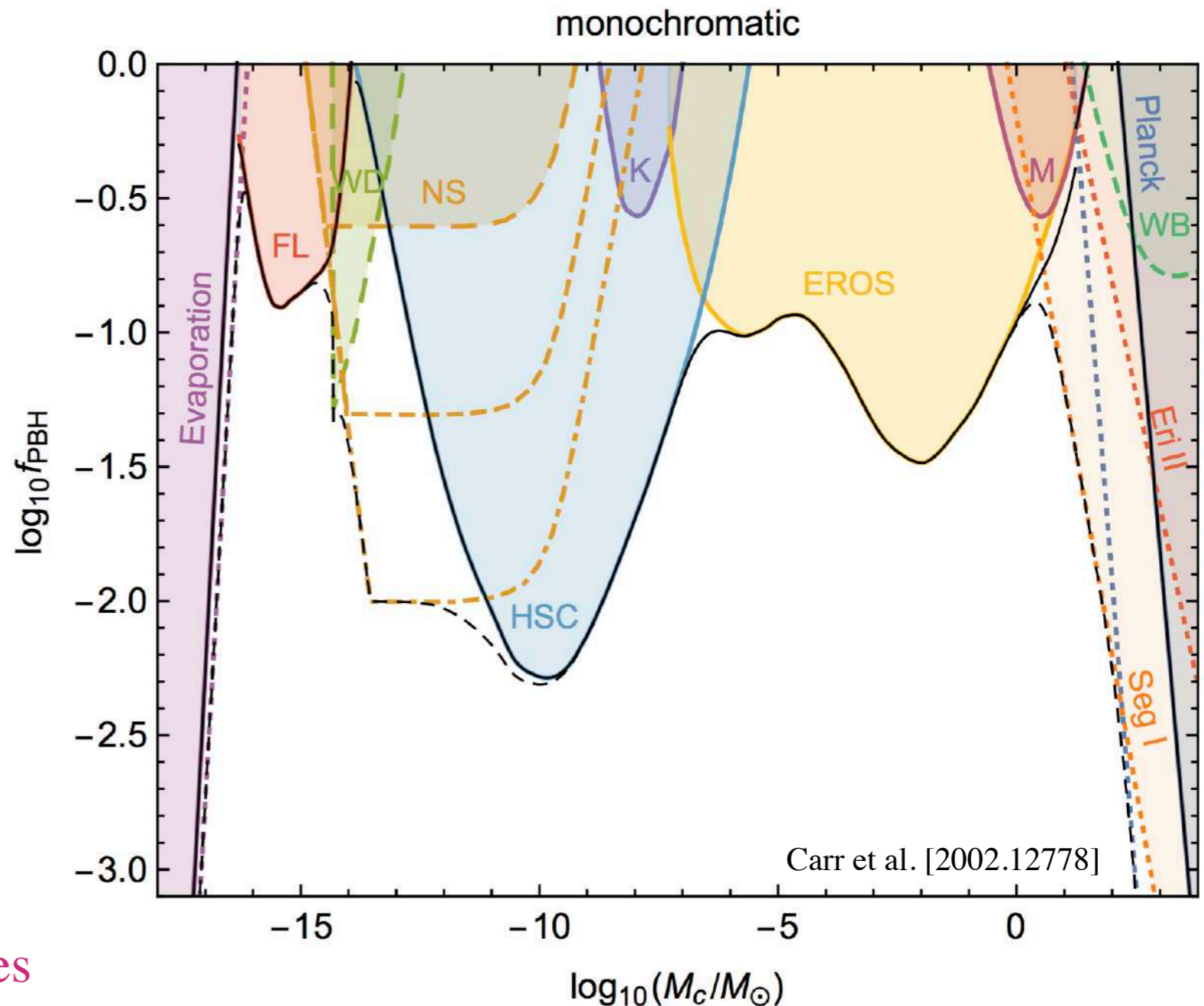
A prime candidate for an “exotic” astrophysical mass object are **Primordial Black Holes** (PBH).

Astrophysical black holes form from **stellar collapse** implying

$$M_{\text{BH}} \sim M_{\odot} \sim 10^{30} \text{ kg}$$

PBHs form from **primordial overdensities** in the Early Universe.

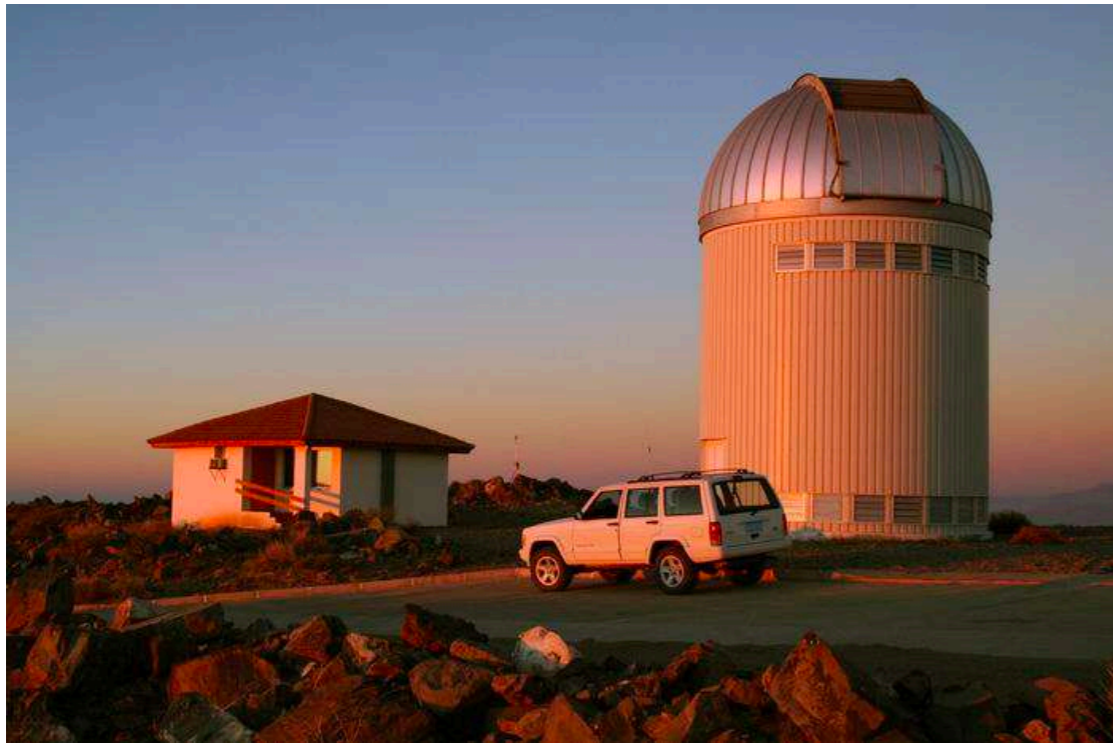
PBH can have a **large range of masses** depending on model of cosmology.



