

**Testing quantum mechanics and
gravity by using levitated
mechanics**

Hendrik Ulbricht

University of Southampton

Thanks to ...

www.quantumnano.org

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Experiments, applications & space: Peter Barker, Tjerk Oosterkamp, Andrea Vinante, Alessio Belenchia, Jize Yan, Maria Chiara Braidotti, Daniele Faccio.

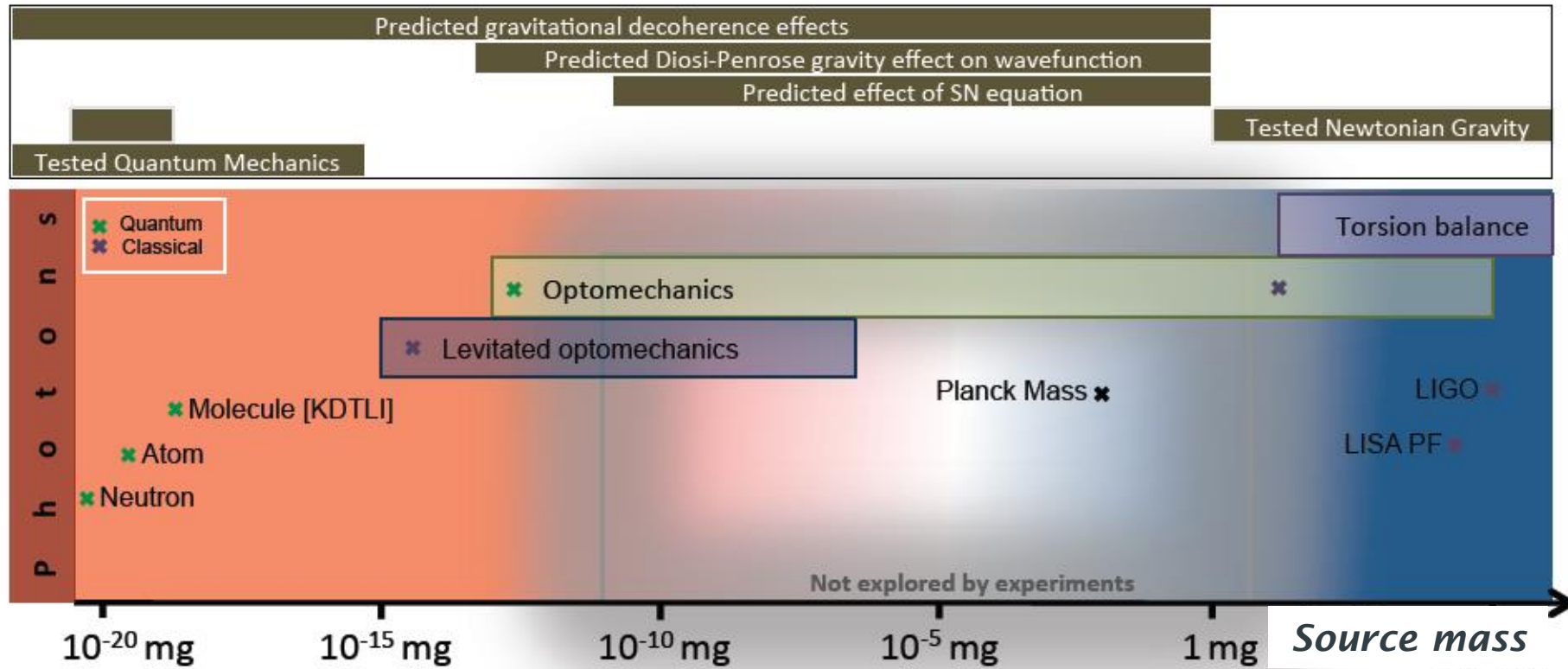
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Main menu

- Testing macroscopic (large-mass) quantum.
- Testing small-mass gravity.
- Amplification of elm fields by mechanical rotation.

Test gravity & quantum interplay in low energy regime

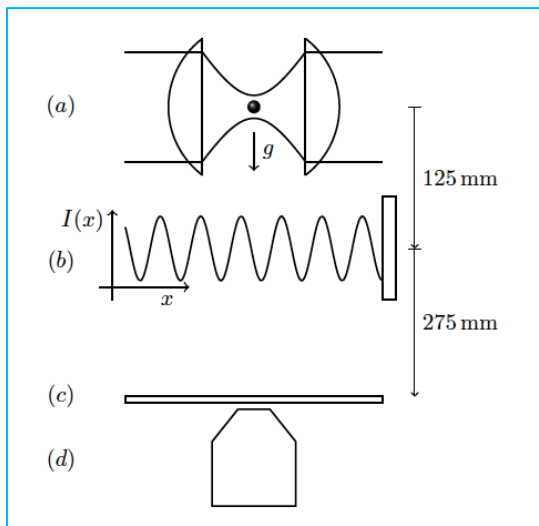


Smallest source mass where Newtonian gravity is confirmed by experiment: ~100 mg
What if the source mass is even smaller and in a spatial superposition?
How does the gravitational field look like then?

EXERIMENTS: LEVITATED MECHANICAL SYSTEMS

Nanoparticle Talbot interferometer (NaTali):

directly testing macroscopic quantum superpositions



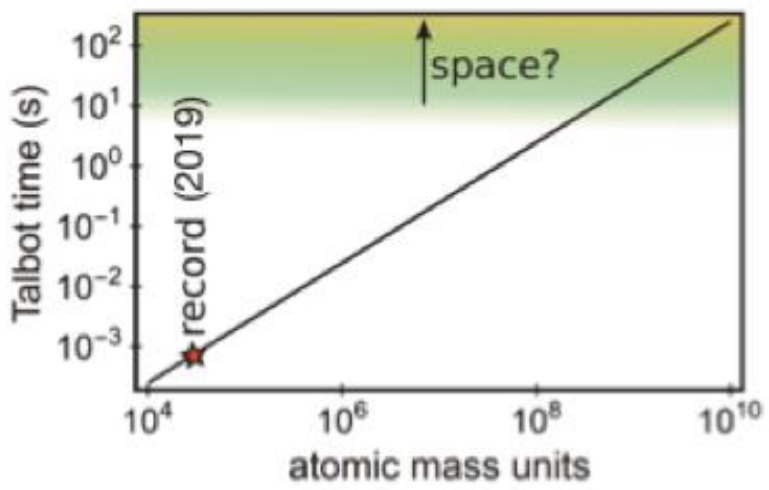
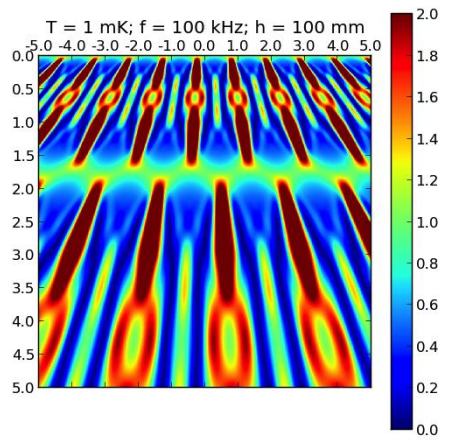
Step 1 - simulation: Spatial superposition of particle of mass: $10^6 - 10^7$ amu (20 nm in diameter)

- Wigner function model to calculate quantum carpet.
-> Thermal and collisional decoherence are negligible.



Step 2 - Experiment: Particle source has been realized by particle levitation & cooling, grating implementation ongoing

Quantum carpet:
Simulated interference pattern



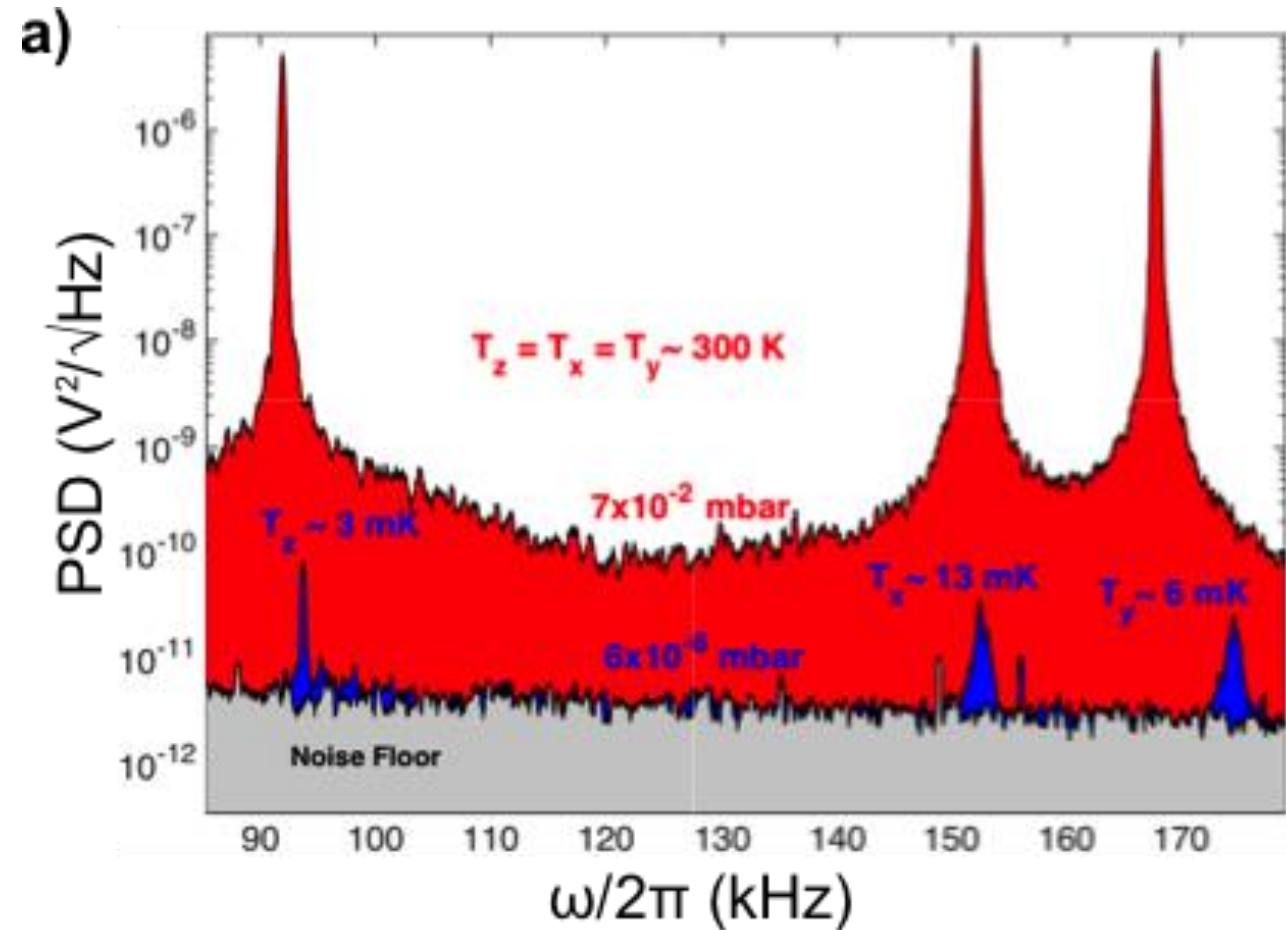
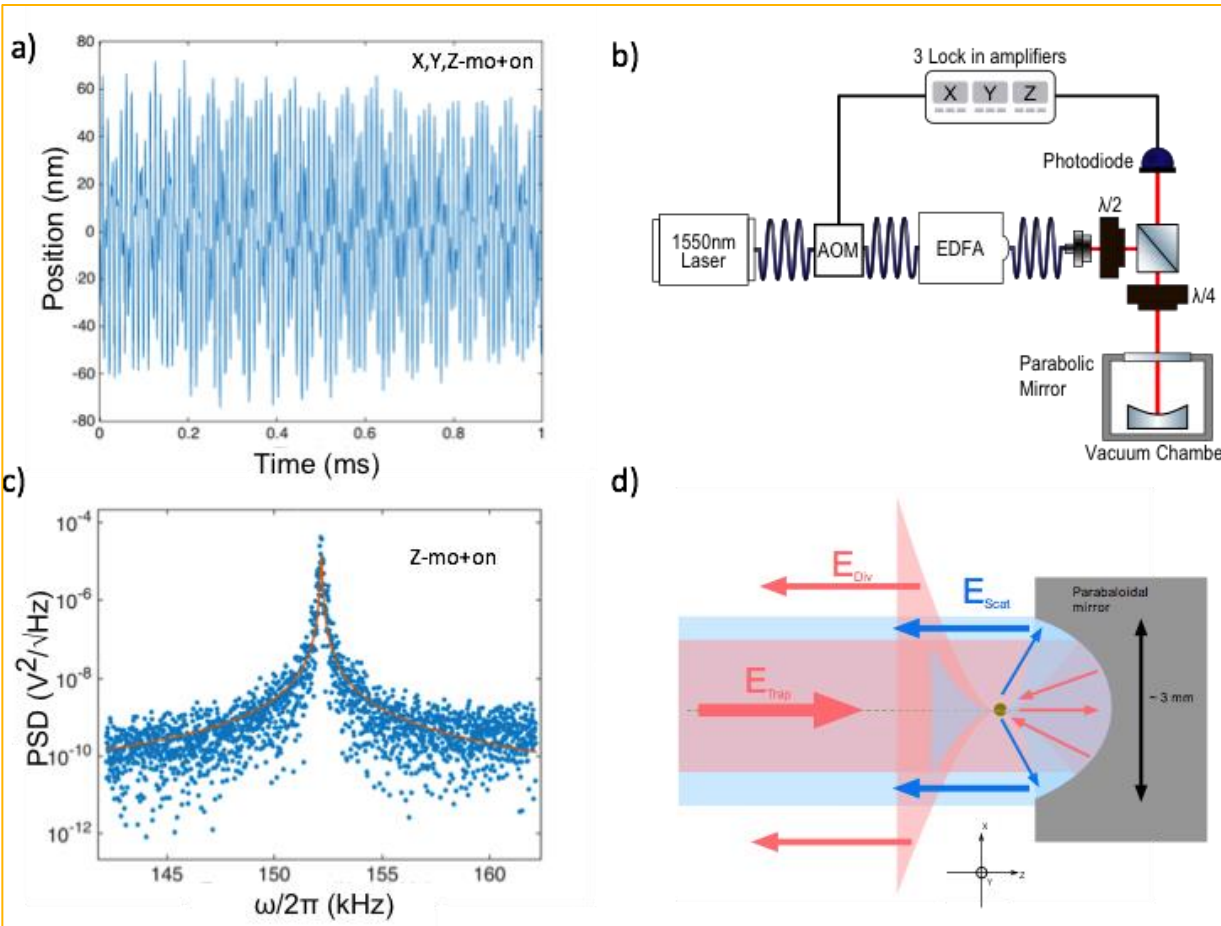
Bateman, J., S. Nimmrichter, K. Hornberger, and H. Ulbricht
Near-field interferometry of a free-falling nanoparticle from a point-like source
Nature Communications 4, 4788 (2014).

Belenchia, A., Carlesso, M., Donadi, S., Gasbarri, G., Ulbricht, H., Bassi, A. and Paternostro, M., 2021.
Test quantum mechanics in space. *Nature*, 596(7870), pp.32-34.

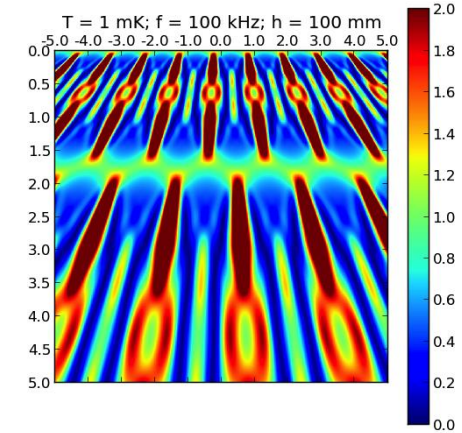
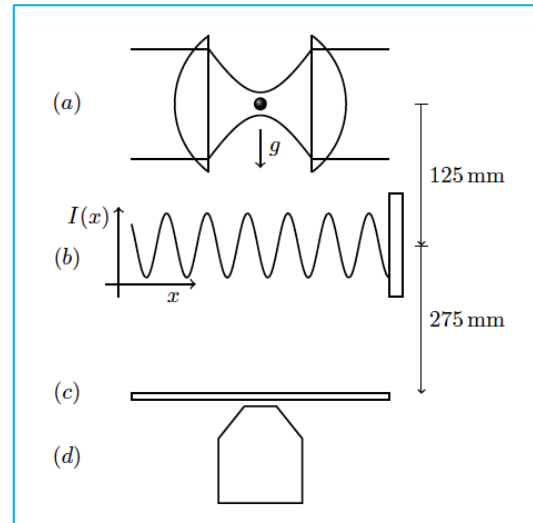
Trap and measure position, then feedback cool to ~1mK

Equation of motion: $\ddot{x}(t) + \Gamma_0 \dot{x}(t) + \omega_0^2 x(t) = \frac{1}{m} [F_{\text{fluct}}(t) + F_{\text{feed}}(t)]$

Power spectral density: $S_x(\omega) = \frac{k_B T_0}{\pi m} \frac{\Gamma_0}{([\omega_0 + \delta\omega]^2 - \omega^2)^2 + \omega^2 [\Gamma_0 + \delta\Gamma]^2}$



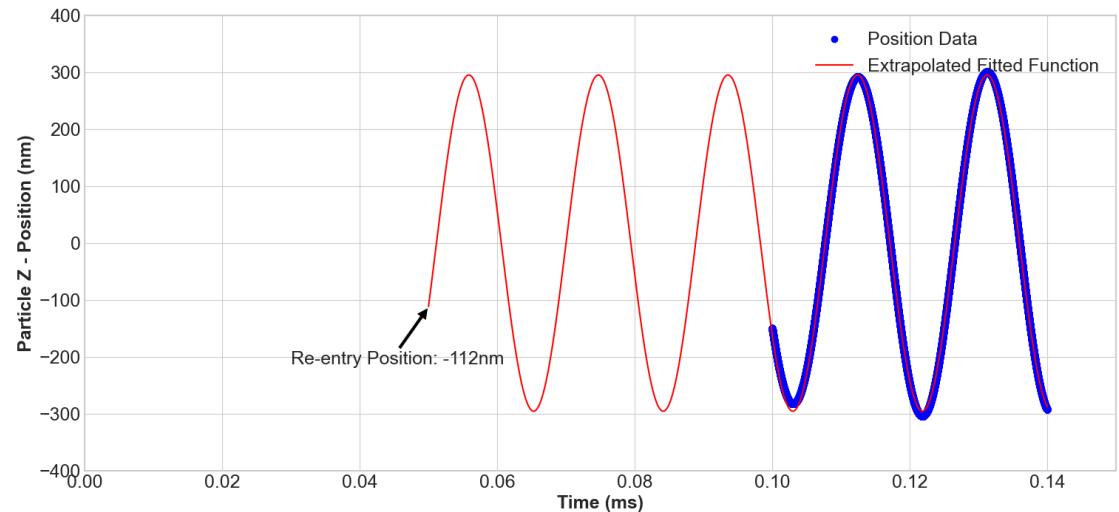
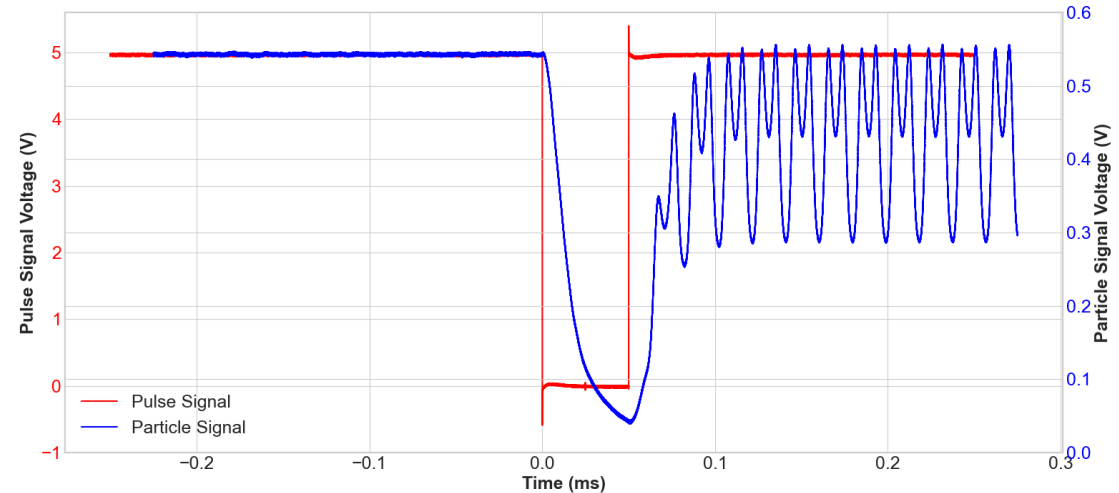
Quantum carpet: Simulated interference pattern



LONG FREE COHERENT EVOLUTION TIME

Freefall scheme: recapture in trap gives 500 microseconds

- Re-entry position can be detected by filtering and extrapolating particle signal close to re-entry.
- Data from turning trap off/on and detecting position as proof of concept.
- Needs proper tracking model and filtering (Jason Ralph)



More free evolution time by Throw and Catch:

up to 100 milliseconds

Wardak, J., Georgescu, T., Gasbarri, G., Belenchia, A. and Ulbricht, H., 2024. Nanoparticle Interferometer by Throw and Catch. *Atoms*, 12(2), p.7.

