Exercises for lectures on BSM physics by Csaba Csaki Days 1-2

1. Calculate the leading shift (the quadratically divergent part) in the Higgs mass parameter in the standard model and verify the expression presented in lecture.

2. Show that the masses of all particles within a supermultiplet are equal.

3. Show that the vacuum energy in SUSY theories is positive definite.

4. Show that the effect of a SUSY transformation $e^{i\xi Q + \bar{Q}\bar{\xi}}$ has the effect

$$(x^{\mu}, \theta, \bar{\theta}) \rightarrow (x^{\mu} + i\theta\sigma^{\mu}\bar{\xi} - i\xi\sigma^{\mu}\bar{\theta}, \theta + \xi, \bar{\theta} + \bar{\xi})$$
.

- 5. Show that $\overline{D}y = 0$.
- 6. Show that the effect of SUSY transformations on a chiral superfield is

$$\delta\varphi = \sqrt{2}\epsilon\psi, \ \delta\psi = \sqrt{2}i\sigma^{\mu}\bar{\epsilon}\partial_{\mu}\varphi + \sqrt{2}\epsilon F, \ \delta F = \sqrt{2}i\bar{\epsilon}\bar{\sigma}^{\mu}\partial_{\mu}\psi.$$

7. Calculate $\int d^4\theta \Phi^{\dagger} \Phi$.