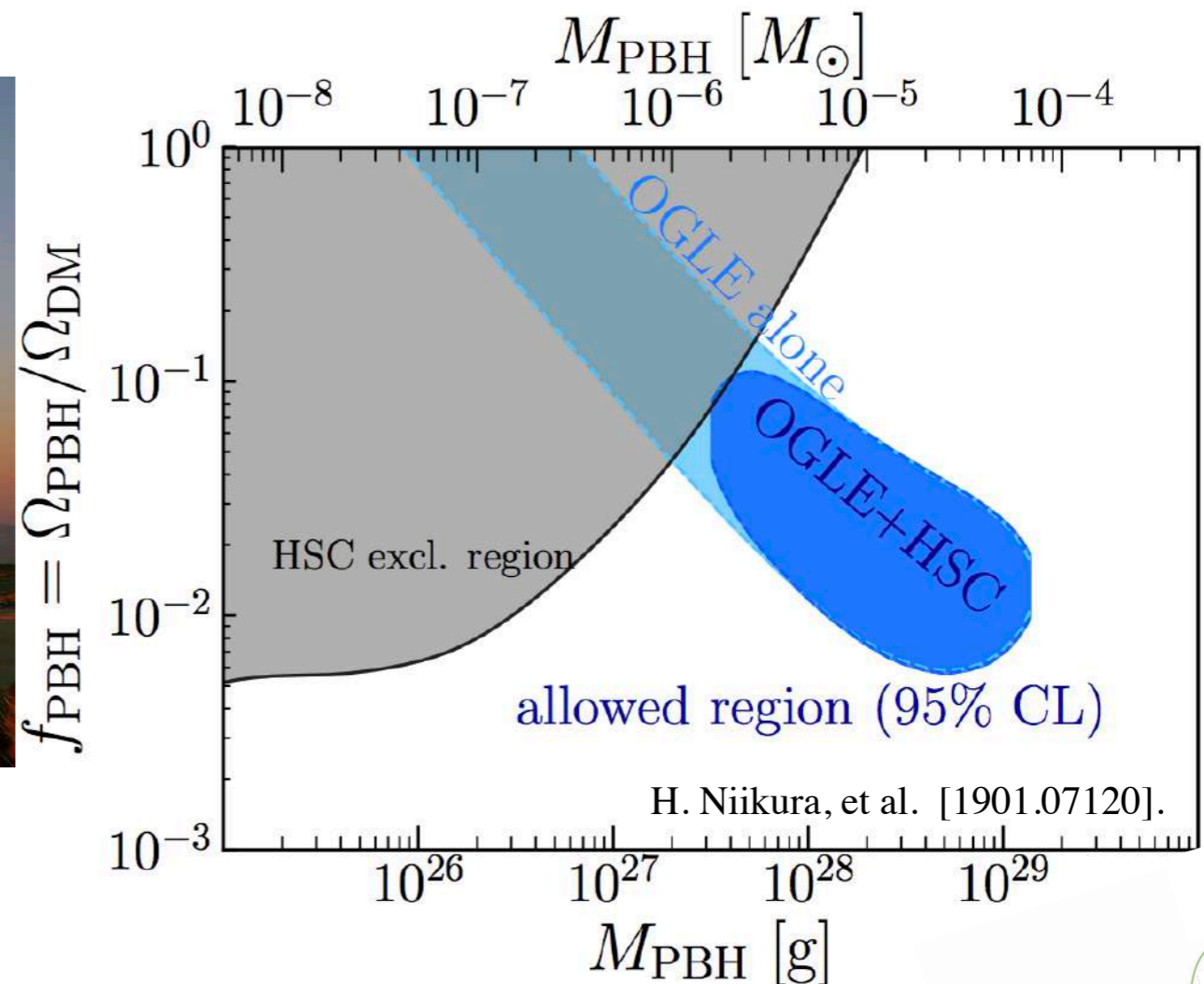
# The OGLE Excess

Notably, another tentative experimental **excess in unexplained microlensing events** seen by the OGLE telescope consistent with the Planet 9 mass range.