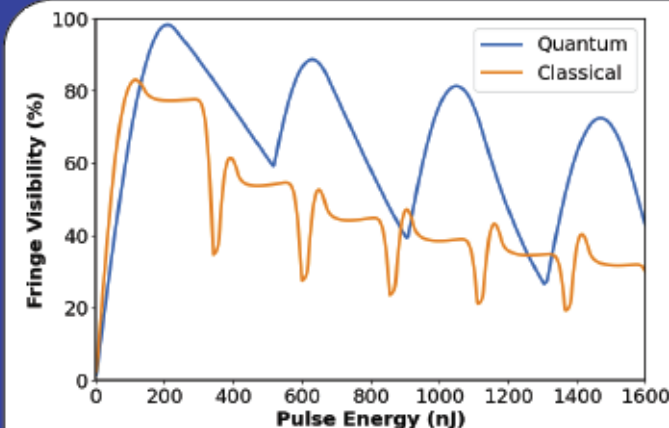
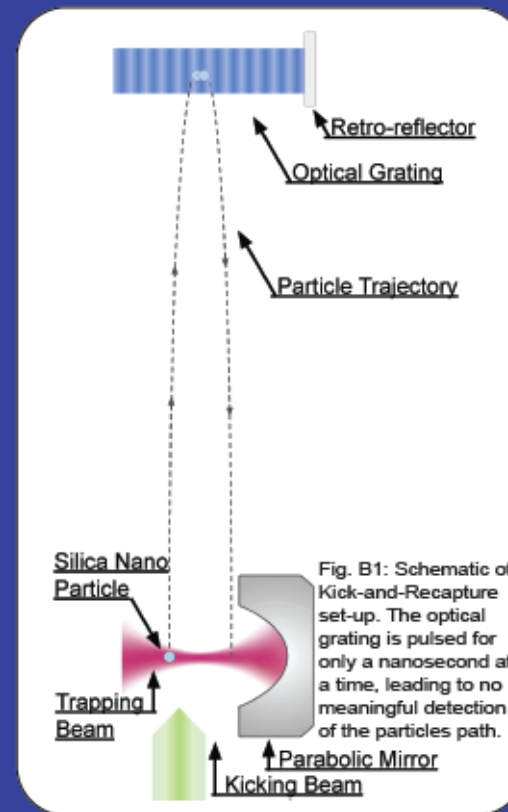


Fig. B2: Theoretical Quantum and Classical fringe visibility as function of optical grating intensity. A SiO₂ particle, $m = 10^6$ AMU, cooled down to 1 mK C.O.M. motion was assumed. $P = 10^{-10}$ mbar, $T_{\text{flight}} = 58$ ms or 1.6 cm flight height.

Large Scale Quantum

Molecules up to 10^5 AMU have been shown to still display quantum interference during free evolution. Launching SiO₂ nanospheres from an optical trap through an optical gratings we aim to demonstrate Talbot-Lau interference [2].

The 100 nm particles (10^{10} AMU) are cooled down to near the ground-state through parametric feedback cooling, after which they are kicked using a YAG laser.

Interference during free-fall is reconstructed after the particle travels through an optical UV grating and is recaptured into the trap. The recapture position is retraced, reconstructing the interference pattern of the same particle over many kick and recaptures.

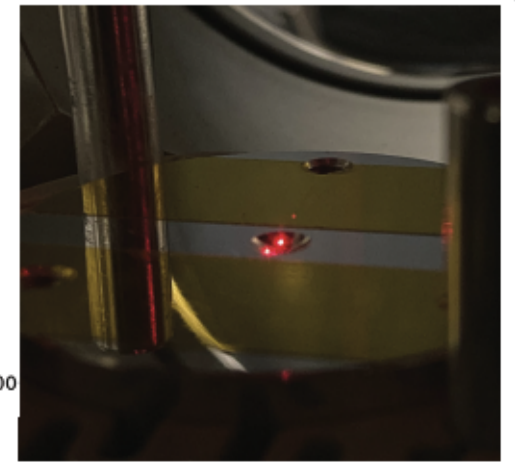
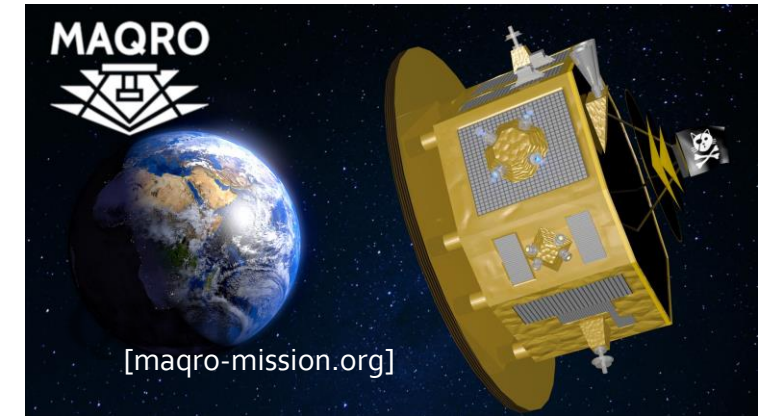


Fig. B3: Photo of a particle trapped above the parabolic mirror, illuminated by a red laser.

Satellite for long free evolution time: 100 secs (in free fall)

- **Main objective:** Generate macroscopic quantum superposition of a 100 nm+ particle.
- **Space advantage:** Long free-evolution time

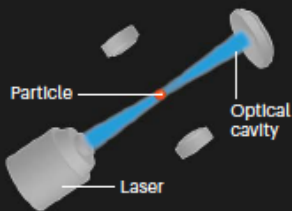


THREE STAGES IN SPACE

Researchers want to test ever-larger particles for quantum wave behaviour. Doing this in space removes experimental hurdles seen on Earth, such as gravity and noise, meaning larger particles can remain stable for longer as they develop their quantum behaviour. Conducting the tests involves three stages.

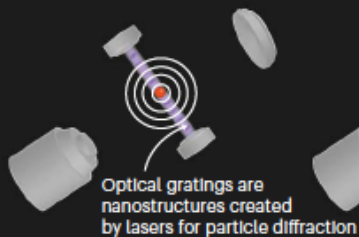
1. Prepare

Lasers cool a suitable particle in an optical cavity operating at low pressure.



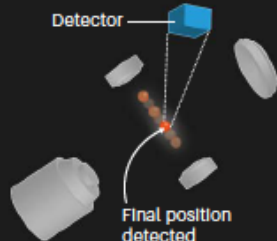
2. Wait

Waves develop and an optical grating is applied to create quantum superpositions. Particles then propagate freely.



3. Detect

Particles finally reach a suitable detection stage.



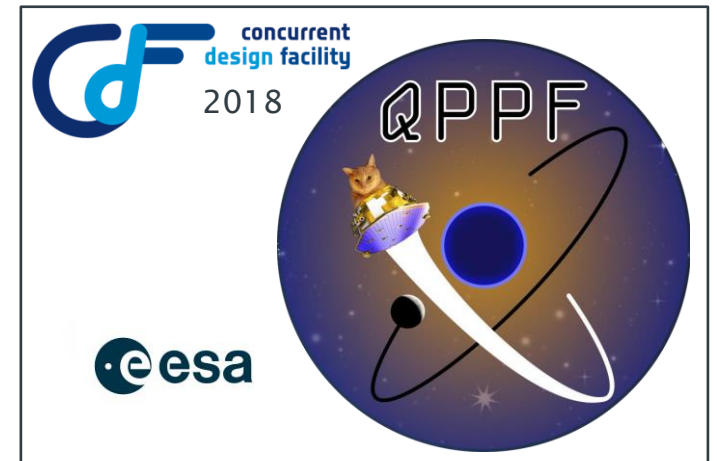
Theoretical foundations

Belenchia, A., et al., *Test quantum mechanics in space*, **Nature** 596, 32-34 (2021).

Belenchia, A., et al. *Quantum physics in space*, **Physics Reports** 951, 1-70 (2022).

Kaltenbaek, R., et al. *Research campaign: Macroscopic quantum resonators (MAQRO)*, **Quantum Science and Technology** 8, 014006 (2023).

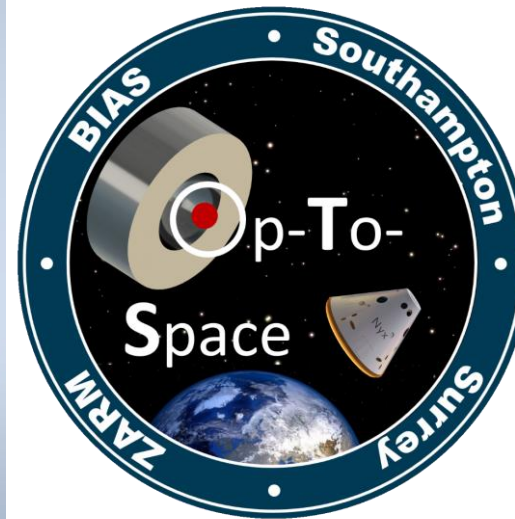
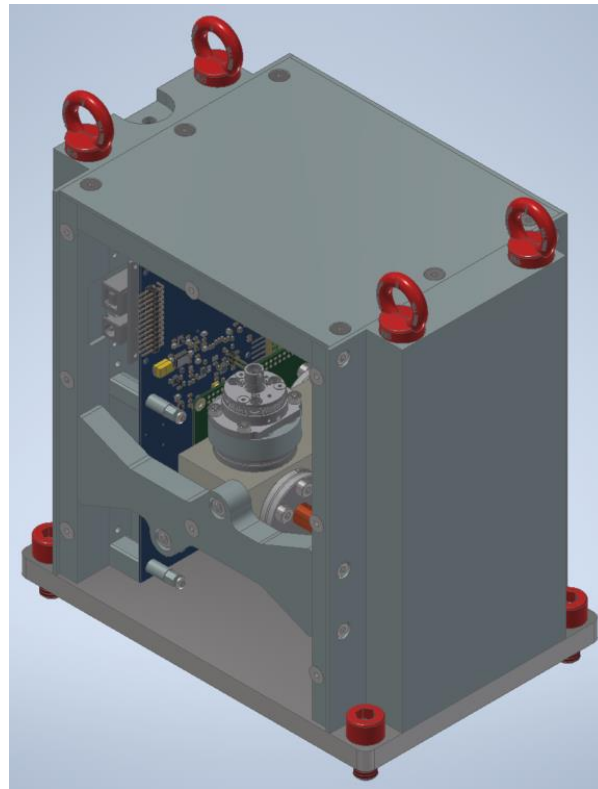
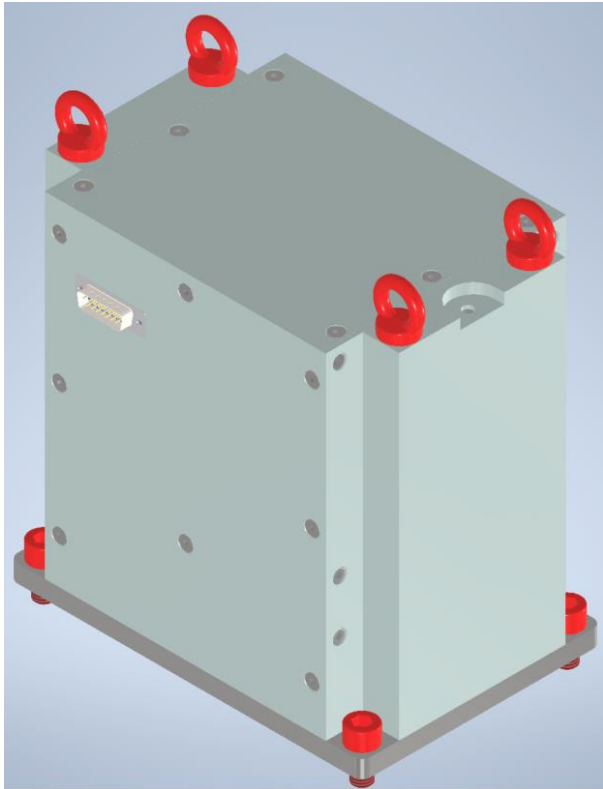
Gasbarri, G., et al. *Testing the foundation of quantum physics in space via Interferometric and non-interferometric experiments with mesoscopic nanoparticles*. **Communications Physics** 4, 155 (2021).



Levitated mechanics in free fall – satellite launch June 2025

Payload box:

- Size: 200 x 200 x 140 mm
- Weight: 10 kg
- 10 W power consumption (average)
- 1 optical trap, 1 diamagnetic trap, autonomous operation by FPGA and microcontroller.
- Tested for space: shock & vibration, thermal, EMC (next week).



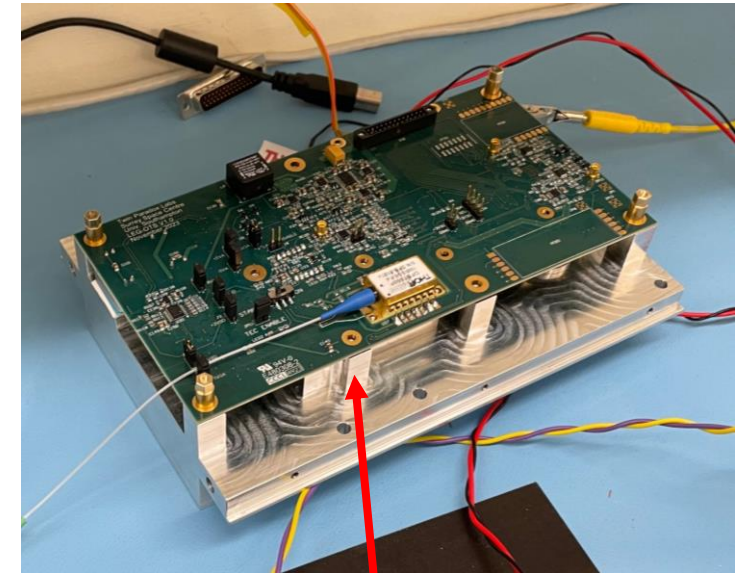
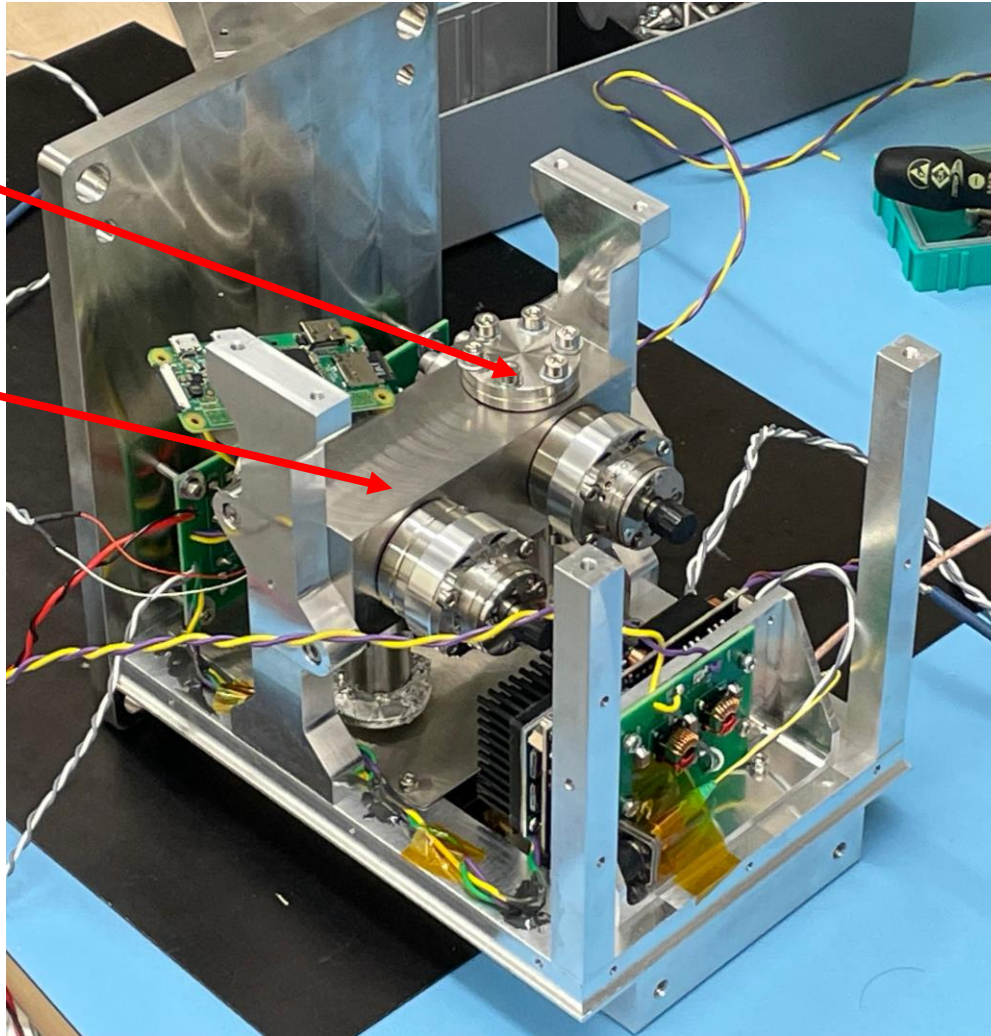
What is inside the box?

Optical trap for silica particles

Diamagnetic trap for graphite

Piezo-based particle loading system

Optical fiber system for detection, UHV chambers (passively NEG pumped, $1 \text{ e-}9 \text{ mbar}$)



PCB with laser PID controller
FPGA for electronics
Microcontroller to operate Experiments and DAQ.