Indicative of **PBH population** with  $M \in [0.5M_{\oplus}, 20M_{\oplus}]$  ;  $f_{\text{PBH}} \in [0.005, 0.1]$



Optical Gravitational Lensing Experiment



# Catching a PBH

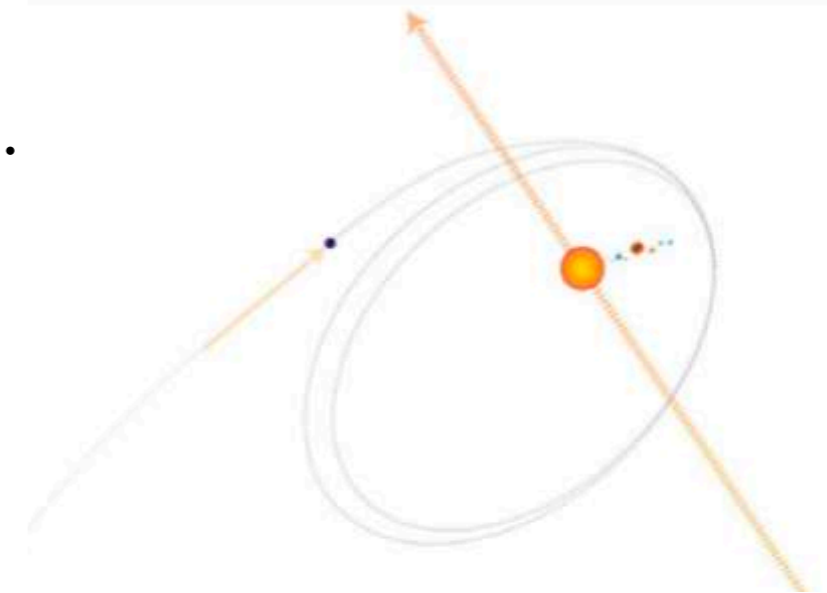
Find **probability** of Solar System catching a PBH vs planet.

Gravitational **capture rate** of an object is given by

$$\Gamma = \int n_0 F(v + v_{\odot,r}) \frac{d\sigma}{dv} v dv$$

where  $F(\cdot)$  and  $n_0$  are velocity distribution and density of the objects to be captured and  $v_{\odot,r}$  is the velocity of the Sun with respect to the rest frame of the objects.

Gouliniski and Ribak [1705.10332].

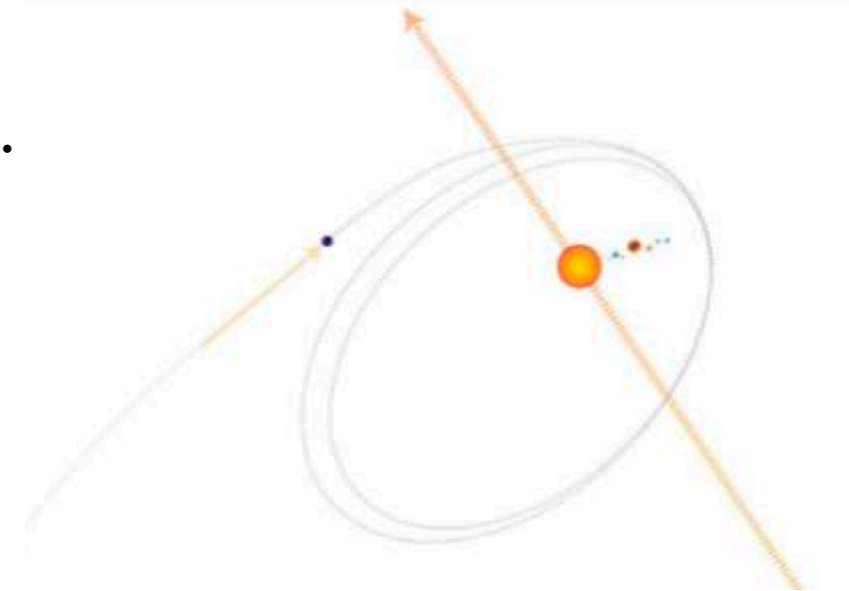


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Note, velocity dispersions are well approximated by the zero-order value  $F(v_{\odot})$ .

Then to test PBH hypothesis vs captured free floating planet (FFP), we consider **ratio of capture rates**. Common factors drop out, yielding:

$$\frac{\Gamma_{\text{BH}}}{\Gamma_{\text{FFP}}} \simeq \frac{n_{\text{BH}} F_{\text{PBH}}(v_{\odot,\text{PBH}})}{n_{\text{FFP}} F_{\text{FFP}}(v_{\odot,\text{FFP}})} \sim 1 \times \left( \frac{0.2 \text{pc}^{-3}}{n_{\text{FFP}}} \right) \left( \frac{40 \text{km/s}}{\sigma_{\text{FFP}}} \right)^3 \left( \frac{f_{\text{BH}}}{0.05} \right) \left( \frac{5 M_{\oplus}}{M_{\text{BH}}} \right).$$



# III. Dark Matter around PBHs





# Dark Matter Microhalo

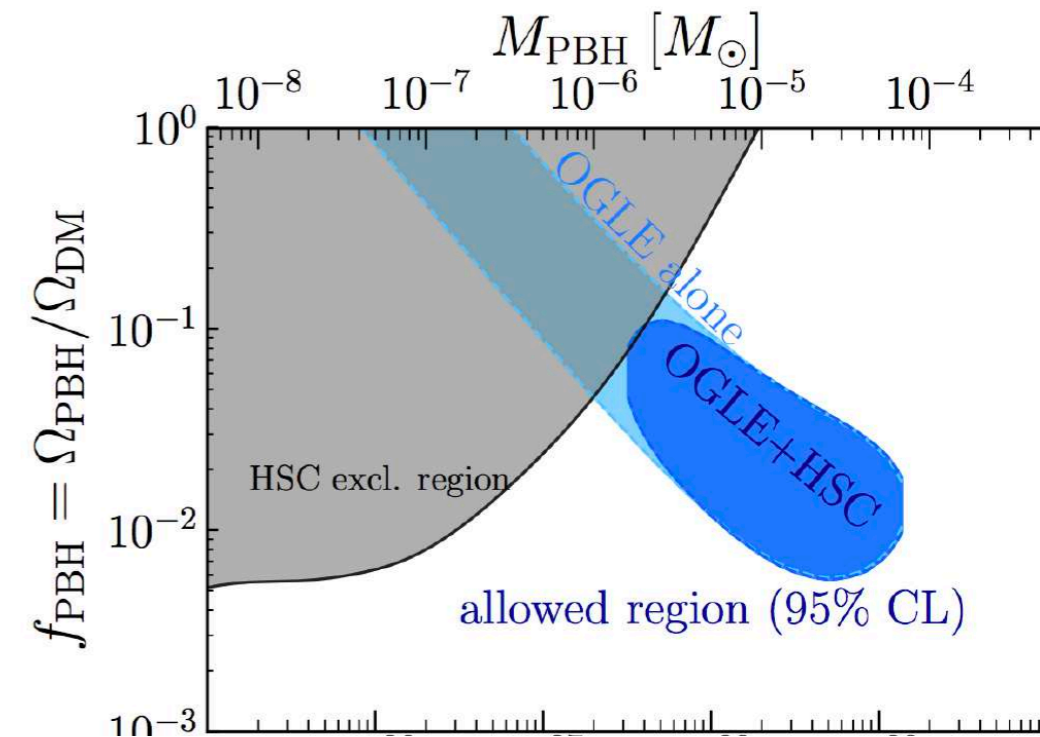
For  $f_{\text{PBH}} \in [0.005, 0.1]$  implies also particle dark matter.

Generically this leads to **dark matter halos around the PBH**.

The **total mass** of the halo satisfies

$$M_{\text{BH}} = \frac{4\pi}{3} \rho(t) r_{\text{in}}^3(t)$$

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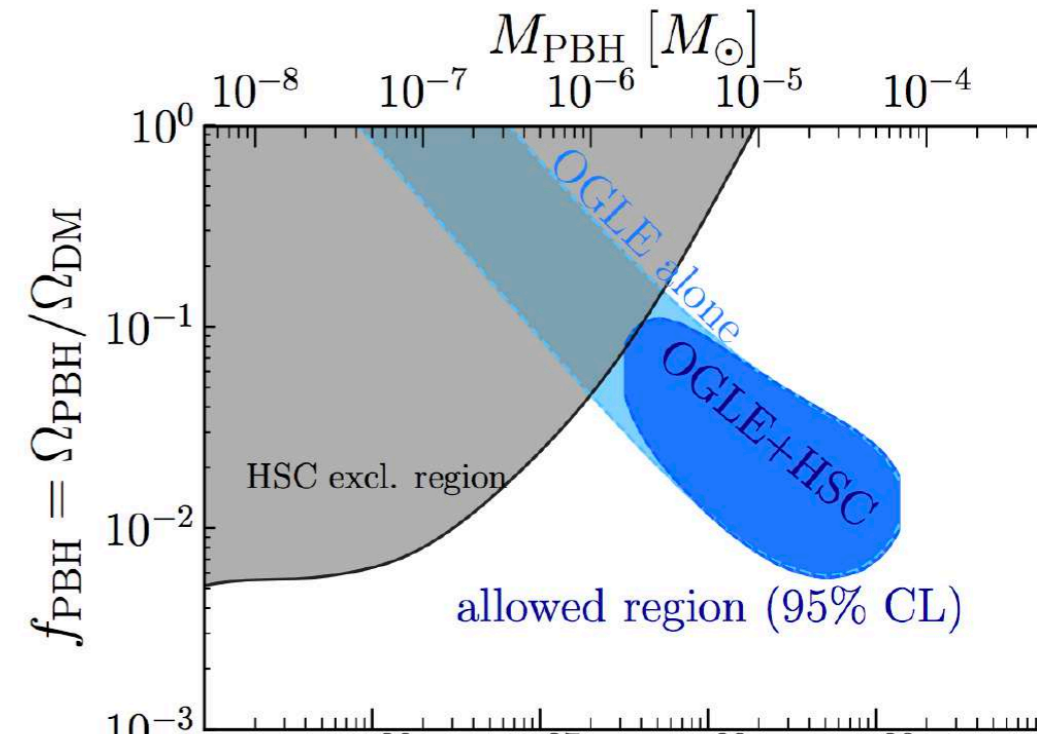
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Defining  $r_{\text{eq}} \equiv r_{\text{in}}(t_{\text{eq}}) \sim 220 \text{ AU} \times (M_{\text{BH}}/5M_{\oplus})^{1/3}$

evaluated at matter-radiation equality and for which  $\rho_{\text{eq}} \equiv \rho(t_{\text{eq}}) \simeq 2.1 \times 10^{-19} \text{ g/cm}^3$

With **density profile** (nb. requires some care)  $\rho(r) = \frac{\rho_{\text{eq}}}{2} \left( \frac{r_{\text{eq}}}{r} \right)^{9/4}$