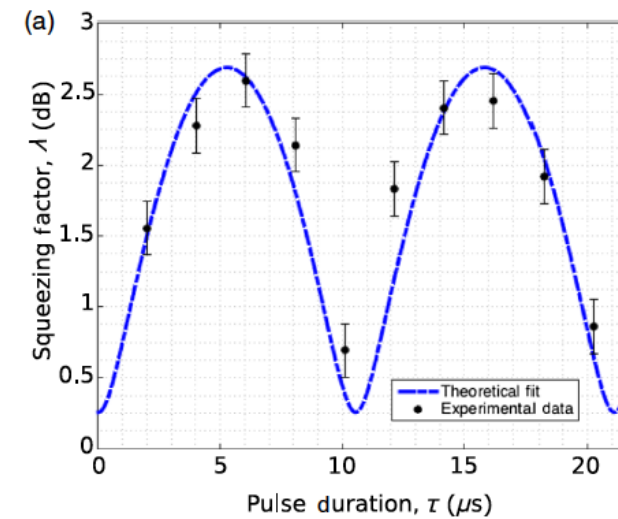
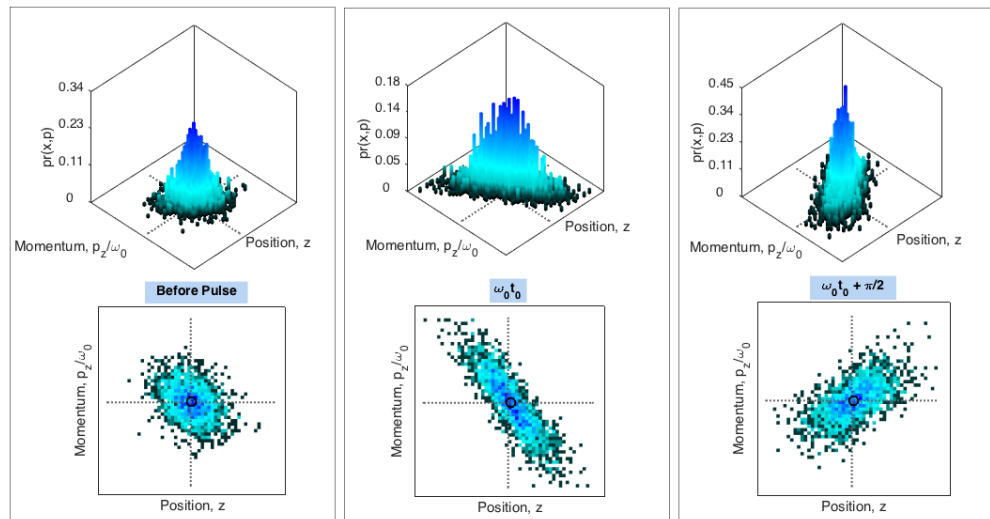
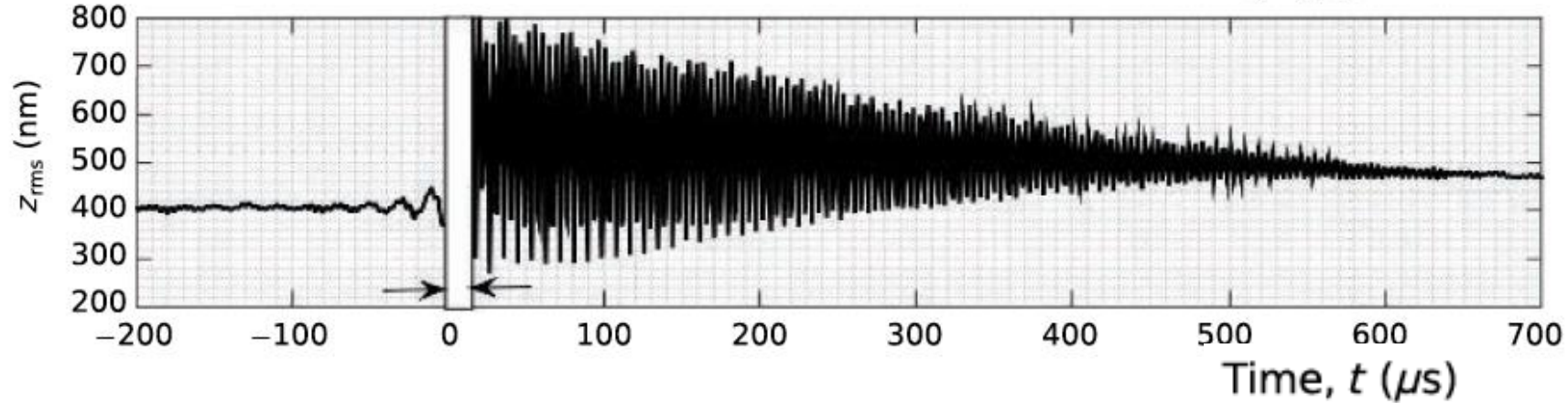
Fully autonomous operation

OR

**ACCELERATE EVOLUTION OF
QUANTUM STATE COHERENTLY**

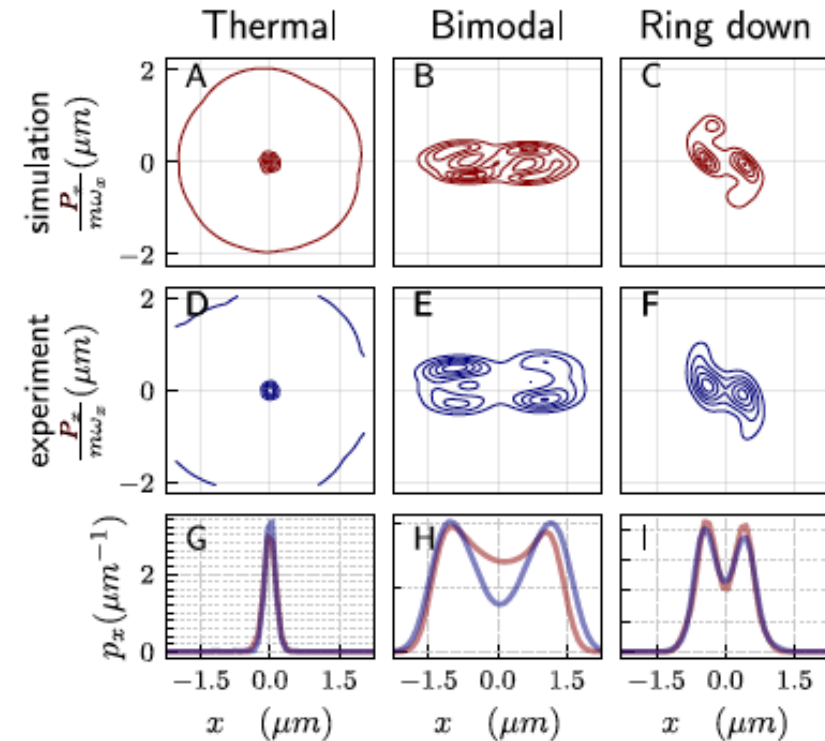
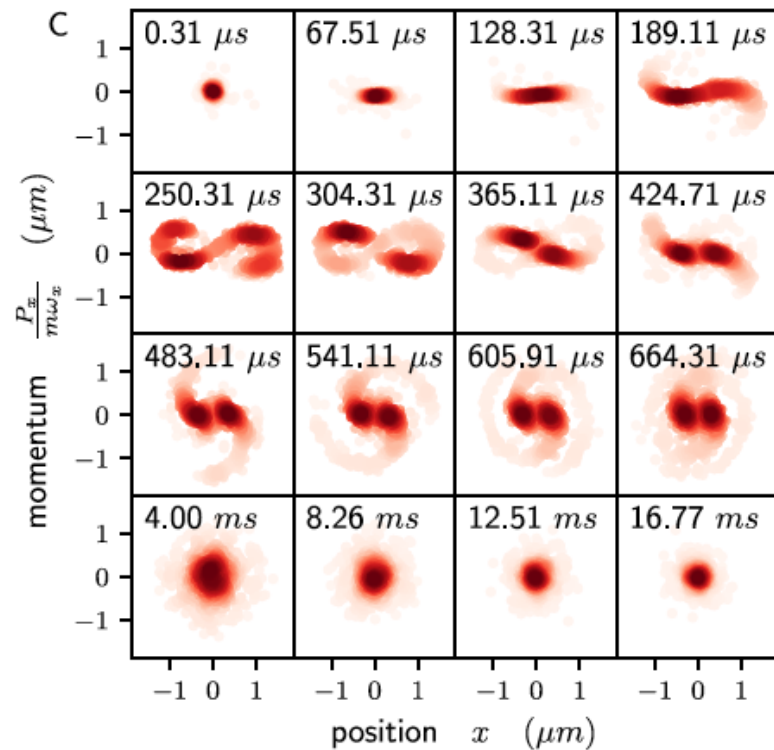
Squeezing the thermal motion by frequency jump

Time trace:



Rashid, M., T. Tufarelli, J. Bateman, J. Vovrosh, D. Hempston, M. S. Kim, and H. Ulbricht, *Experimental Realization of a Thermal Squeezed State of Levitated Optomechanics*, PRL 117, 273601 (2016).

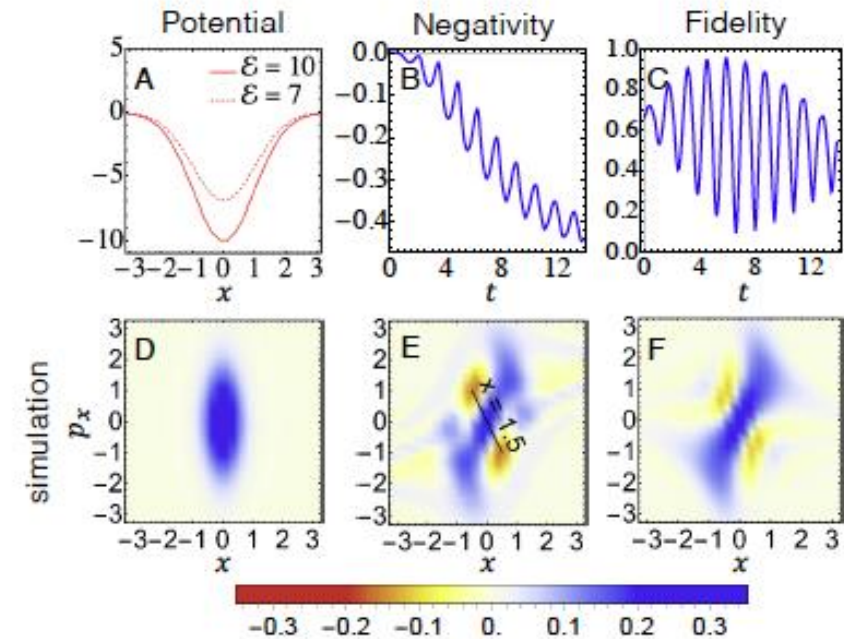
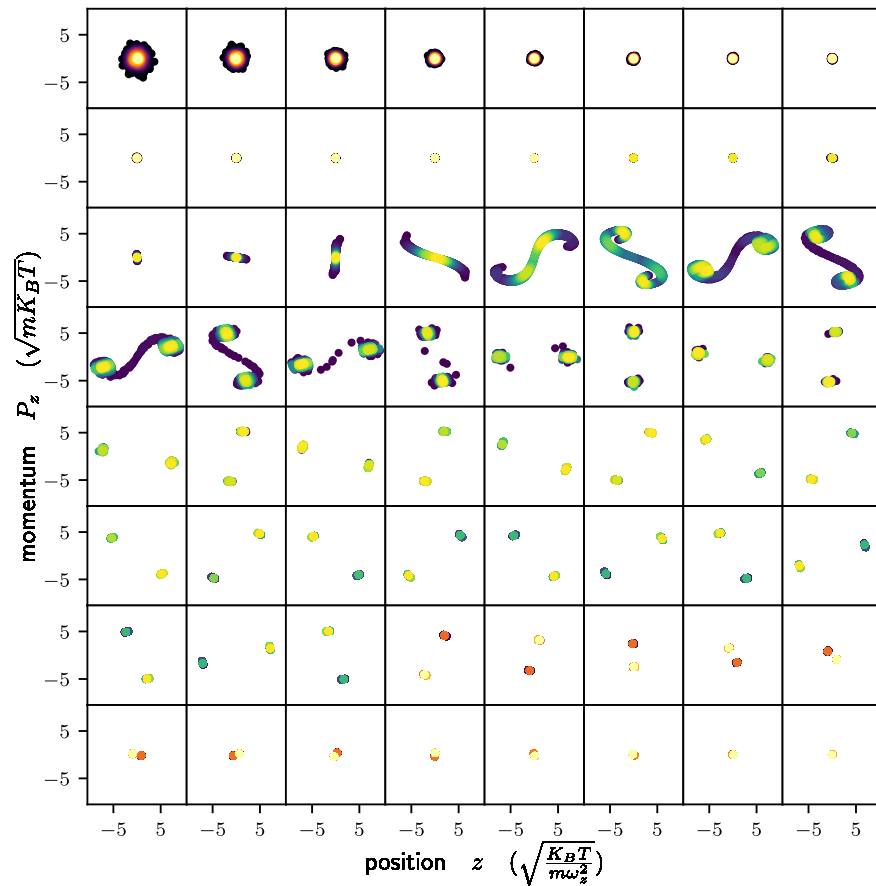
Experiment: Bi-modal distribution by squeezing thermal state: accessing x^4 Duffing trap non-linearity



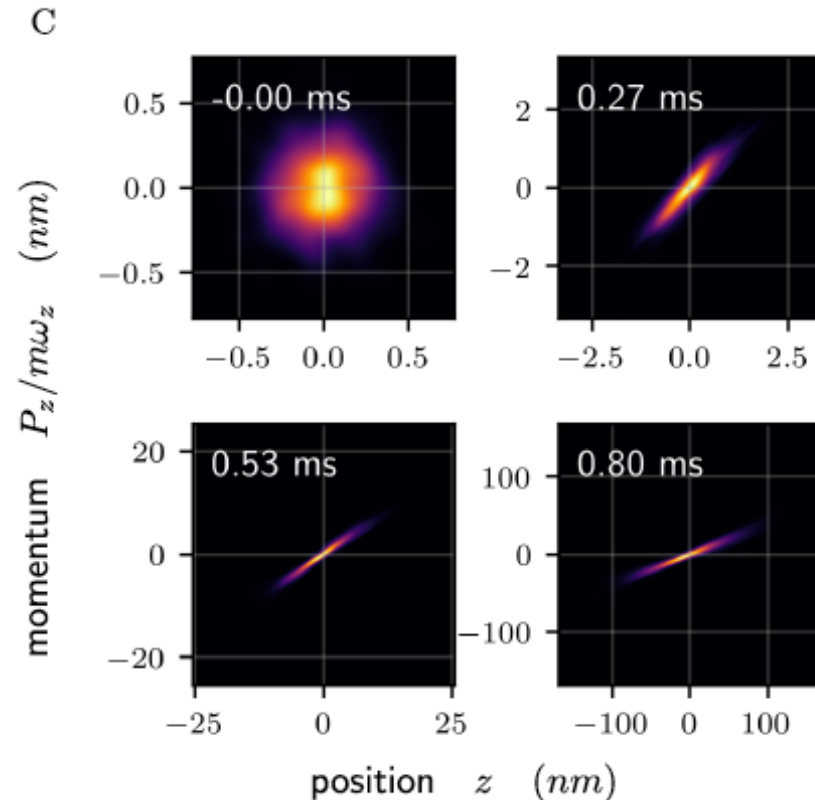
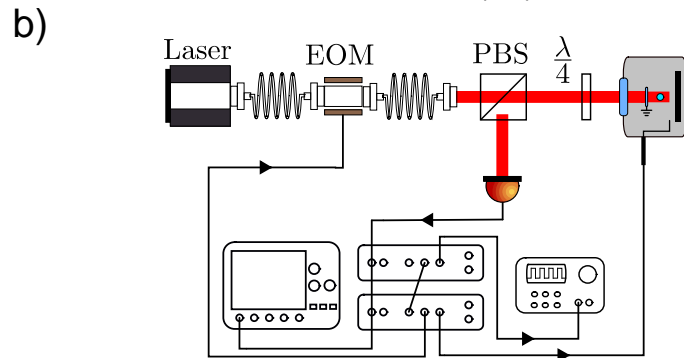
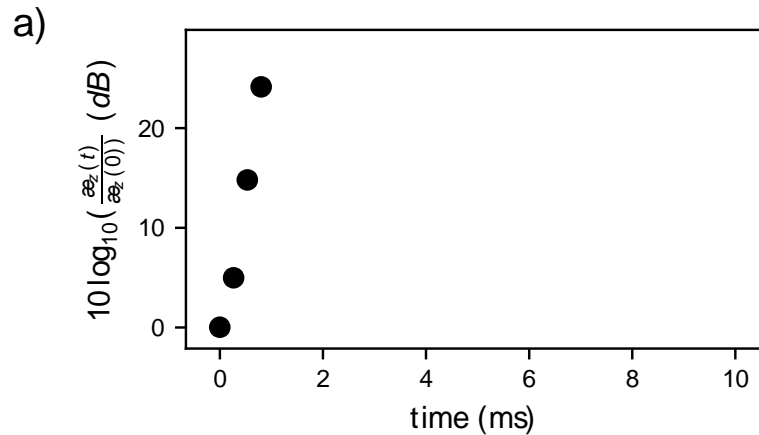
Muffato, R., Georgescu, T., Homans, J., Guerreiro, T., Wu, Q., Chisholm, D., Carlesso, M., Paternostro, M. and Ulbricht, H., 2024.

Generation of classical non-Gaussian distributions by squeezing a thermal state into non-linear motion of levitated optomechanics. *arXiv preprint arXiv:2401.04066*.

Simulation: Non-Gaussian states by squeezing thermal state: squeezing + cooling + non-linearity



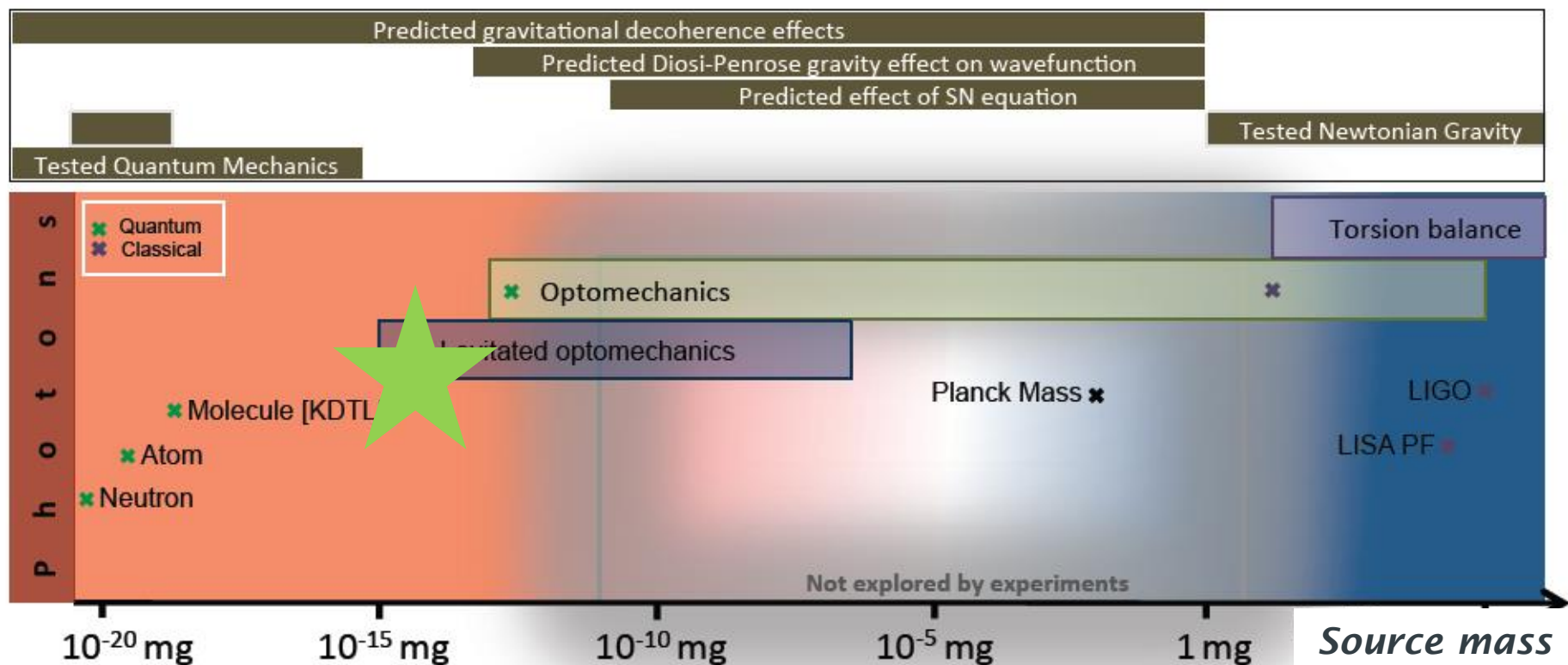
Experiment results: the other option coherent expanding the motional state:



- Pre-cooled to 1000 phonons, then state expanded by trap modulation
- After 1ms of expansion, motional state is about the size of the particle