# Tidal Stripping

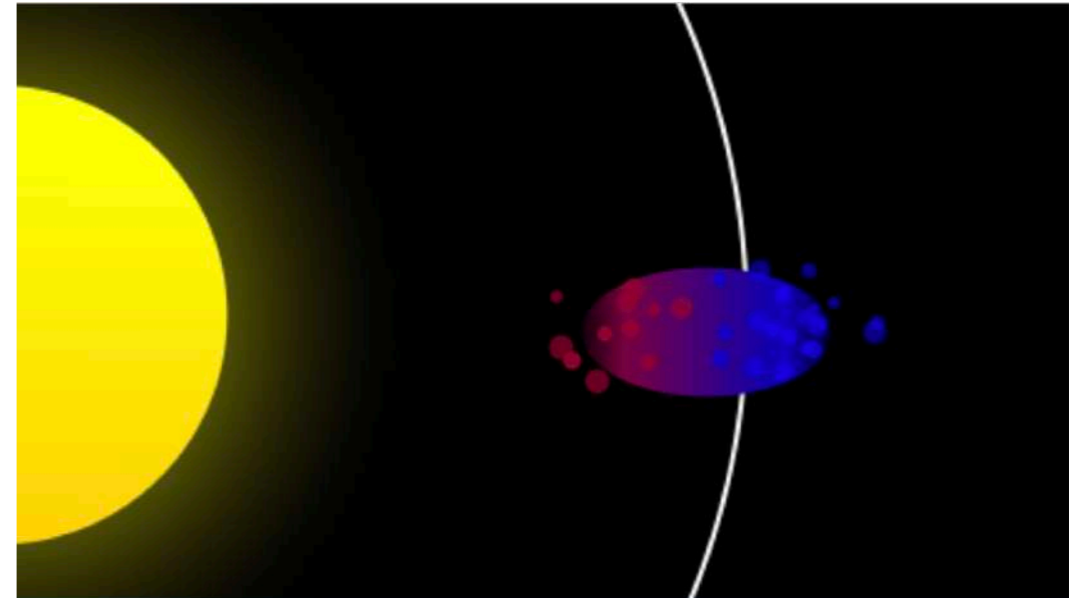
Profile terminates at certain radius.

Following formation the PBH halo can be subsequently **stripped by encounters** with other bodies.

Tidal stripping radius given by the **Roche limit**:

$$r_{t,*} \sim r_* \left( \frac{M_{\text{initial}}}{2M_{\odot}} \right)^{\frac{1}{3}}$$

where  $r_*$  is distance between two bodies and  $M_{\text{initial}}$  refers to the body being stripped.



# Tidal Stripping

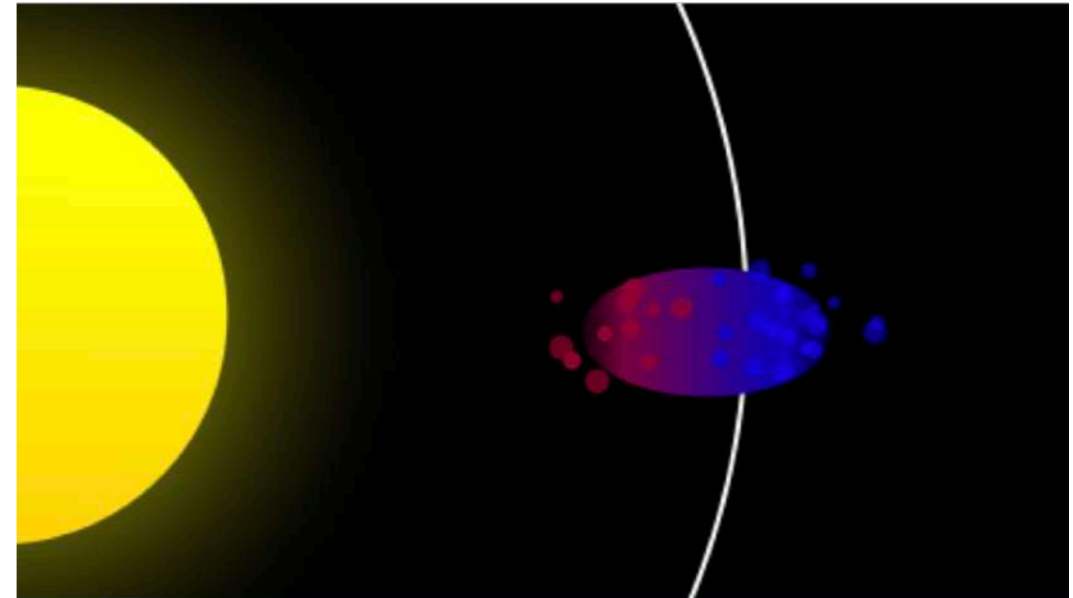
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Thus once the PBH settles into an **orbit around the Sun**, tidal radius cuts off the PBH halo at

$$r_{t,\odot} \sim r_p \left( \frac{M_{\text{BH}}}{2M_{\odot}} \right)^{\frac{1}{3}} \sim 8\text{AU} \left( \frac{r_p}{400\text{AU}} \right) \left( \frac{M_{\text{BH}}}{5M_{\oplus}} \right)^{\frac{1}{3}}$$

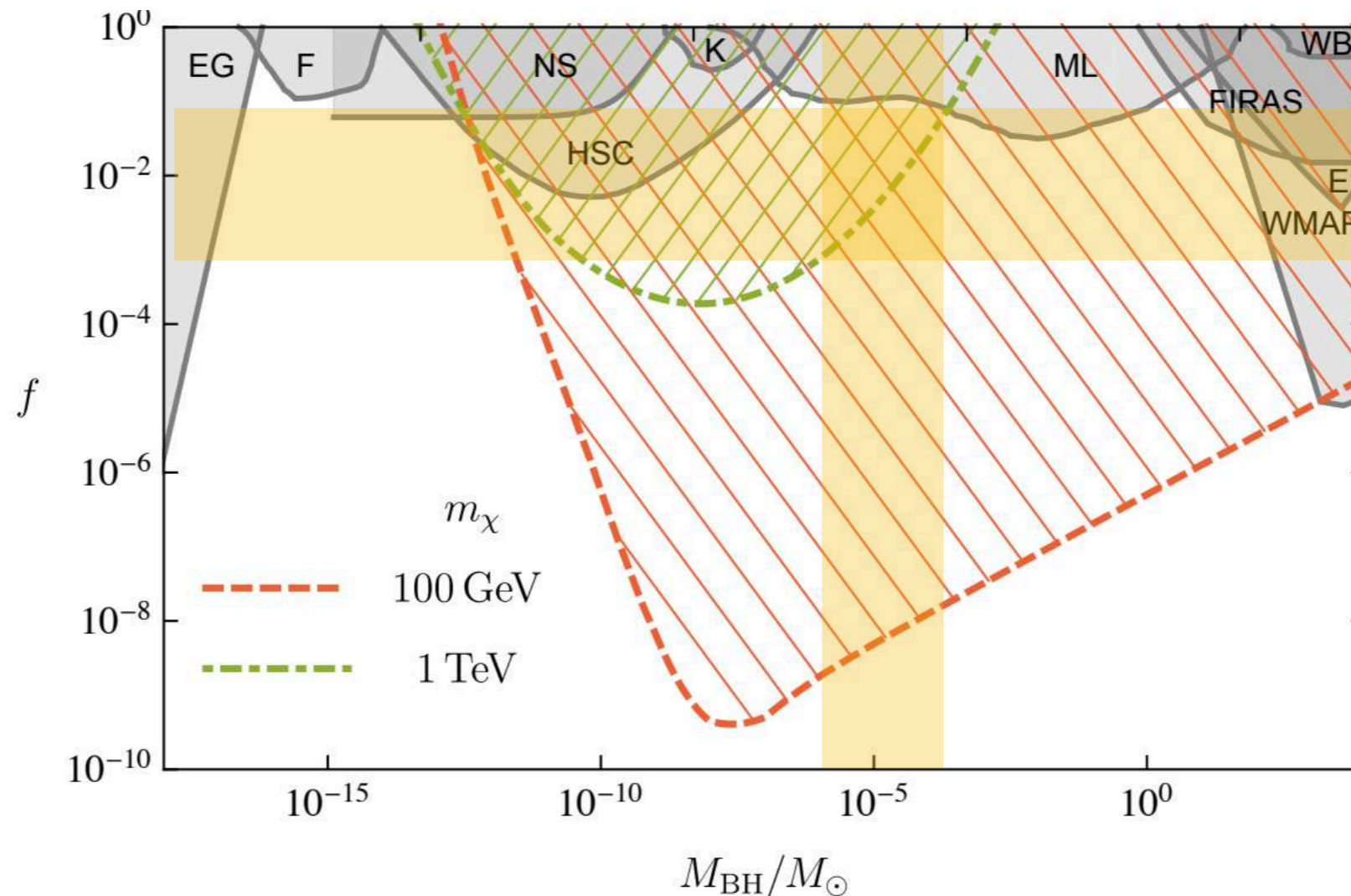
Note that 8 AU is  $10^9$  km, compare this to Earth mass PBH with diameter 10cm!



# Mostly WIMP Scenario

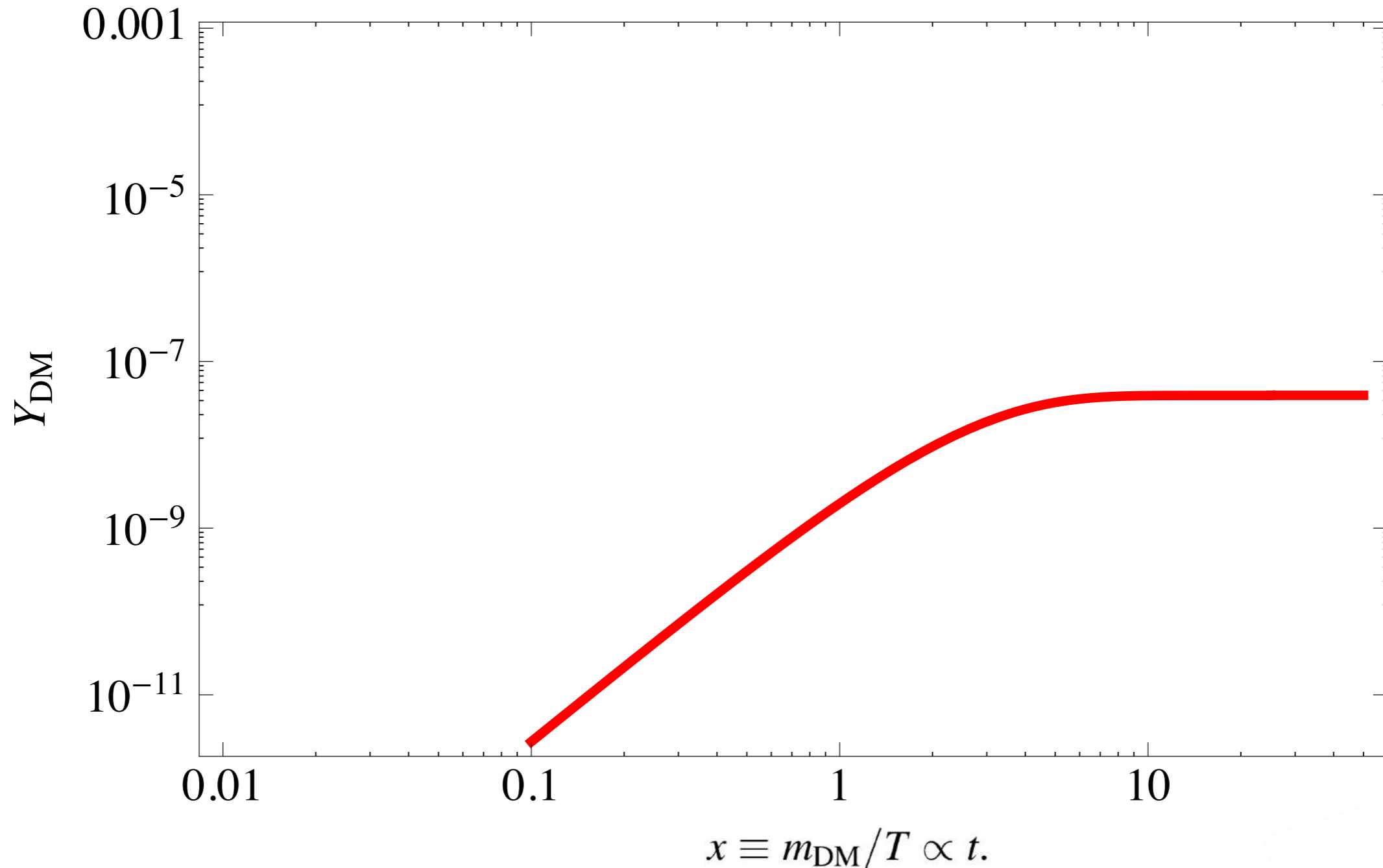
Consider the OGLE PBG population  $M \in [0.5M_{\oplus}, 20M_{\oplus}]$ ;  $f_{\text{PBH}} \in [0.005, 0.1]$