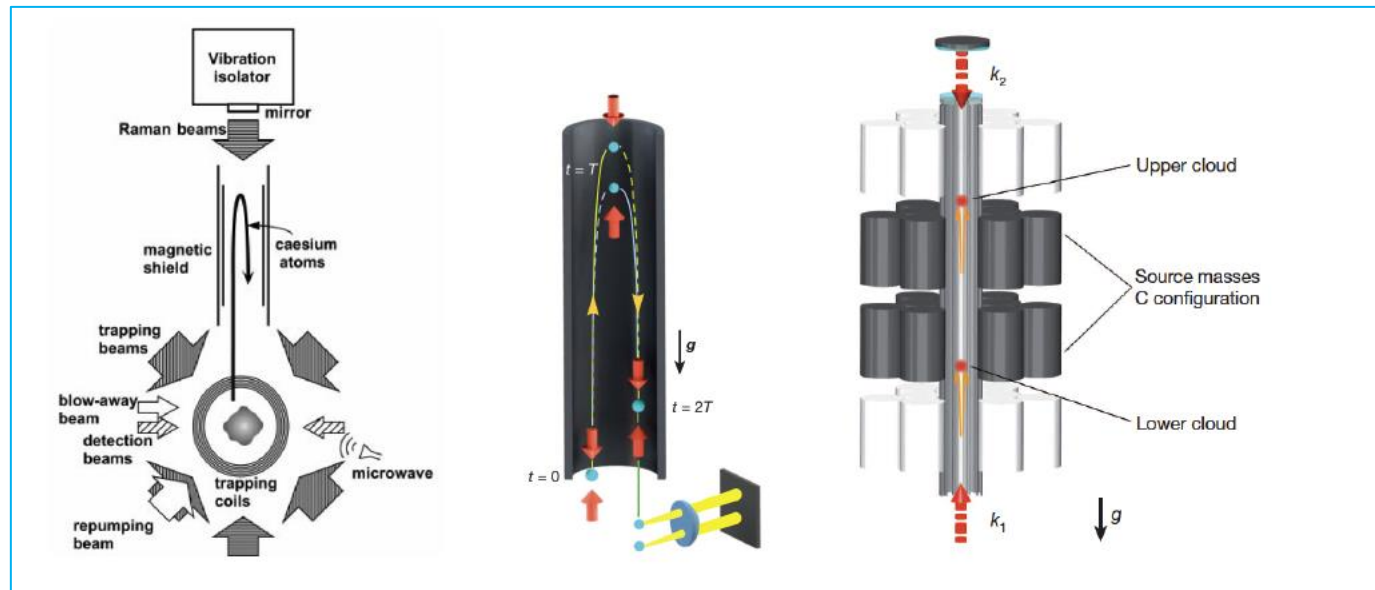
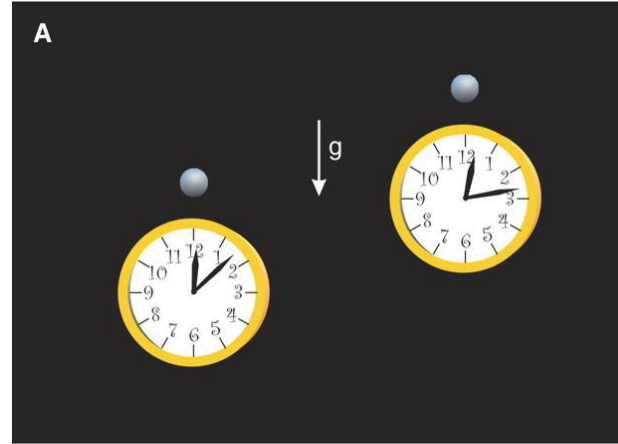
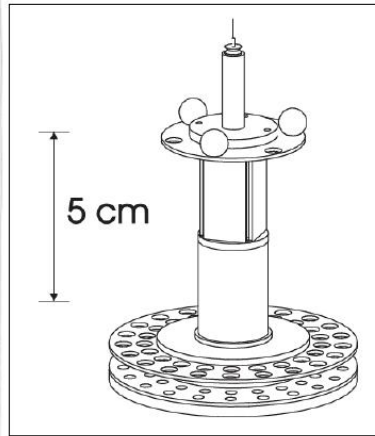
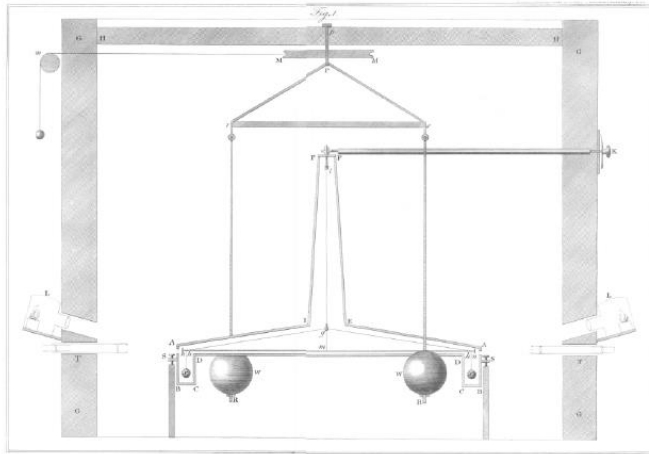
Macroscopic quantum: where are we?

Experimental target with levitated particles at the moment (100 nm particle)
[*Superposition size larger than the size of the particle*]



MEASURING TWO-MASS GRAVITY

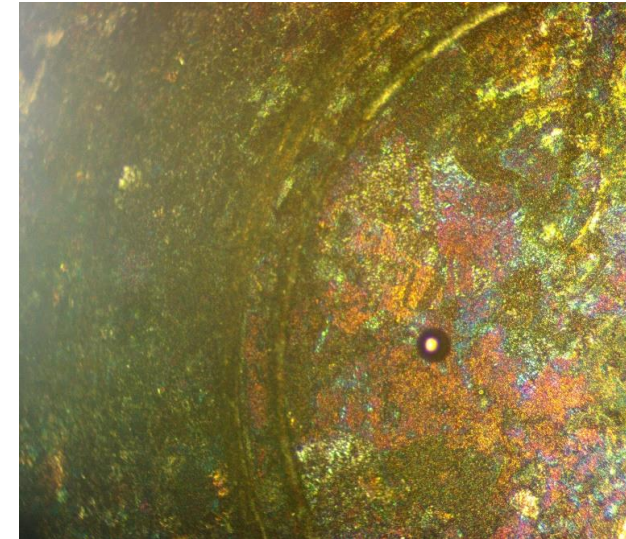
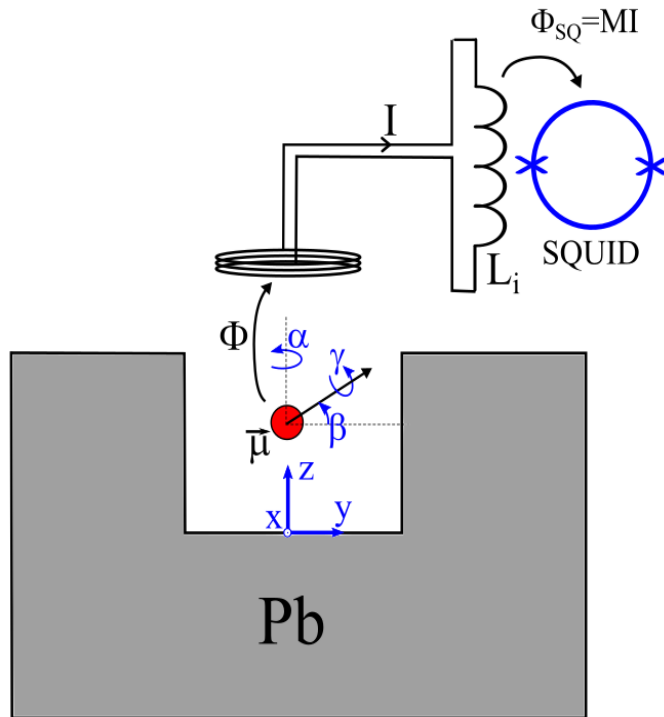
How do we measure gravity?



- Torsion pendulum
- Atom interferometer
- Optomechanics: LIGO
- Clocks for GR effects

Levitated small mass experiments: Meissner trapping of ferromagnets

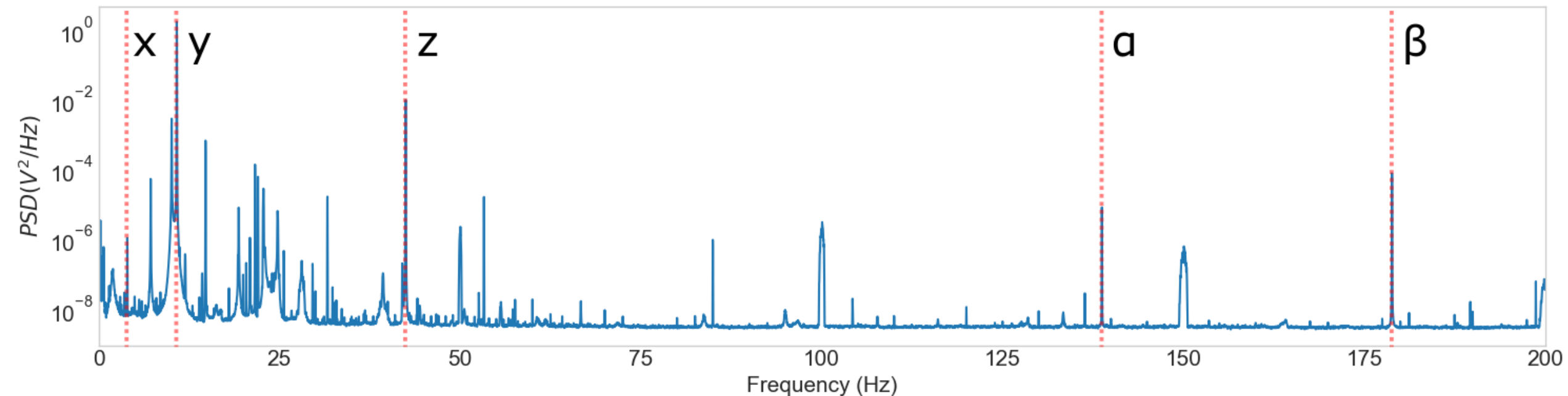
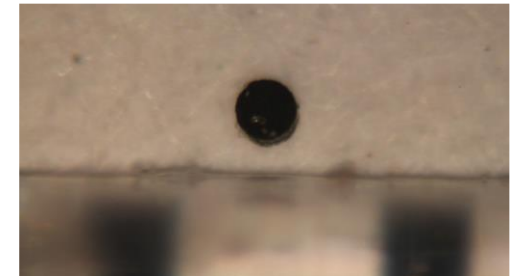
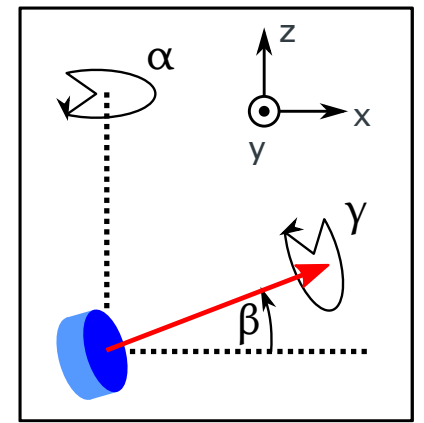
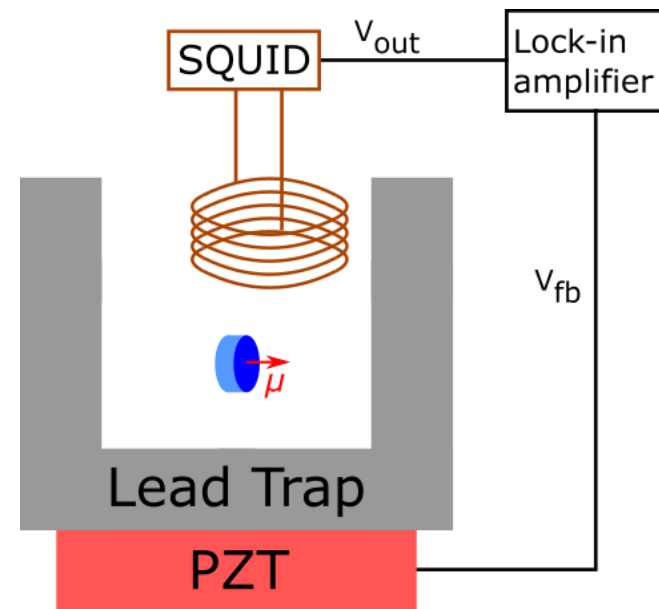
Simple passive trap: particle in the hole:
Lateral surface provides x,y confinement



NdFeB microsphere radius = 27 μm
Trap Radius = 2 mm

Feedback Cooling: PZT kicks

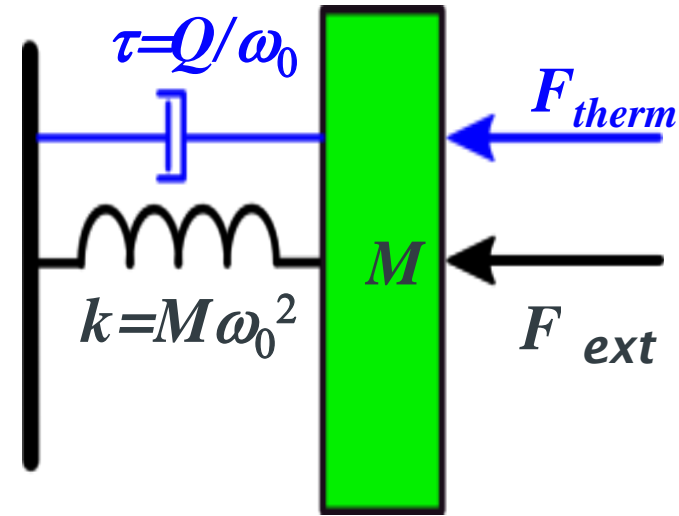
- 100 μm thickness x 200 μm diameter NdFeB magnet
- 3 translational (x, y, z) and 2 librational (α , β) modes
- Background temperature = 410 mK
- Gas pressure = 4×10^{-7} mbar



Force (noise) in harmonic oscillator:

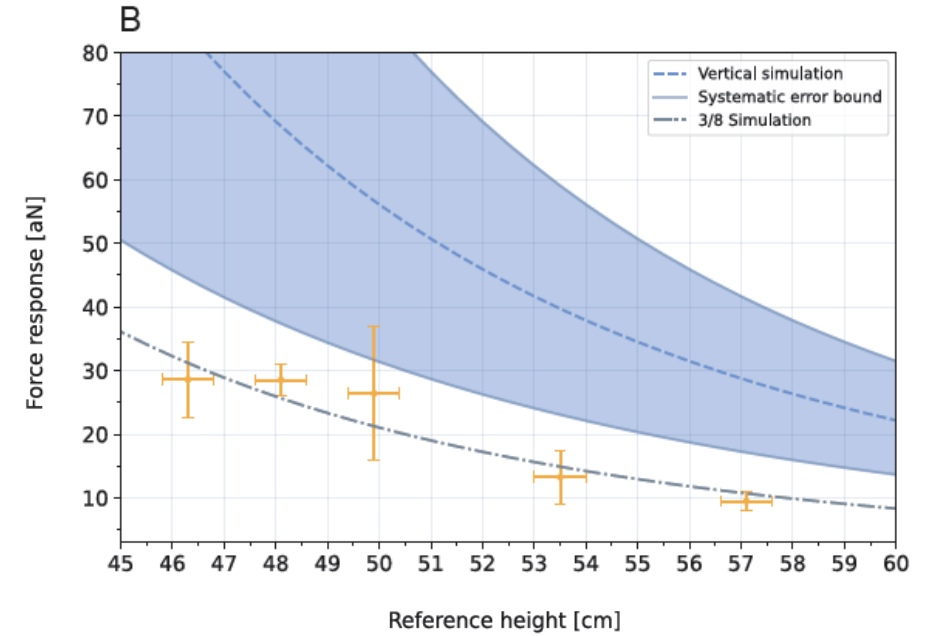
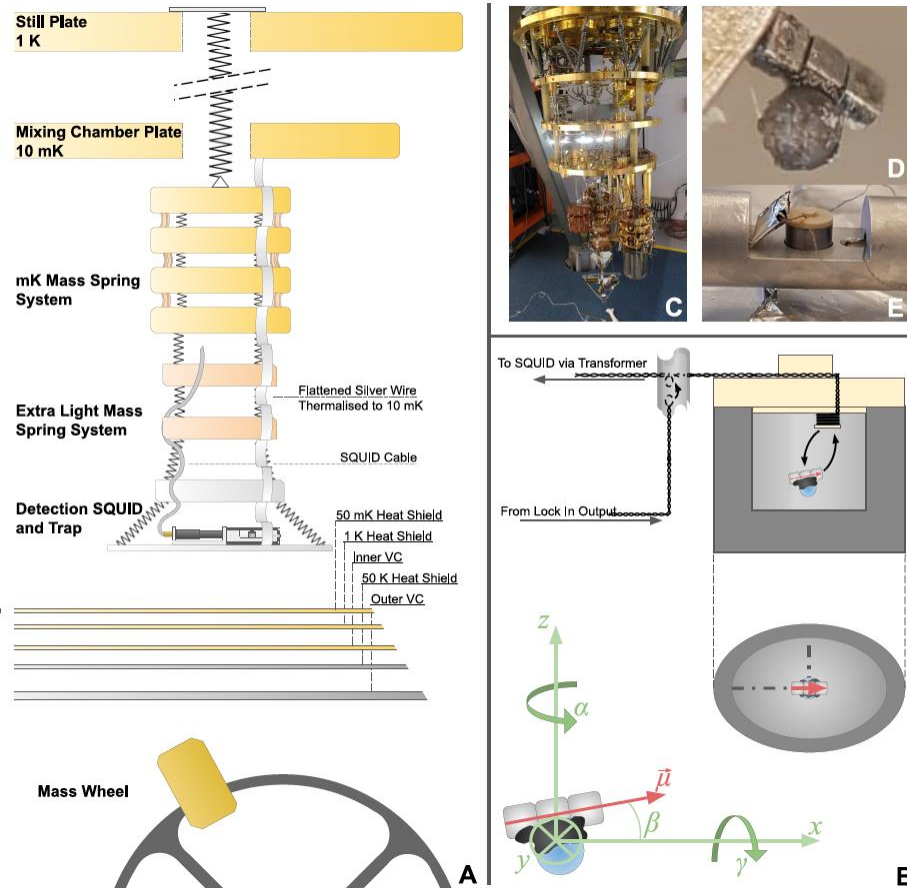
Thermal bath affect minimum force measured:

$$F_{min} = \sqrt{\frac{4k_B T_0 m \omega_0}{Q \tau}},$$



- M. Bahrami et al, PRL **112** 210404 (2014)
- S. Nimmrichter et al, PRL **113** 020045 (2014)
- L. Diosi, PRL **114**, 050403 (2015)
- D. Goldwater et al. Phys. Rev. A **94**, 010104 (2015)
- A. Vinante et al, PRL **116**, 090402 (2016)

Gravity testing with levitated ferromagnet (in Leiden)



- Probe mass: 0.43 mg
- Source mass: 2.45 kg (on wheel)
- $Q = 10^7$ @ 26 Hz
- 30 aN, 8 mHz linewidth
- 3/8 of expected Newtonian gravity

Our next gravity experiment

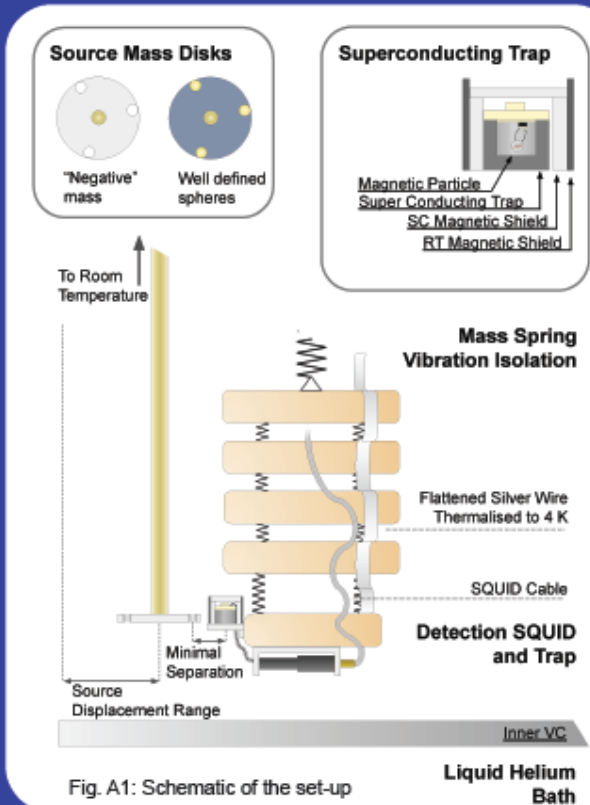


Fig. A1: Schematic of the set-up

Small Scale Gravity

To test the interplay between quantum mechanics and gravity, we must push gravitational detection to ever smaller scales, whilst pushing quantum mechanical effects to ever larger scales.

Passive levitation of magnets in superconducting traps offers great scalability, up from micrometer sized particles to centimeter sized objects. This allows us to push on both boundaries in the same set-up.

To detect gravitational coupling, we use 500 μm sized particles coupled to a cryogenic mass-wheel.

From this, we will be able to detect gravitational coupling down to 10^{-13} g, an improvement from our previous work at roughly 10^{-11} g [1]. In this range, proposed theories of Modified Newtonian Gravity should deviate from classical predictions.