For a WIMP DM cross section  $\langle\sigma v\rangle_0 \sim 3 \times 10^{-26} \text{cm}^3/\text{s}$  this is **VERY excluded**.



# Freeze-in Dark Matter

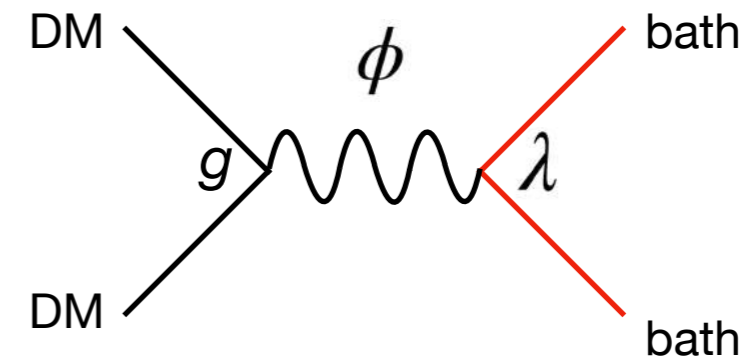
An alternative to WIMPs which have much smaller annihilation is **Freeze-in**.



# Characteristic cross section

In this scenario the **relic density** of dark matter scales as follows

$$\Omega_{\text{DM}} \propto m Y_{\text{FI}} \propto \lambda^2$$



Parametrically

$$\Omega_{\text{DM}} \simeq 0.2 \left( \frac{m}{100 \text{ GeV}} \right) \left( \frac{\lambda}{6 \times 10^{-12}} \right)^2 \left( \frac{10 \text{ TeV}}{M_\phi} \right)$$

With these **benchmark** values it implies an **annihilation cross section**

$$\langle \sigma v \rangle_{\text{ch}} \simeq 1.3 \times 10^{-56} \text{ cm}^3 / \text{s} \times \left( \frac{g}{10^{-2}} \right)^2.$$

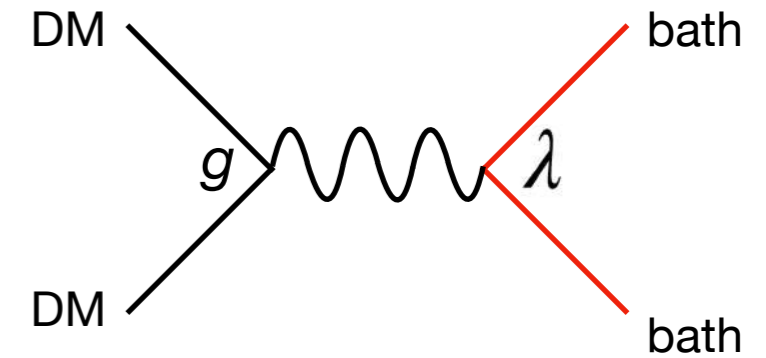
The coupling  $g$  is largely unfixed.



# Annihilation Rate

The dark matter **annihilation rate** is given by

$$\Gamma = 4\pi \int r^2 dr \left( \frac{\rho(r)}{m} \right)^2 \langle \sigma v \rangle$$



Using the **density profile** from earlier:  $\rho(r) = \frac{\rho_{\text{eq}}}{2} \left( \frac{r_{\text{eq}}}{r} \right)^{9/4}$

and the characteristic cross section:  $\langle \sigma v \rangle_{\text{ch}} \simeq 1.3 \times 10^{-56} \text{cm}^3/\text{s} \times \left( \frac{g}{10^{-2}} \right)^2$

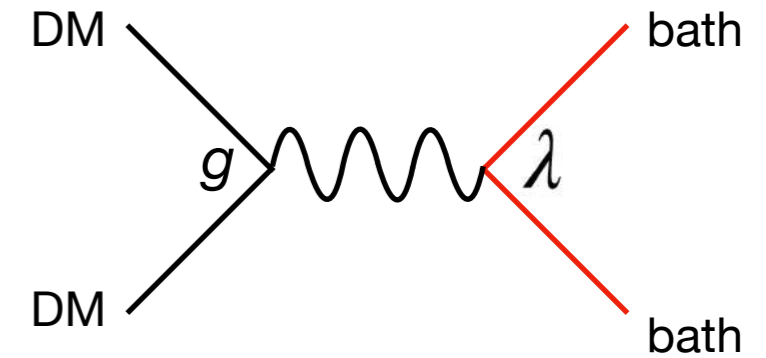




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Putting this together, the **annihilation rate for Freeze-in dark matter** is

$$\Gamma = \sqrt{\frac{3\rho_{\text{eq}}}{8\pi G^3}} \frac{\langle \sigma v \rangle}{m^2} = 10^{20} \text{s}^{-1} \left( \frac{\langle \sigma v \rangle}{\langle \sigma v \rangle_{\text{ch}}} \right) \left( \frac{100 \text{GeV}}{m} \right)^2$$