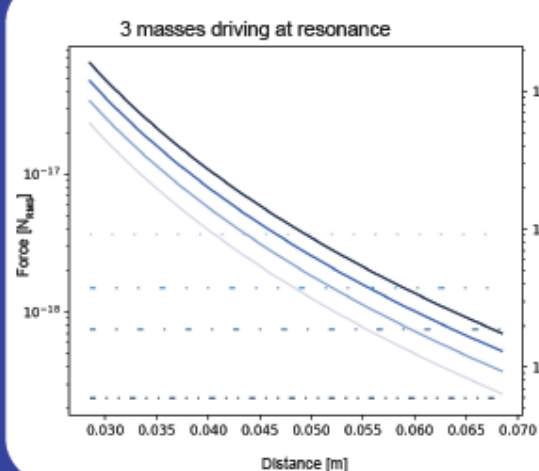
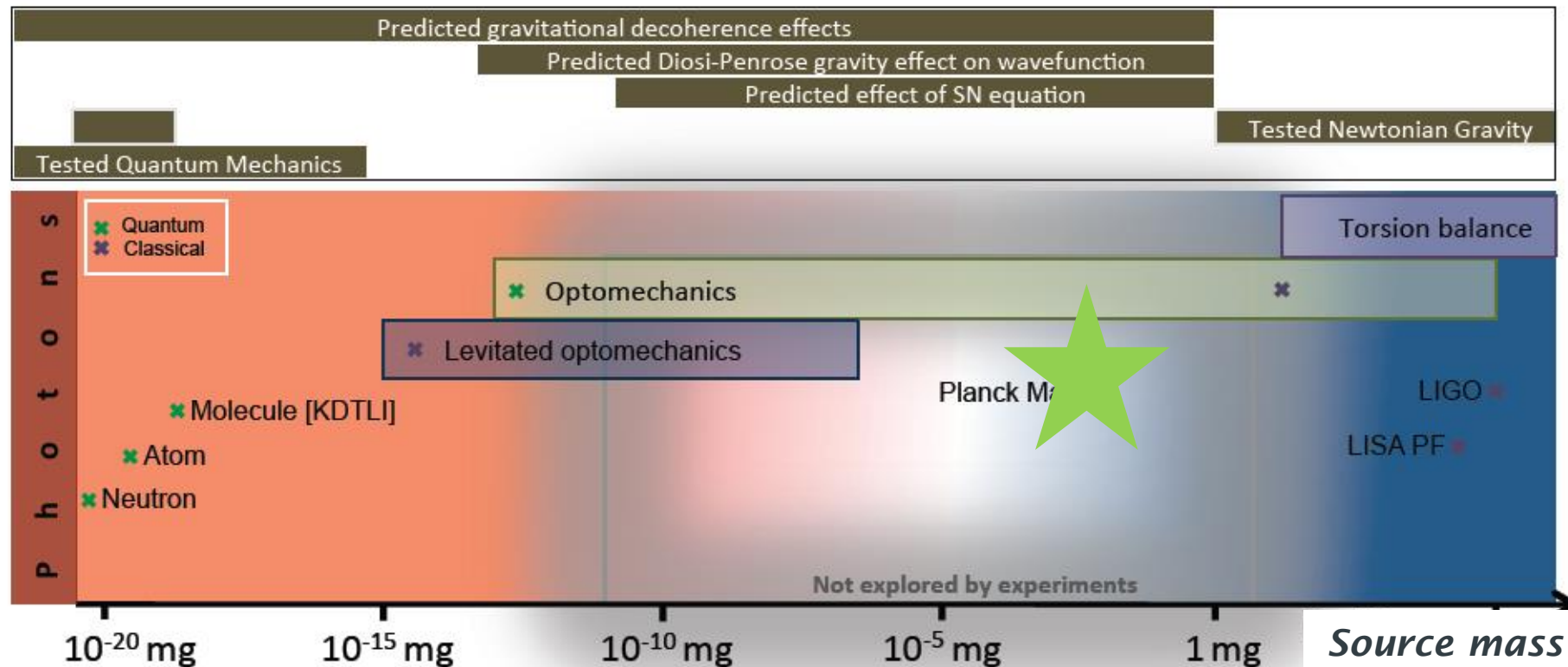


Fig. A2: Theoretical prediction for Force/Acceleration as function of Source Displacement, assuming a sensing mass of 1 mm diameter and a Q factor of 10^6

- 1.5 mm source
- 1.7 mm source
- 1.9 mm source
- 2.1 mm source
- · · S_w after 1h
- · · S_w after 6h
- · · S_w after 24h
- · · S_w after 240h

Small mass gravity: where are we?

Current experimental target with probing by levitated particle (10 microgram)



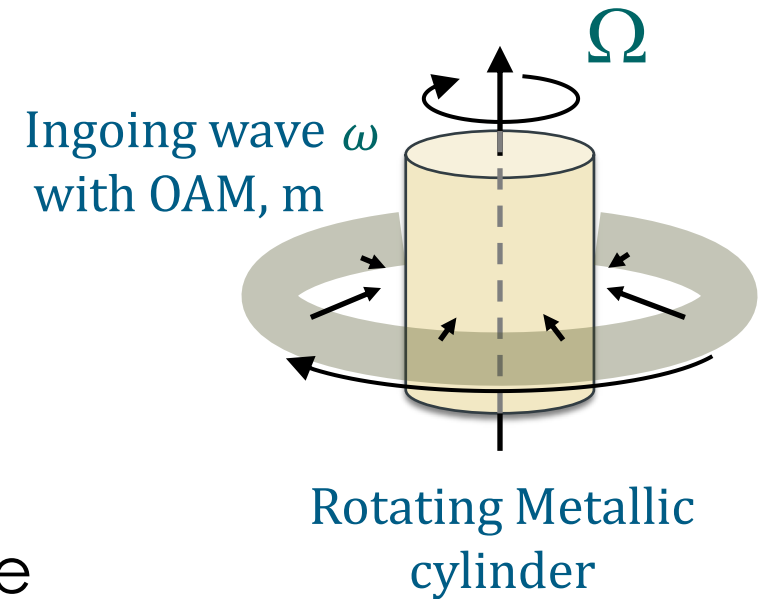
ZEL'DOVICH EFFECT

Rotating absorbers can amplify waves that have angular momentum



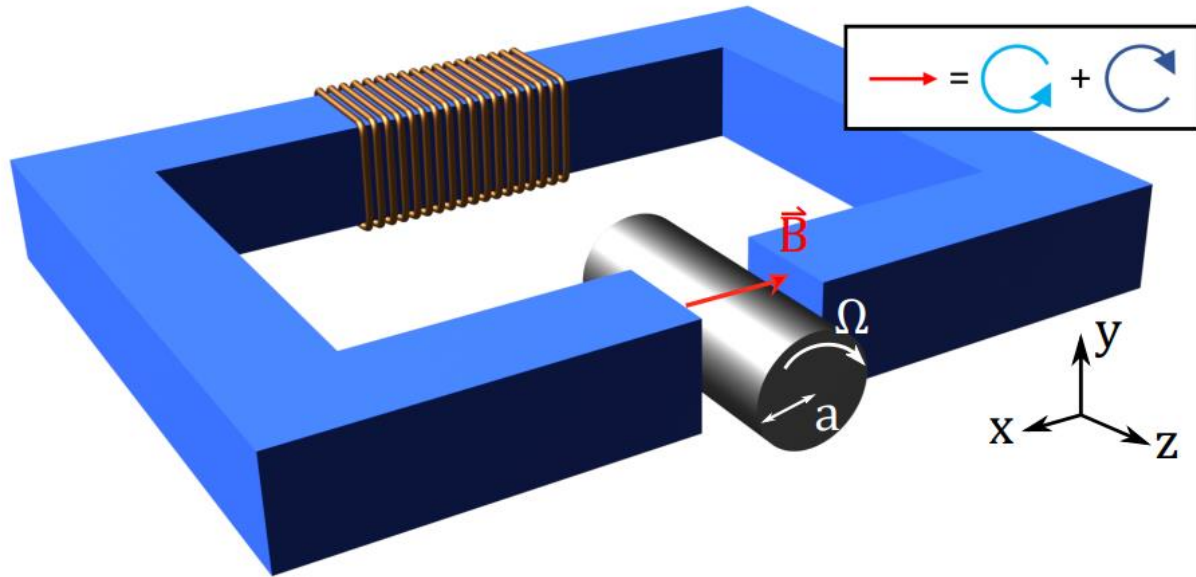
Waves of frequency ω and angular momentum order m should become amplified after interacting with an absorber co-rotating at Ω when:

$$(\omega - m\Omega) < 0$$

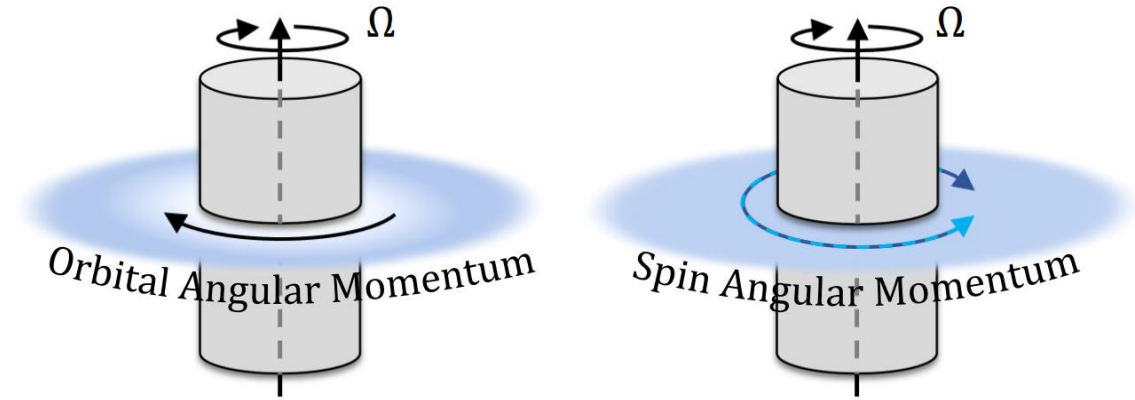


Zel'dovich Effect with EM

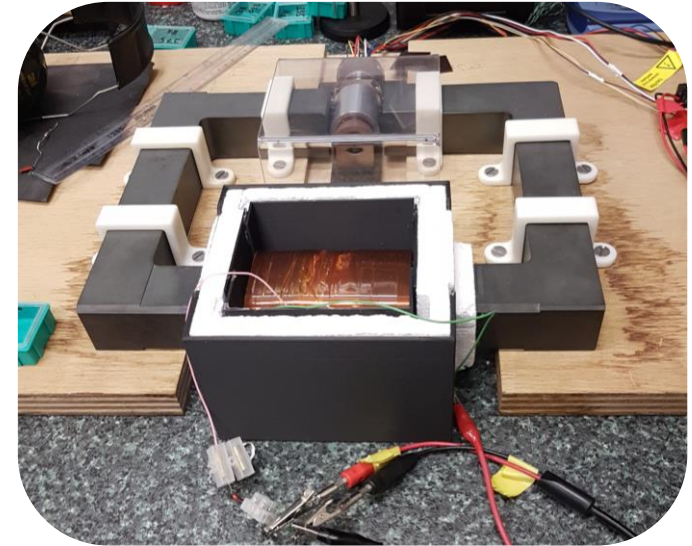
- Resonant LC circuits (frequency ω) forming magnetic fields interacting with a rotating metal cylinder (frequency Ω)



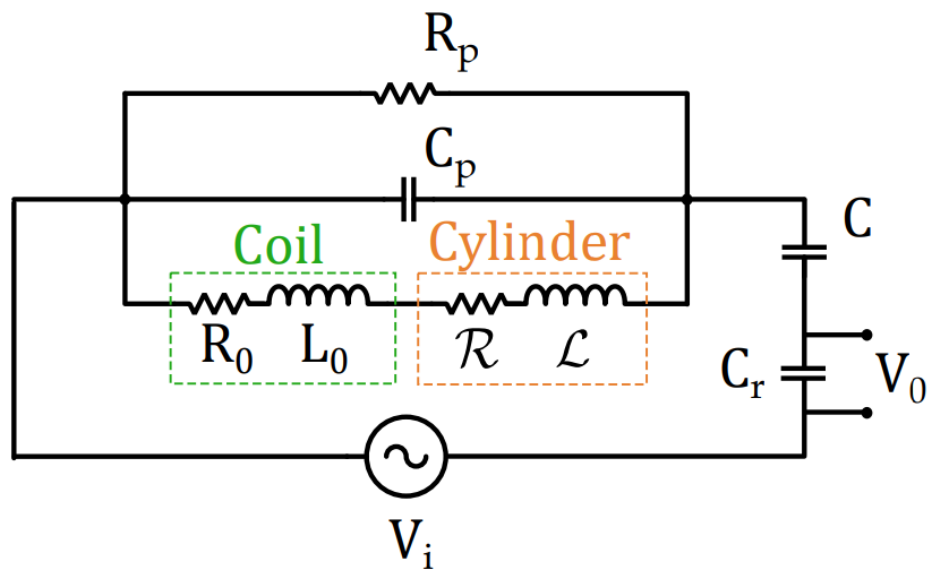
$$\begin{aligned} \mathbf{B}_0 &= I\beta(1, 0, 0)^T e^{i\omega t} \\ &= \frac{1}{2}I\beta [(1, i, 0)^T + (1, -i, 0)^T] e^{i\omega t} \end{aligned}$$



$$(\omega - \ell\Omega) < 0 \quad \Rightarrow \quad (\omega - s\Omega) < 0$$

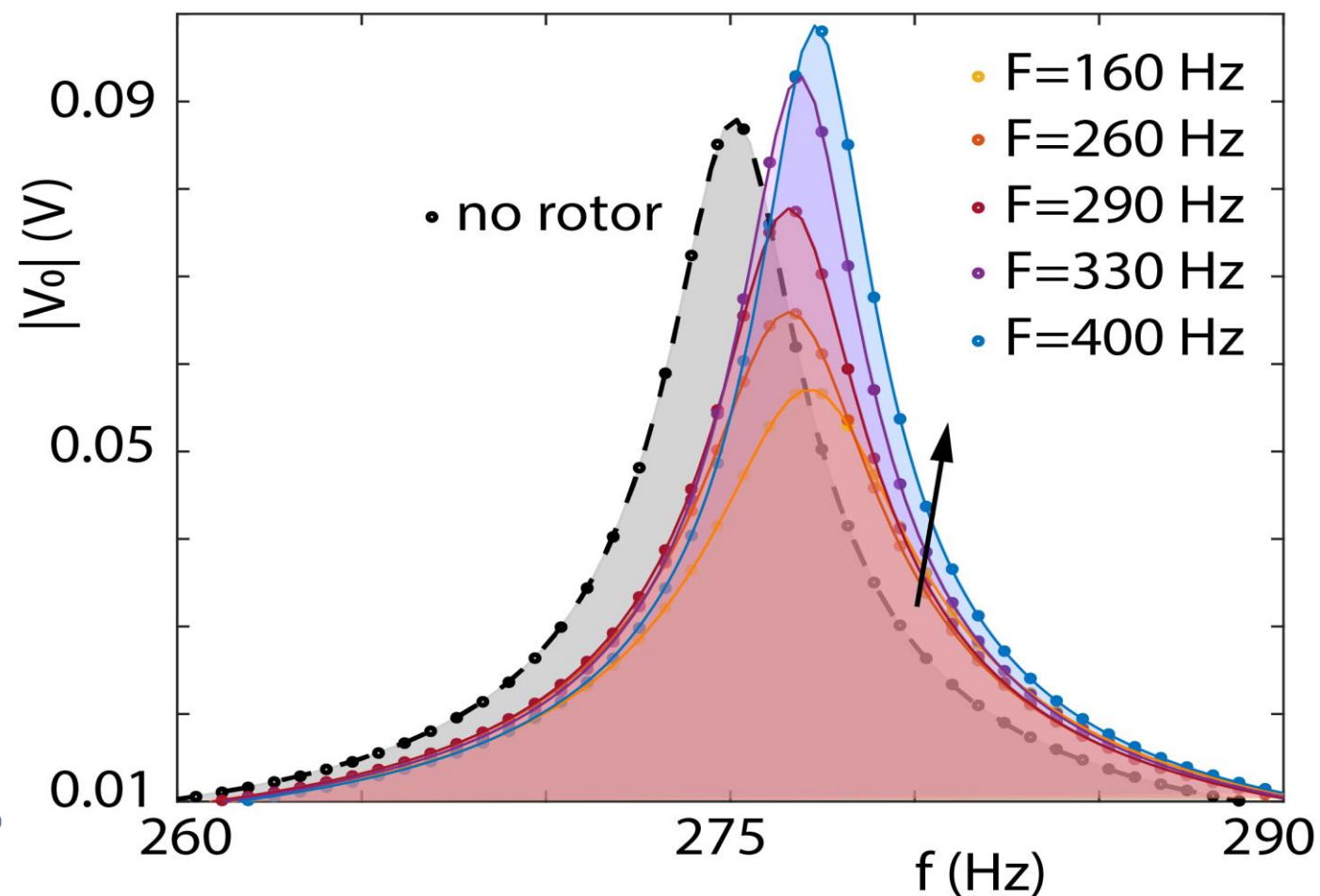
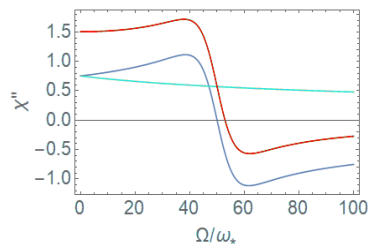


$$\mathcal{R} = \text{Re}[V/I] = \omega\beta^2 [\chi''(\omega - \Omega) + \chi''(\omega + \Omega)]$$

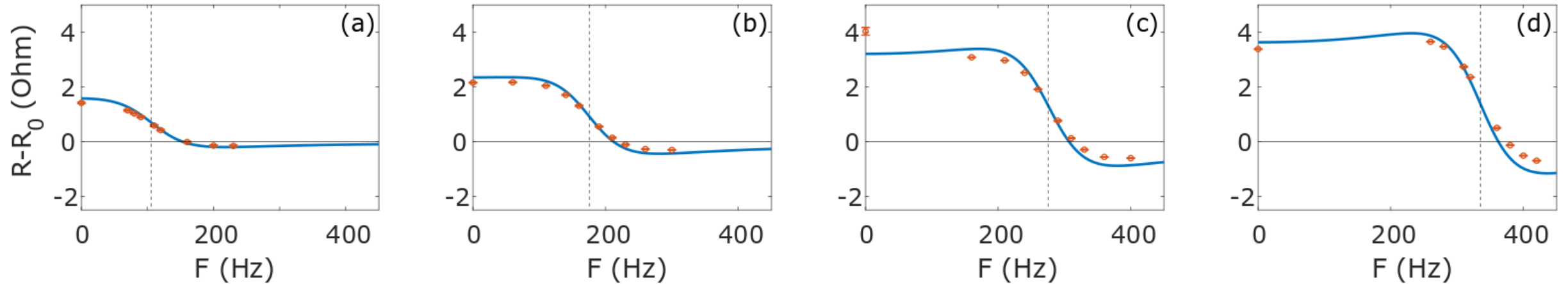


(β is a coupling factor that depends on the system geometry)

Amplification threshold rotation frequency F_{th} slightly higher than resonant circuit frequency f_0 , due to presence of lossy counter-rotating component