# Limits from Flux

The **photon flux** from annihilation in a distribution a distance  $r_9$  from Earth:

$$\Phi_\gamma = \frac{\kappa_1 \Gamma}{4\pi r_9^2}$$

where  $\kappa_1$  is the average number of photons per annihilation; take  $\kappa_1 \sim 10$



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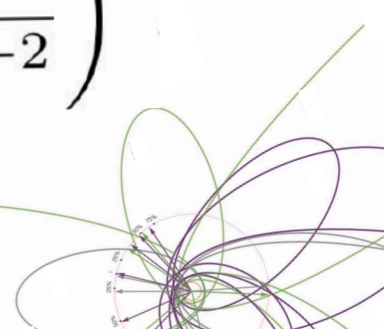
The **smallest detectable** in 8 year **FERMI-LAT catalog** has

$$\Phi_\gamma = 8.8 \times 10^{-12} \text{photons/cm}^2/\text{s}$$

Since  $\Gamma$  **depends on the annihilation cross section**, this implies a limit:

$$\langle \sigma v \rangle < 5.1 \times 10^{-56} \text{cm}^3/\text{s} \left( \frac{m}{100 \text{GeV}} \right)^2$$

And is satisfied **freeze-in** model:  $\langle \sigma v \rangle_{\text{ch}} \simeq 1.3 \times 10^{-56} \text{cm}^3/\text{s} \times \left( \frac{g}{10^{-2}} \right)^2$



# Conclusions

There is **tentative evidence** from observations of TNO orbits for a **9th Planet**.

OGLE has **unexpected microlensing events** indicative of new compact bodies.

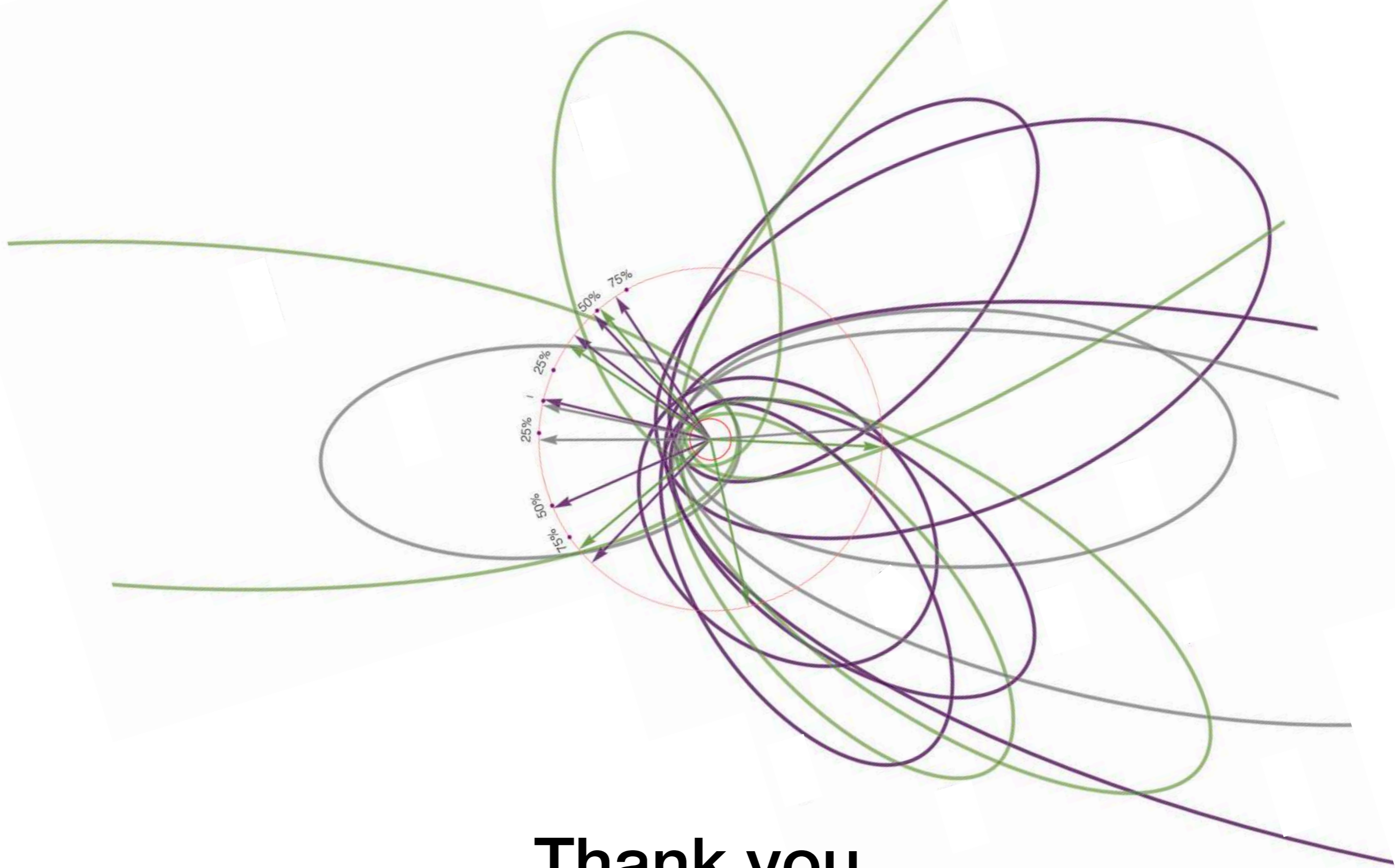
Remarkably these two excesses hint at the **same mass range**: around  $5 M_{\oplus}$

Interpreting the OGLE excess as PBH, the **capture probability similar** to a planet

Looking for a **PBH requires distinct searches** compared to looking for a planet

For some interesting directions see: Witten: 2004.14192  
Siraj & Loeb: 2005.12280  
Henghes et al [DES]: 2009.12856





**Thank you**

arXiv:1909.11090