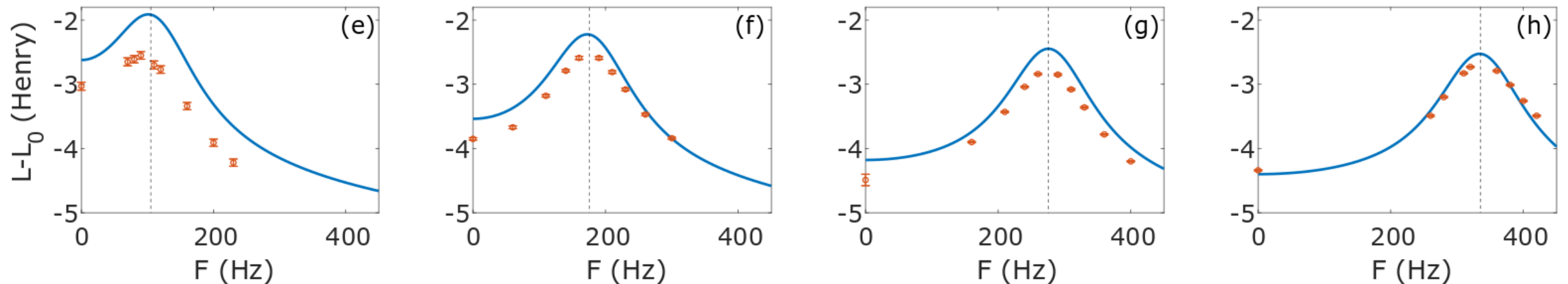


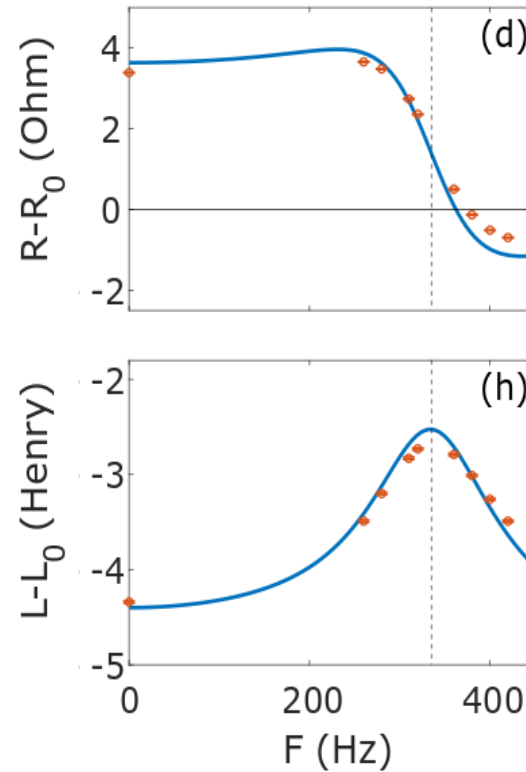
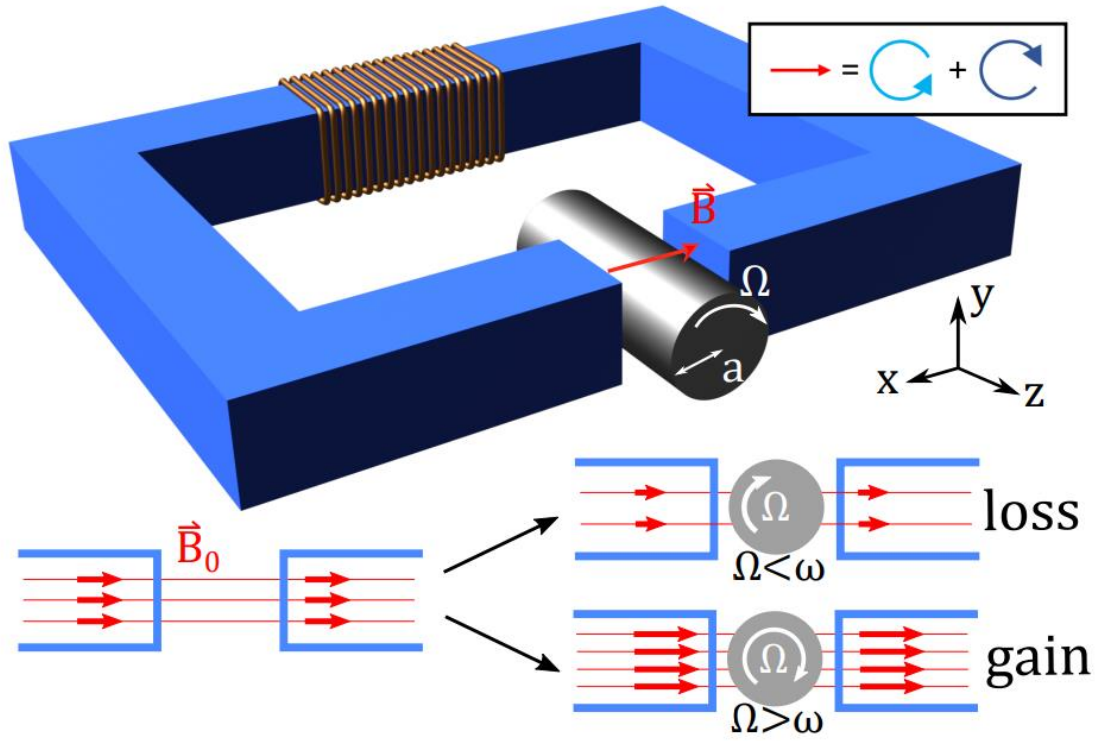
$$\mathcal{R} = \text{Re}[V/I] = \omega\beta^2 [\chi''(\omega - \Omega) + \chi''(\omega + \Omega)]$$



Changing capacitors gives different resonant frequencies of the circuit (dotted vertical line). Bigger effects at higher frequencies

$$\mathcal{L} = \text{Re}[\Phi/I] = \beta^2 [\chi'(\omega - \Omega) + \chi'(\omega + \Omega)]$$





$$R_0 = 2.03 \text{ k}\Omega$$

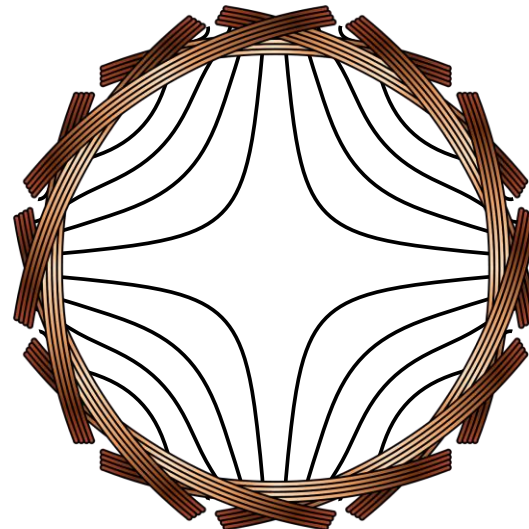
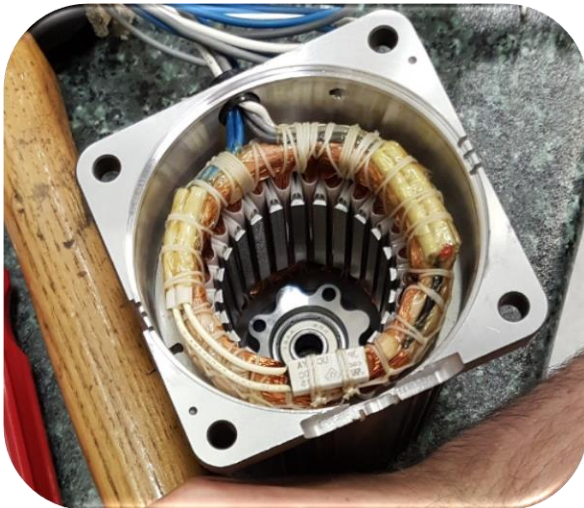
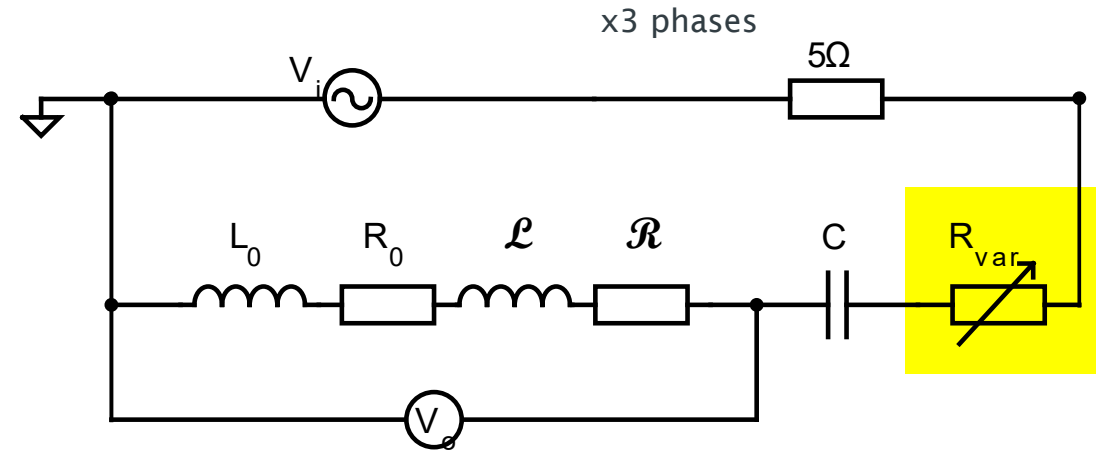
$$L_0 = 263 \text{ H}$$

- New-found links to induction generators

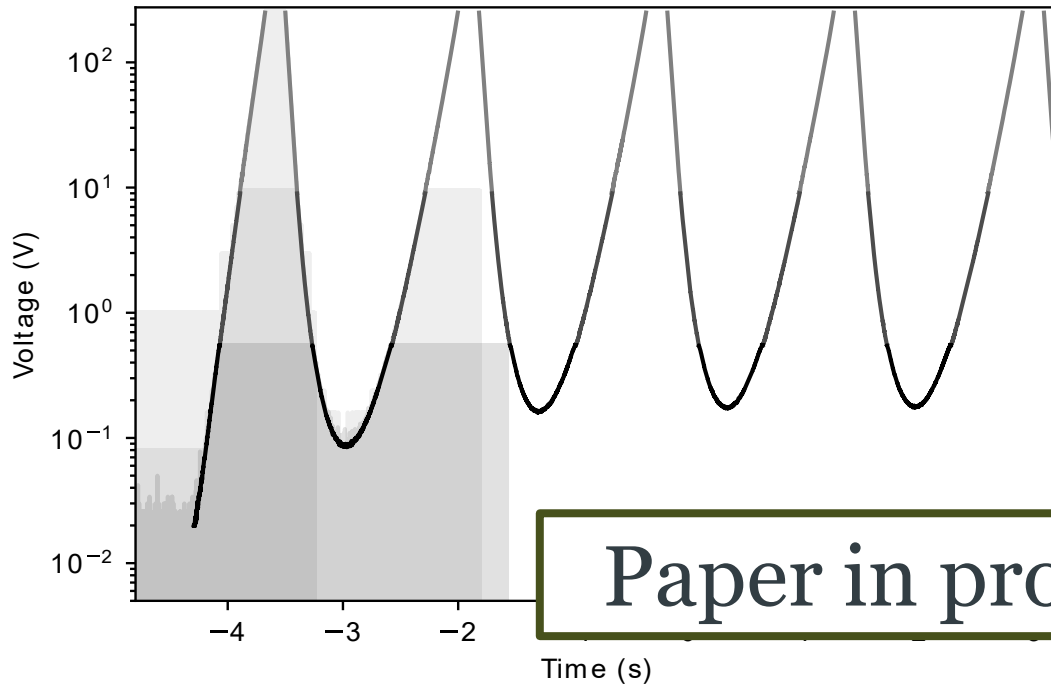


Zel'dovich Effect with EM: 3-phase configuration

- Resonant LC circuits from induction motor coils forming a **rotating magnetic field** interacting with a rotating metal cylinder
- Previous: coupling low, extra counter-rotating component, overall circuit resistance (2kOhm) much bigger than change due to effect.(2-60hm)
- This: high coupling, rotating (quadrupole) magnetic field, lower overall circuit resistance (~80 Ohm) on same order as change



36 krpm (demand speed)



Paper in progress.....

Generation regime – seeded by thermal/electronic noise

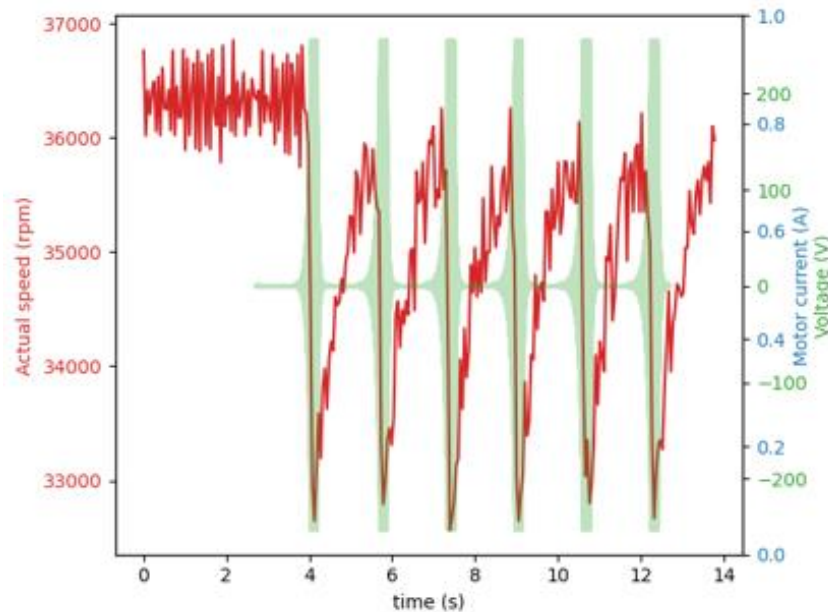
amplified, and all others become attenuated. In the presence of an external reflector with small losses (resonator), the amplification following single scattering may turn into generation. The linear velocity on the surface of the

Ya.B. Zel'dovich. *JETP Lett.* 14, 180 (1971)

Zel'dovich, Ya. B., Rozhanskii, L. V. & Starobinskii, A. A. *Radiophys Quantum Electron* 29, 761-768 (1986).

By itself, a few tenths of a per cent is unimpressive; but any amplification mechanism admits improvement by positive feedback. To illustrate, in a rather speculative vein, we propose the “black-hole bomb” (closely related to a recent suggestion of Zel'dovich⁶): locate a rotating black hole and construct a spherical mirror around it. The mirror must reflect low-frequency radio waves (equation (4); and we now make the transition from scalar to electromagnetic fields) with reflectivity $\gtrsim 99.8\%$, so that in one reflexion and subsequent superradiant scattering there is a net amplification. The system is then

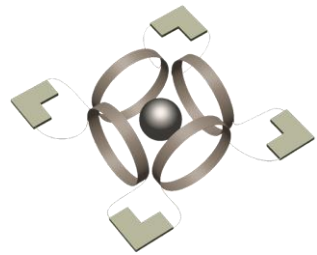
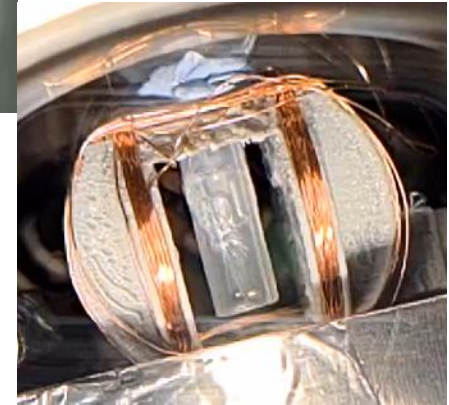
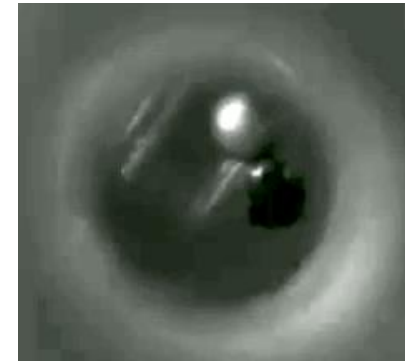
Press and Teukolsky, ‘Floating Orbits, Superradiant Scattering and the Black-Hole Bomb’. *Nature* 238 (1972)



Project: Zel'dovich Effect with EM

Future: possible routes to the quantum realm

- Levitated microsphere spinning at MHz or more (?)
- Interacts with surrounding superconducting circuit
 - GHz rotation could move test to the quantum spontaneous generation regime



M. C. Braidotti, A. Vinante, G. Gasbarri, D. Faccio, & H. Ulbricht, *Phys. Rev. Lett.* **125**, 140801 (2020).
[10.1103/PhysRevLett.125.140801](https://doi.org/10.1103/PhysRevLett.125.140801)



Summary of talk

- Pushing on gravity and quantum experiments.
- Testing macroscopic quantum.
- Testing small-mass gravity.
- Then both: gravity in superpositions. [did not manage in time]

IDEAS FOR GRAVITY IN QUANTUM SUPERPOSITIONS

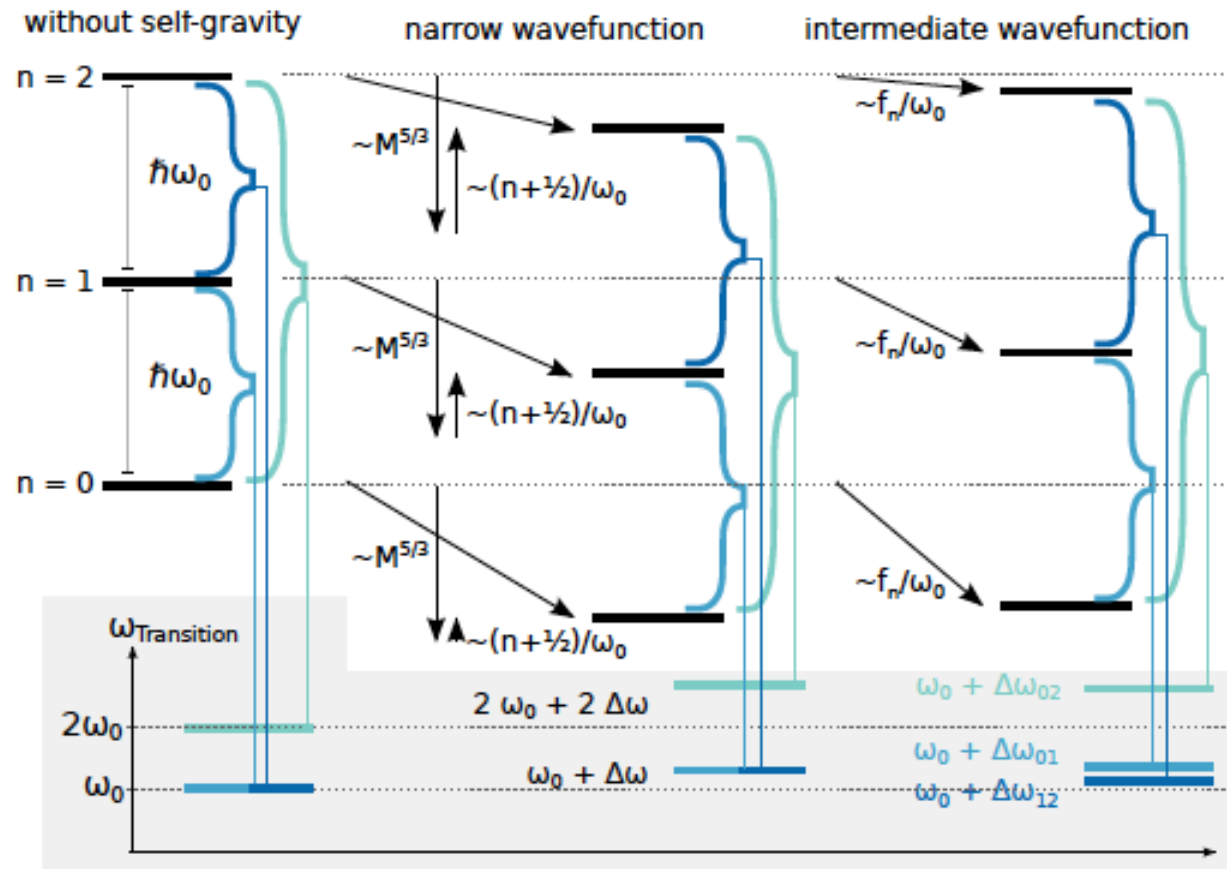
Schroedinger-Newton (SN): semi-classical gravity

$$R_{\mu\nu} + \frac{1}{2}g_{\mu\nu}R = \frac{8\pi G}{c^4} \langle \Psi | \hat{T}_{\mu\nu} | \Psi \rangle .$$

$$i\hbar \frac{\partial}{\partial t} \psi(t, \mathbf{r}) = \left(\frac{\hbar^2}{2M} \nabla^2 + V_{\text{ext}} + V_g[\psi] \right) \psi(t, \mathbf{r})$$
$$V_g[\psi](t, \mathbf{r}) = -G \int d^3r' |\psi(t, \mathbf{r}')|^2 I_{\rho_c}(\mathbf{r} - \mathbf{r}') .$$

Obvious option for test: study free wavefunction expansion

Predicted shifts of energy levels according to SN

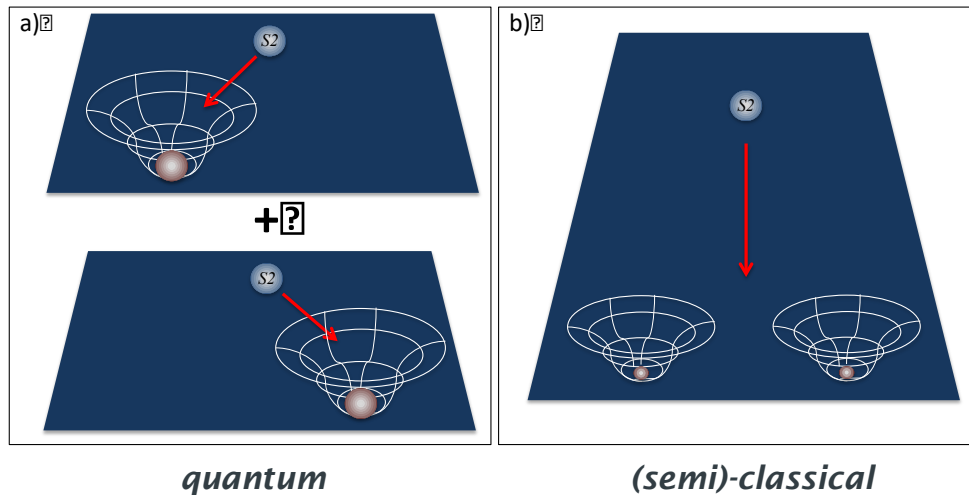


- SN shift of energy levels of mechanical harmonic oscillator
- Feasible for a test with existing tech

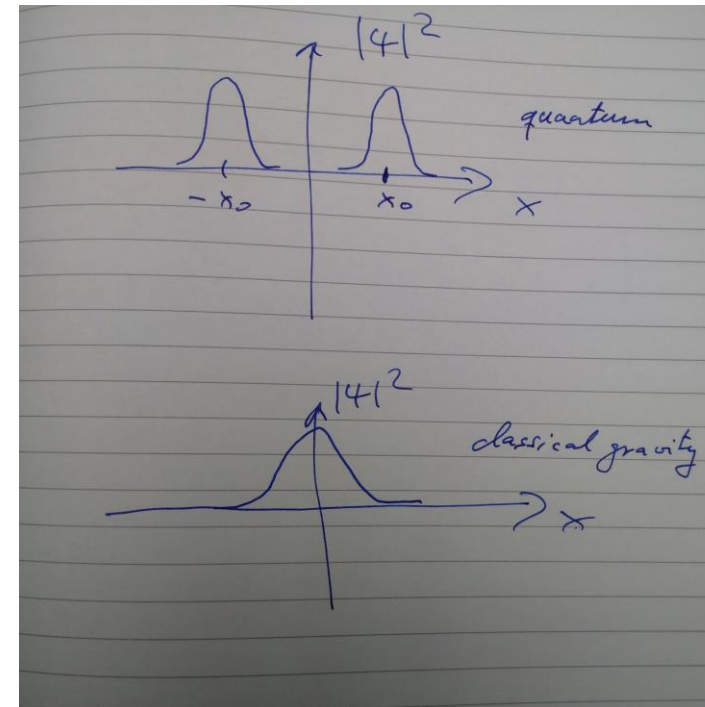
Feynman's (Bronstein's) old question ...

How does the gravitational field of a spatial quantum superposition state look like?

Concept of experiment:



Expected experimental outcome,
Multiple measurements of probe/test
Mass:



Quantum and (semi)-classical gravity have distinctively different outcome of the experiment.

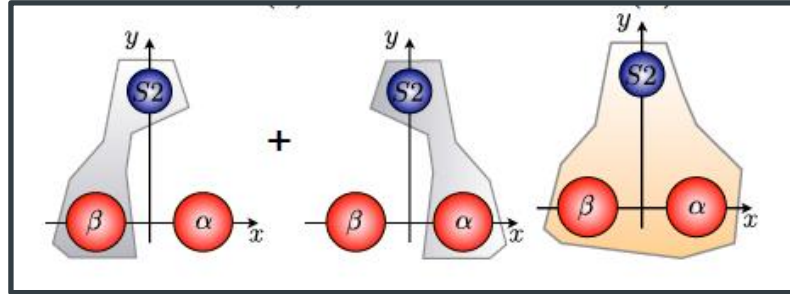
M. Bahrami, A. Bassi, S. McMillen, M. Paternostro, H. Ulbricht, Is Gravity Quantum?, arXiv:1507.05733 (2015).

Testing the gravitational field generated by a superposition state.

Challenge: find two (sufficiently large) masses at sufficiently close proximity, where the source mass is in quantum state (super-position) and the test mass is sufficiently sensitive to probe the gravity field generated by source.

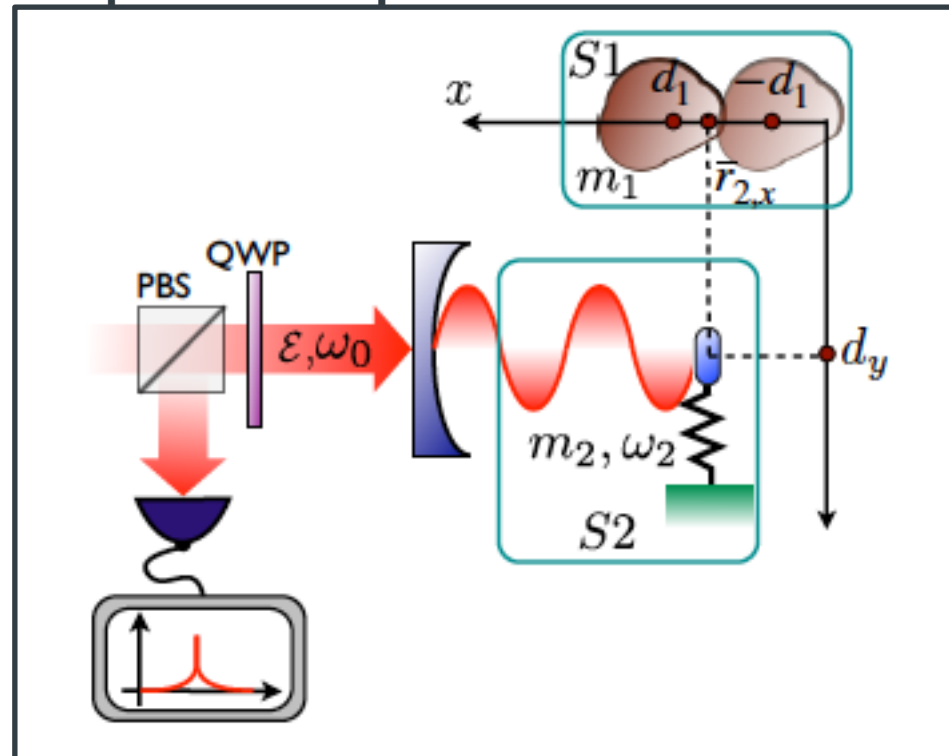
Answer: Optomechanics.

IDEA



- Testing by direct measurement of density noise spectrum
- or by indirect measurement of (quantum) correlations in optical field.
- Biggest challenge: Van der Waals+Casimir-Polder

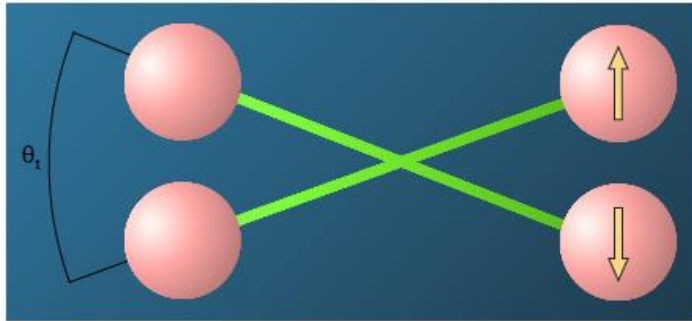
Proposed setup



Matteo Carlesso, Angelo Bassi, Mauro Paternostro, Hendrik Ulbricht

Testing the gravitational field generated by a quantum superposition, New Journal of Physics 21, 093052 (2019).

Angular superposition: Does gravity destroy the superposition?



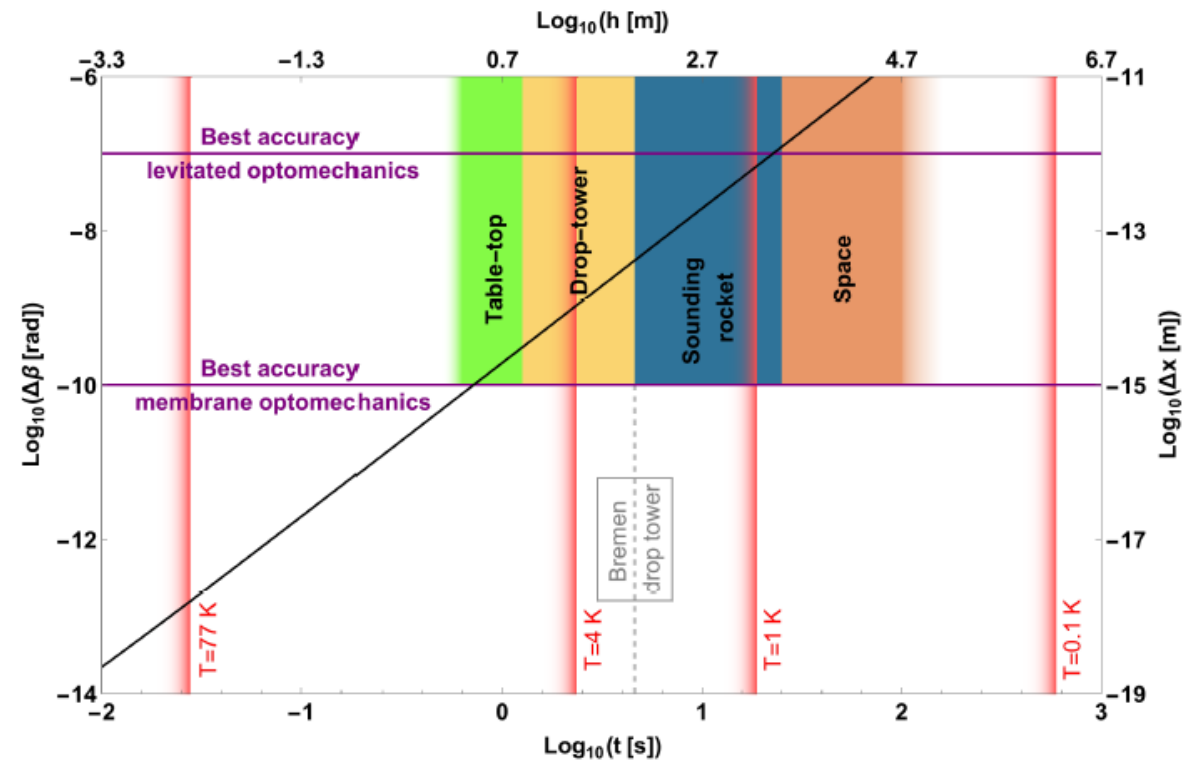
4 seconds of free fall required.
 -> drop tower, Einstein elevator or space experiment
 -> **no interactions based on QFT.**

Parameter of proposal:

Mass:	10^{-20} kg
Length of handle:	$10 \mu\text{m}$
Angle separation:	10^{-4} rad
H-field gradient:	10^6 T/m
Free fall time:	4 s
Temperature:	1 K
Vacuum:	10^{-14} mbar

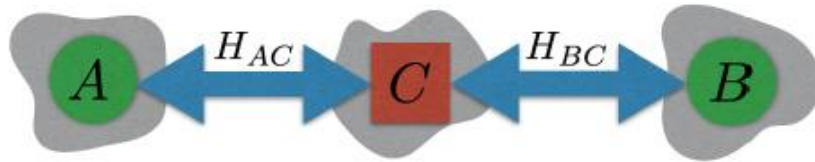
For practical purposes:

libration/rotation degree of freedom is favorable.



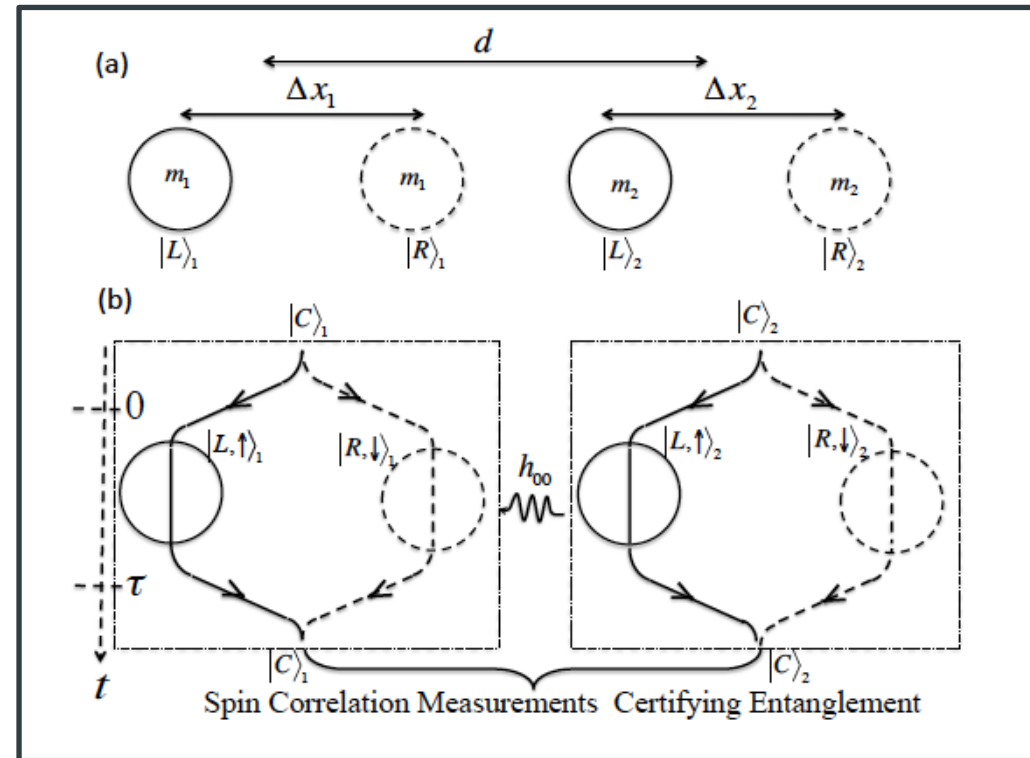
Gravity as entangler: What does it tell about gravity?

Proposed experiment: use NV-centre electron Spin as witness of entangling two particles which only interact by gravity, ... formalized as ABC model



Parameter of proposal:

Masses:	10^{-14} kg
Superposition size:	$250 \mu\text{m}$
Separation (closest approach):	$200 \mu\text{m}$
Free fall time:	3.5 s
Magnetic field gradient:	10^6 T/m
Temperature (internal):	77 K
Vacuum:	10^{-17} mbar

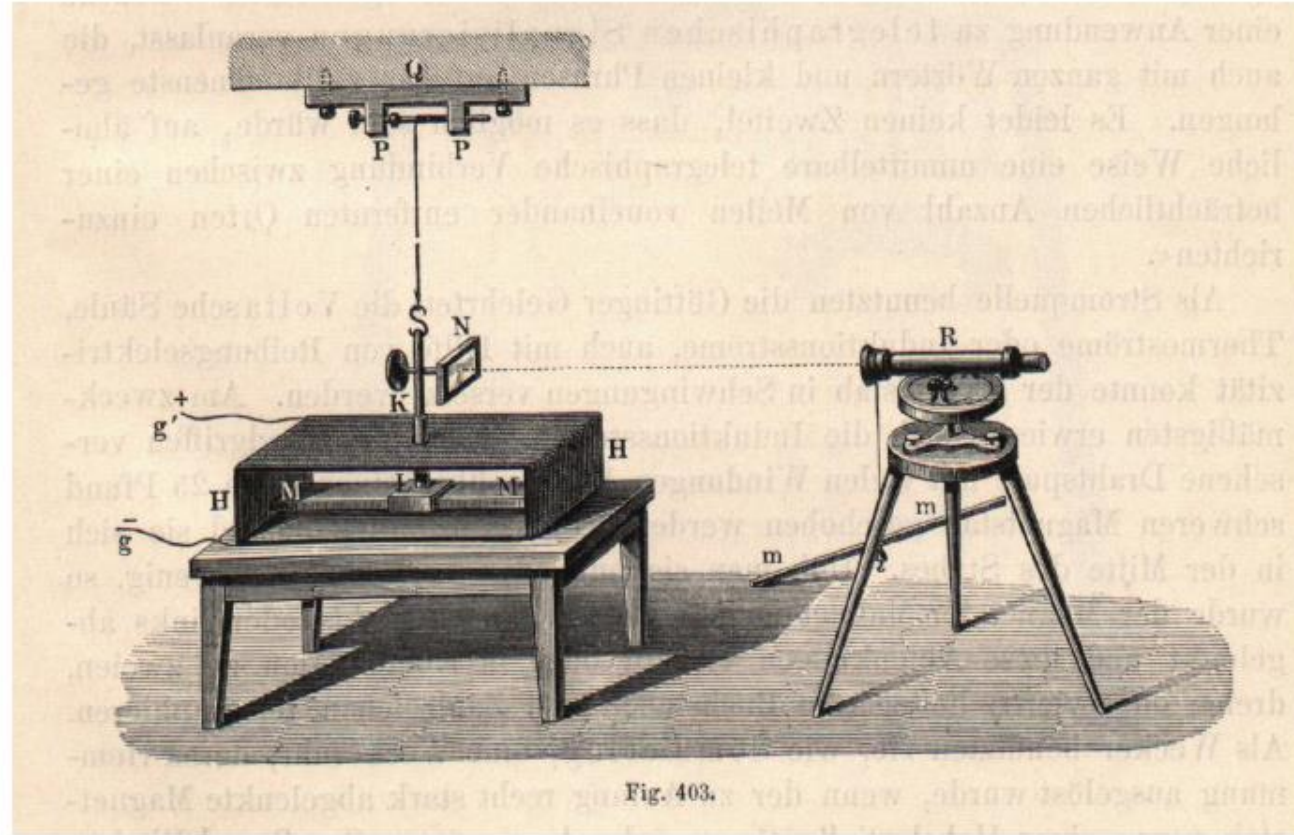


Bose, S., A. Mazumdar, G. W. Morley, H. Ulbricht, M. Toroš, M. Paternostro, A. Geraci, P. Barker, M. S. Kim, G. Milburn, **A Spin Entanglement Witness for Quantum Gravity**, Phys. Rev. Lett. 119, 240401 (2017).

[Krisnanda, T., M. Zuppardo, M. Paternostro, T. Paterek](#), **Revealing non-classicality of inaccessible objects**, Phys. Rev. Lett. 119, 120402 (2017).

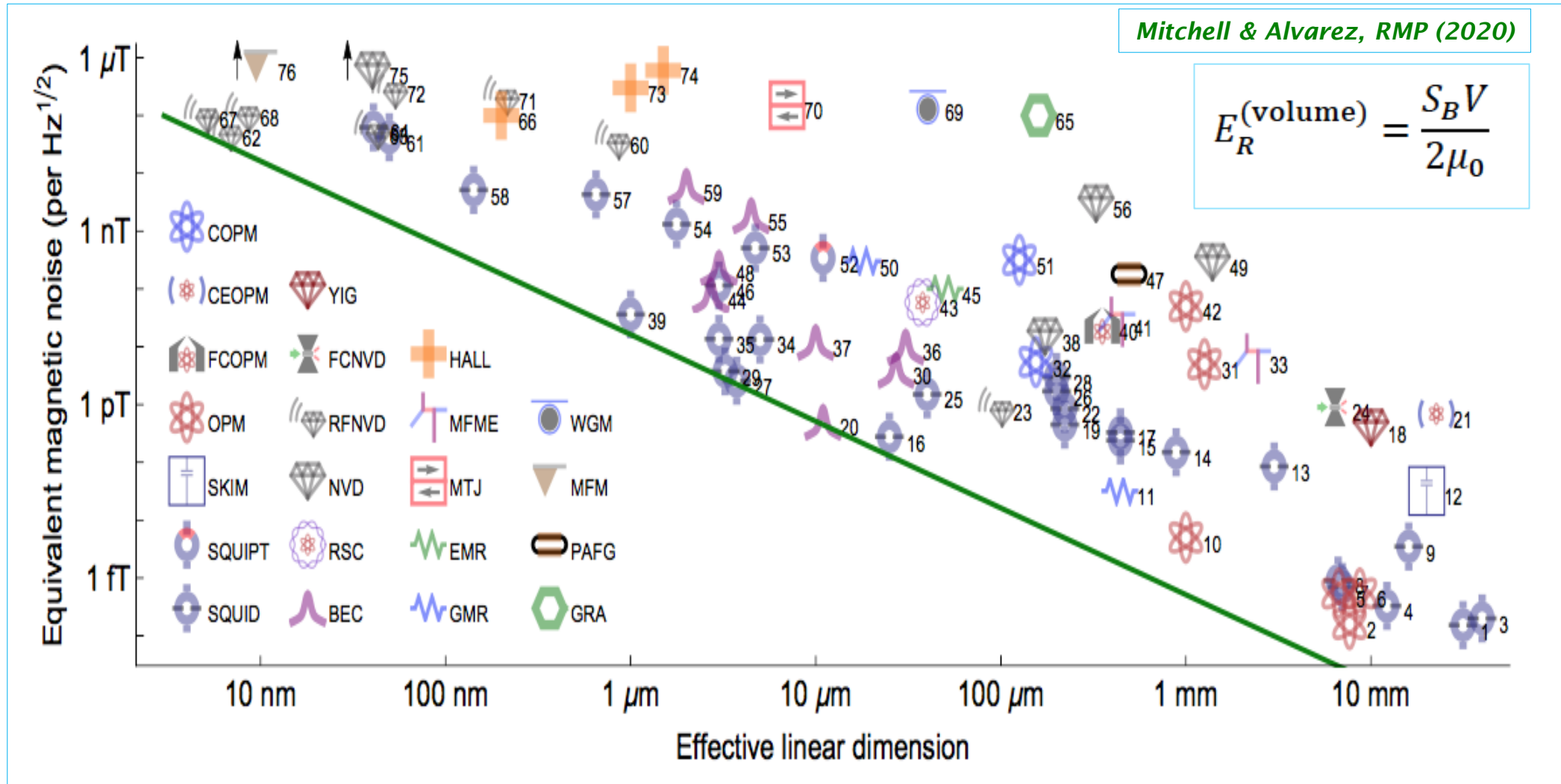
MEASURING B-FIELDS

How do we measure magnetic fields?



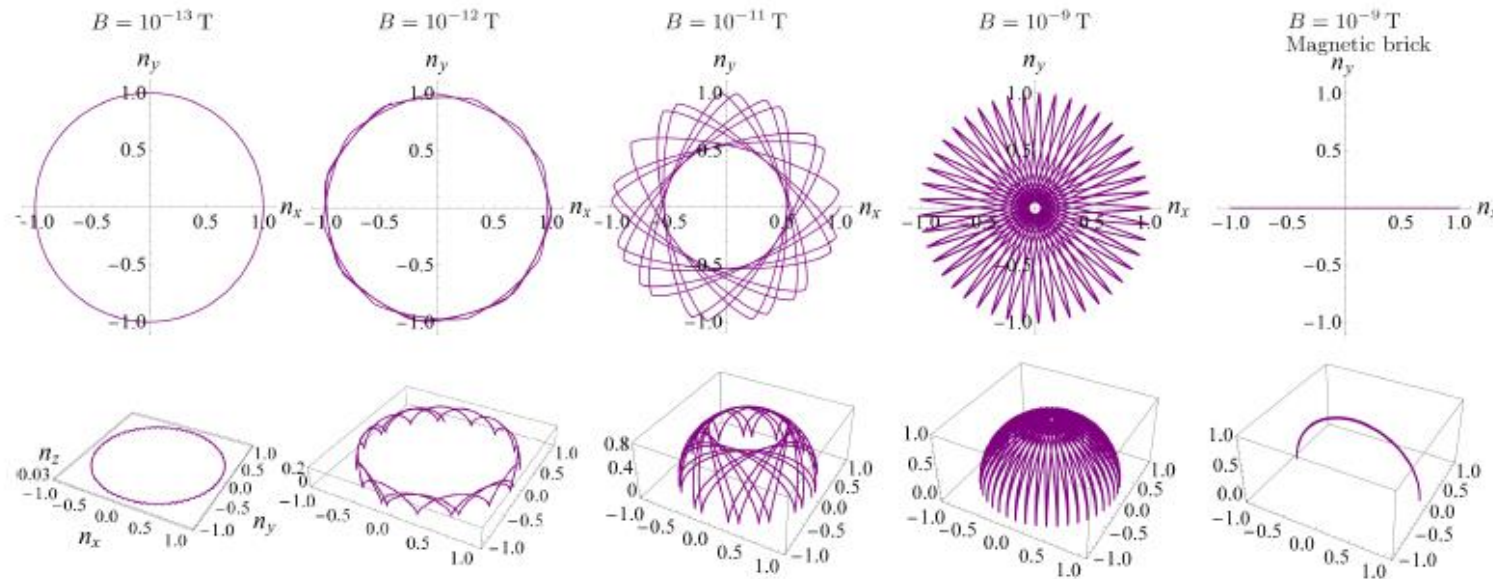
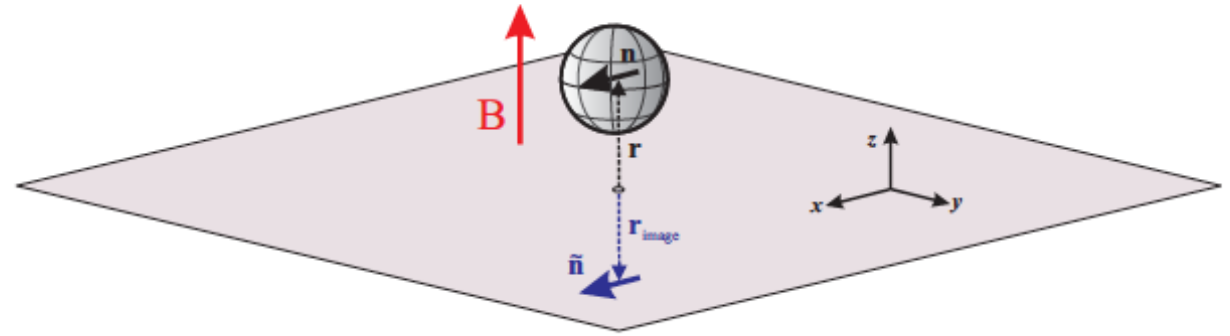
C.F. Gauss, *Intensitas vis magnetica et terrestris ad mensuram absolutam revocata*, Göttingen, 1833

Empirical result: energy resolution limit (ERL) in B-field sensing applies universally.

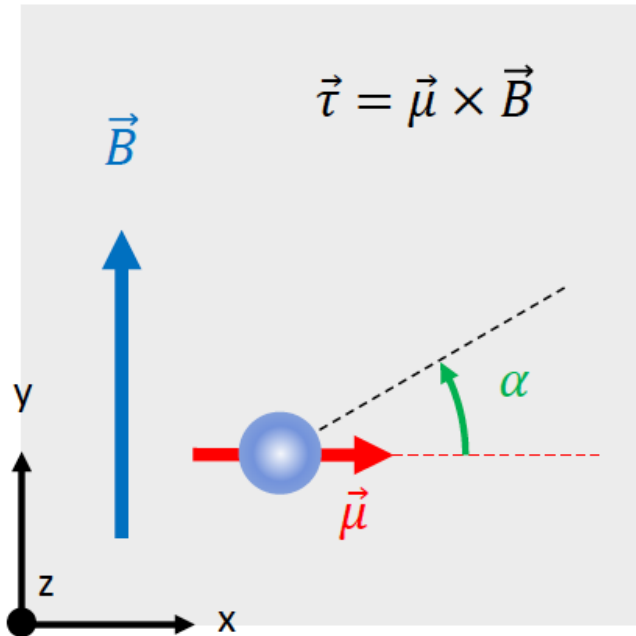


A realization of B-field sensor by ferromagnetic

gyroscope: Precession and nutation motion to probe tiny force, Einstein-de Haas effect



How to evaluate ERL with levitated micromagnets



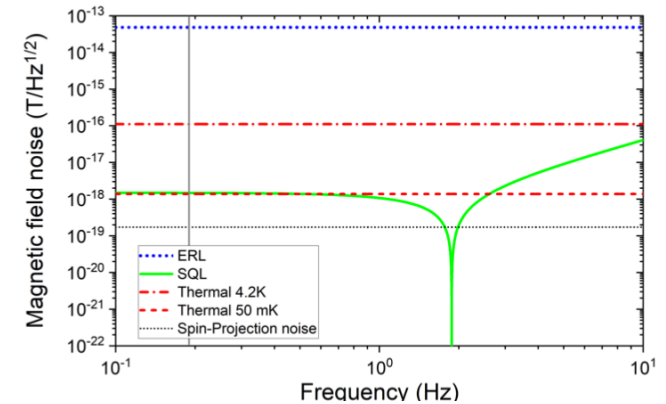
Thermal torque noise:

$$S_{\tau, \text{thermal}} = 4k_B T I \frac{\omega_\alpha}{Q_\alpha}$$

Standard Quantum Limit torque noise:

$$S_{\tau, \text{SQL}} = \frac{4mr^2}{5} \hbar \sqrt{(\omega_\alpha^2 - \omega^2)^2 + \left(\frac{\omega\omega_\alpha}{Q_\alpha}\right)^2}$$

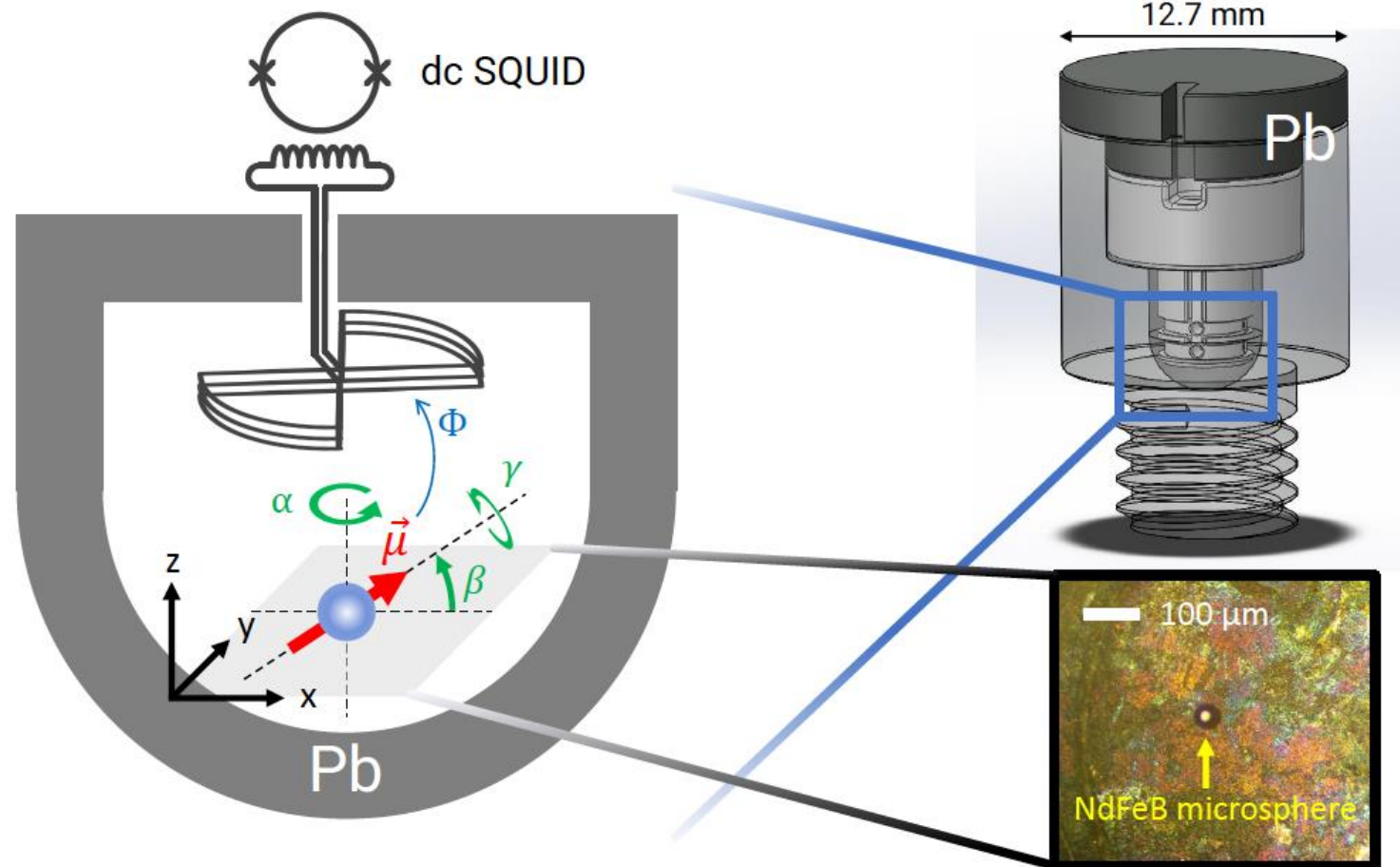
Typical set-up: $S_{\tau, \text{thermal}} \gg S_{\tau, \text{SQL}} @ 4.2 \text{ K}$



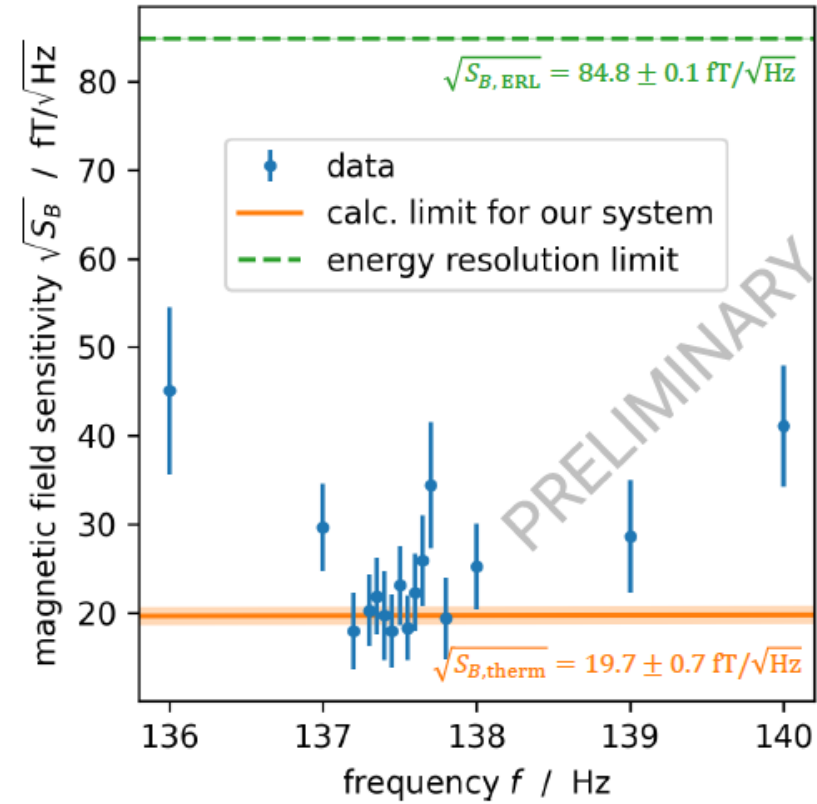
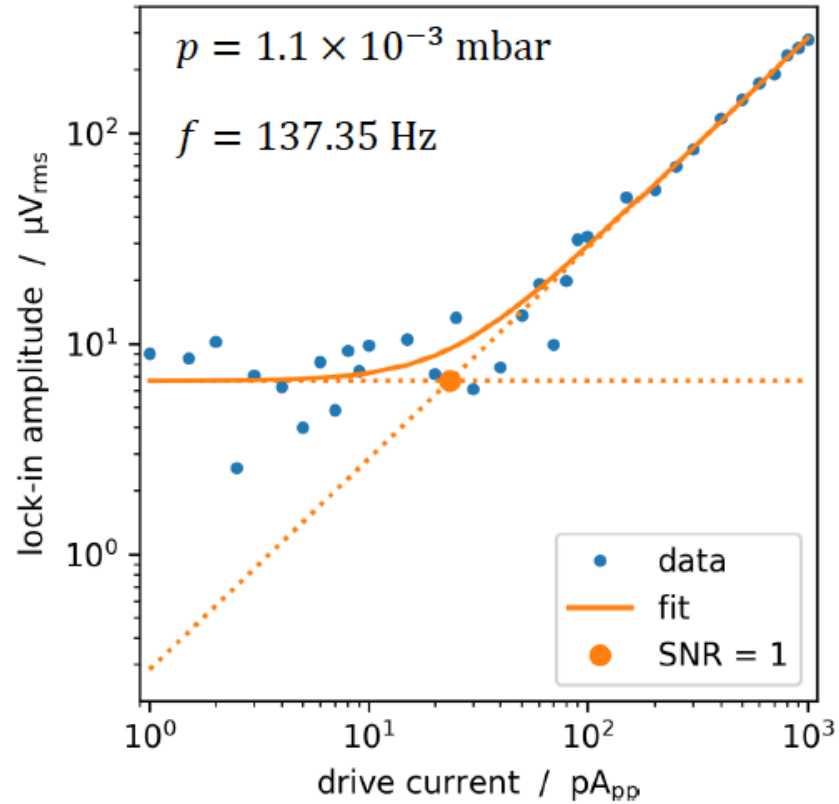
⇒ Magnetic noise: $S_{B, \text{thermal}} = \frac{S_{\tau, \text{thermal}}}{\mu^2} = \frac{12k_B T \rho f_\alpha}{5M^2 r Q_\alpha} \ll S_{B, \text{ERL}}$

Experimental Set-up (in Trento)

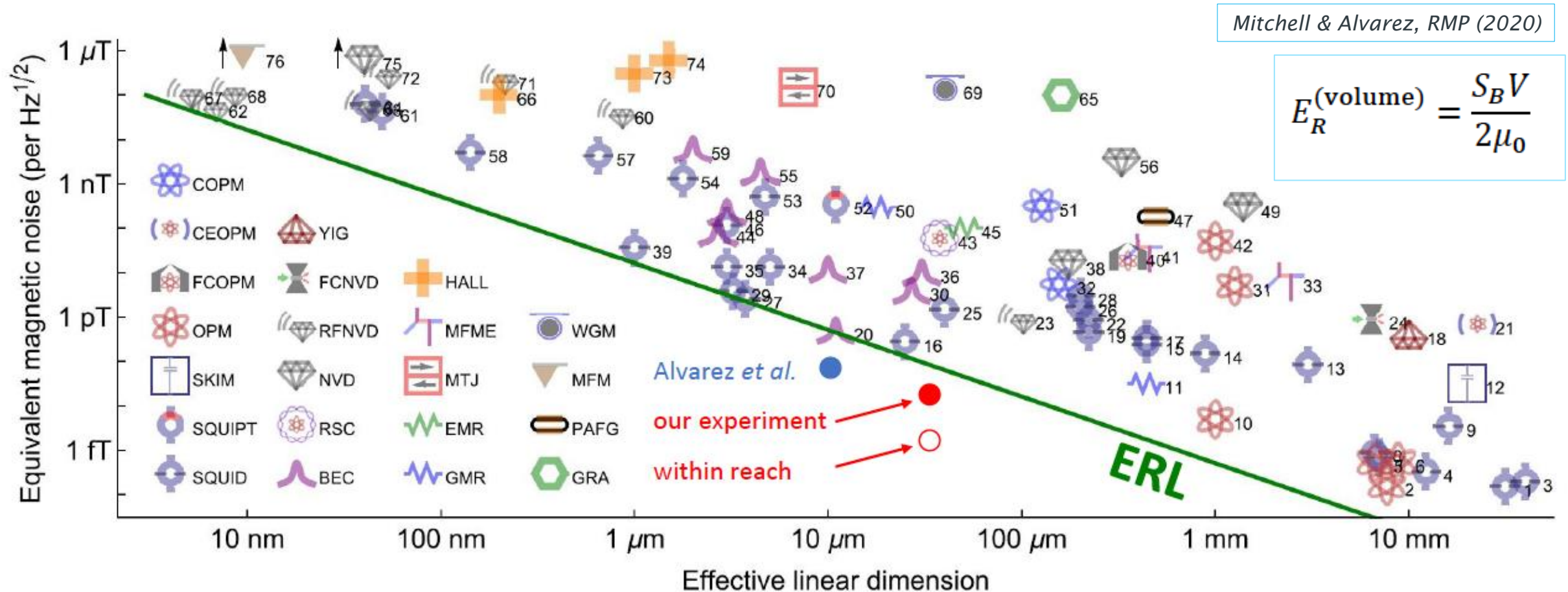
Felix Ahrens & Andrea Vinante



Experimental results: magnetic field sensitivity @ 4K



Experimental result: B-field sensing below ERL



Alvarez et al., *Proc. Natl. Acad. Sci. USA*, 119, e2115339119 (2022)

Ahrens, F., Ji, W., Budker, D., Timberlake, C., Ulbricht, H., & Vinante, A. (2024).

Levitated ferromagnetic magnetometer with energy resolution well below \hbar . *arXiv preprint arXiv:2401.03774*.